



2.6. Student Performance and Learning Outcomes

2.6.1 The institution has stated learning outcomes (Program and Course outcomes), graduate attributes, which are integrated into the assessment process and widely published through the website and other documents, and the attainment of the same is evaluated by institution.



**Sushant
University**

**Sample of course file.Student
notebook.Practical notebook**



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Course Activity Sheet (Planning and Review)

Academic Year: 2024-25

Programme: B. Tech

Semester: I

Course Name: -

Mathematics - I

Course Code:- 23BTC-OMA11T

LTP: 3-1-0

School: School of Engineering & Technology

Faculty: Dr. Manimala

Planning Checklist

S.No	Activity	Status
1	Is the syllabus copy maintained and submitted by the faculty member?	Yes/No
2	Is lecture plan signed and updated by the faculty member?	yes
3	Is previous year question paper made available?	yes
4	Is Time Table made available?	yes
5	Number of Assignments planned	yes 2
6	Number of quiz planned	2
7	Digital Learning LX (LMS – Review) Is it updated with following (suggestive) : Syllabus Reference material Video links Quiz/Assignment	yes
8	Is mapping of students available on ERP along with the timetable?	yes
9	Suggest atleast one innovative way for better engagement of students in this course	More practice set. Day by day assignment. Weekly doubt session

Manimala
(Signature of Faculty Member with Date)

[Signature]
(Signature of Dean with Date)



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Mid-Semester Review

S.No	Activity	Status
1.	Is the attendance updated on ERP?	Yes/No
2.	Percentage of students who are not meeting the attendance criteria of 75%	10%
3.	Pass percentage in Internal Assessment so far	95%
4.	Identification and motivation for toppers Student Roll No Name 1 240BTCCSE018 Harsit Kr. Pandey 2 240BTCCSE046 Kyathika Rao Seelam 3 4	Mention the activities Difficult level questions given
5.	Identification and motivation for weaker students Student RollNo Name 1 240BTCCSE011 Yuvraaj 2 240BTCCSE038 Bhawik Chawla 3 240BTCCSE051 Mayank Rathore 4	Mention the activities More practice questions. One-to-one interaction Peer. guid/help

Dean's Review and recommendations

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(Signature of Faculty Member with Date)

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(Signature of Dean with Date)



End-Semester Review

S.No	Activity	Status
1.	Is the attendance updated on ERP?	Yes/No
2.	Percentage of students who are not meeting the attendance criteria of 75%	0-1
3.	Pass percentage	
4.	Summary of CO attainment CO1 - 2.25 CO2 - 1.65 CO3 - 1.85	sheet attached CO1 - 2.4 CO2 - 1.92 CO3 - 1.68
5.	Student Feedback	
6.	Exit Feedback by faculty member for improvement in future	Will do more practice Set & 1-1 to interaction

Dean's Review

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Maniwala
 (Signature of Faculty Member with Date)

(Signature of Dean with Date)



Timetable w.e.f. 06/November/2024

Teacher Dr. Manirala

Ansul University, Sector 55, Golf Course Road, Gurgaon, Haryana - 122003

		9:10 - 10:00	10:05 - 10:55	11:00 - 11:50	11:55 - 12:45	12:45 - 13:25	13:25 - 14:15	14:20 - 15:10	15:15 - 16:05	16:10 - 17:00	
	1	2	3	4	5	6	7	8	9		
Mo	Mathematics-I	Discrete Mathematics		Discrete Mathematics		Mathematics-I		Mathematics-I			
	B.Tech CSE - Section B (1st Sem)	B.Tech CSE - AI/ ML (3rd Sem)		B.Tech CSE - Cyber (3rd Sem)		B.Tech CSE - Section A (1st Sem)		B.Tech CSE - Cyber (3rd Sem)			
	D-322	D-413A		D-305		D-413A		D-311		D-301	
Tu	Mathematics-I	Mathematics-I		Discrete Mathematics		Discrete Mathematics		Discrete Mathematics		Remedial Class	
	B.Tech CSE - Section B (1st Sem)	B.Tech CSE - Section A (1st Sem)		B.Tech CSE - All ML (3rd Sem)		B.Tech CSE - Cyber (3rd Sem)		B.Tech CSE - Cyber (3rd Sem)		B.Tech CSE - Section A (1st Sem)	
	D-305	D-207		D-413A		D-301		D-311		D-301	
We	Mathematics-I	Discrete Mathematics		Discrete Mathematics		Mathematics-I		Mathematics-I		Remedial Class	
	B.Tech CSE - Section B (1st Sem)	B.Tech CSE - AI ML (3rd Sem)		B.Tech CSE - Cyber (3rd Sem)		B.Tech CSE - Section A (1st Sem)		B.Tech CSE - Cyber (3rd Sem)		B.Tech CSE - Section B (1st Sem)	
	D-322	D-413A		D-301		D-301		D-311		D-301	
Th	Discrete Mathematics	Mathematics-I		Discrete Mathematics		Mathematics-I		Mathematics-I		Mathematics-I	
	B.Tech CSE - AI ML (3rd Sem)	B.Tech CSE - Section B (1st Sem)		B.Tech CSE - Cyber (3rd Sem)		B.Tech CSE - Section A (1st Sem)		B.Tech CSE - Cyber (3rd Sem)		B.Tech CSE - Section B (1st Sem)	
	D-413A	D-322		D-311		D-301		D-301		D-322	
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Course Outline

Course Title: Mathematics I

Semester: I	Academic Year: 2024-25	Core/Elective: Core	Credits: 4, LTP: 3-1-0
Course Designed by: Dr. Manimala E-mail: manimala@sushantuniversity.edu.in		Course Instructor: Dr. Manimala E-mail: manimala@sushantuniversity.edu.in	
Pre-requisites: Basic concept of Matrix, Calculus, Sequence & Series and Trigonometry			

1. Course Outcomes:

Upon successful completion of the course, the students should be able to:

- CO1: Describe matrix algebra to solving engineering problems. Determine the eigenvalues and eigenvectors of a matrix
- CO2: Distinguish between the concepts of sequence and series. Determine convergence and divergence of series. Understand De Moivre's theorem and find the roots of complex numbers. Application of complex numbers for solving engineering problems
- CO3: Understand application of Leibniz's theorem & Taylor's theorem in real life problems. Demonstrate Knowledge of maxima and minima of function of two variables, Understand Homogeneous Function, asymptotes and curve tracing

2. Program Outcomes:

This section deals with how well this course meets the following eight overall program outcomes (POs):

- PO1: Engineering knowledge:** Apply the knowledge of mathematics, science, engineering fundamentals, and engineering. Specialization to the solution of complex engineering problems.
- PO2. Problem analysis:** Identify, formulate, research literature, and analyze engineering problems to arrive at substantiated conclusions using first principles of mathematics, natural, and engineering sciences.
- PO3. Design/development of solutions:** Design solutions for complex engineering problems and design system components, processes to meet the specifications with consideration for the public health and safety, and the cultural, societal, and environmental considerations.
- PO4. Conduct investigations of complex problems:** Use research-based knowledge including design of experiments, analysis and interpretation of data, and synthesis of the information to provide valid conclusions.



Manimala

PO5. Modern tool usage: Create, select, and apply appropriate techniques, resources, and modern engineering and modeling to complex engineering activities with an understanding of the limitations.

PO6. The engineer and society: Apply reasoning informed by the contextual knowledge to assess societal, health, safety, legal, and cultural issues and the consequent responsibilities relevant to the professional engineering practice.

PO7. Environment and sustainability: Understand the impact of the professional engineering solutions in societal and environmental contexts, and demonstrate the knowledge of, and need for sustainable development.

PO8. Ethics: Apply ethical principles and commit to professional ethics and responsibilities and norms of the engineering practice.

PO9. Individual and team work: Function effectively as an individual, and as a member or leader in teams, and in multidisciplinary settings.

PO10. Communication: Communicate effectively with the engineering community and with society at large. Be able to comprehend and write effective reports documentation. Make effective presentations, and give and receive clear instructions.

PO11. Project management and finance: Demonstrate knowledge and understanding of engineering and management principles and apply these to one's own work, as a member and leader in a team. Manage projects in multidisciplinary environments.

PO12. Life-long learning: Recognize the need for, and have the preparation and ability to engage in independent and life-long learning in the broadest context of technological change.

PSO1: Apply standard Software Engineering practices and strategies in real-time software project development using open-source programming environment or commercial environment to deliver quality product for the organization success

PSO2: Design and develop computer programs/computer-based systems in the areas related to algorithms, networking, web design, cloud computing, IoT and data analytics of varying complexity

PSO3: Acquaint with the contemporary trends in industrial/research settings and thereby innovate novel solutions to existing problems

3. CO and PO mapping

	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	H	H	M	L	L	M	L	L	M	L	L	M	M	L	H
CO2	H	M	M	M		M	L	L	L	L	L	M	M	L	M
CO3	H	M	M	M	L	L	L	L	M	L	L	M	L	M	H



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Syllabus:**Total Hrs.: 56****UNIT I- Matrices****Total: 12 hours**

Matrices and its types, Rank of a matrix. Elementary transformations, Echelon-form of a matrix, normal form of a matrix, Inverse of a matrix by elementary transformations (Gauss- Jordan method).

Linear dependence and linear independence of vectors. Solution of system of linear equations. Non-homogeneous linear equations and homogeneous linear equations. Characteristic equation – Eigen values – Eigen vectors – properties of Eigen values. Cayley-Hamilton theorem (without proof). Inverse of a matrix by using Cayley-Hamilton theorem. Modal matrix.

UNIT II – Infinite Series**Total: 10 hours**

Definition of Sequence and series. Convergence of series – comparison test – D'Alemberts Ratio test. Cauchy's Root Test – Integral Test – Raabe's Test – Logarithmic Test –Gauss Test. Alternating series – Absolute convergence – Leibnitz's Rule (without Proof).

UNIT III - Complex Number**Total: 12 hours**

De Moivre's theorem and roots of complex numbers. Expansion of $\sin n\theta$, $\cos n\theta$ and $\tan n\theta$ in powers of $\sin\theta$, $\cos\theta$, $\tan\theta$. Complex exponential function, Complex trigonometry functions, hyperbolic functions, Inverse hyperbolic functions, Logarithm of complex numbers. Summation of trigonometric series.

UNIT IV- Differential Calculus-I**Total: 10 hours**

Successive differentiation, Leibnitz theorem and applications. Taylor's and Maclaurin's series (without Proof). Functions of two or more variables, limit and continuity, partial derivatives. Total differential and differentiability, derivatives of composite and implicit functions.

UNIT V- Differential Calculus-II**Total: 12 hours**

Higher order partial derivatives. Homogeneous functions and applications, Euler's Theorem, Jacobians, Maxima-minima of function of two variables. Lagrange's method of undetermined multipliers. Differentiation under integral sign (Leibnitz rule). Curvature, asymptotes, curve tracing.



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4. Text Book(s):

- T1.** N.P.Bali and Manish Goyal, "A Text book o Engineering Mathematics",Laxmi Publications (P) Limited, 2010.
- T2.** Dr. B. S. Grewal, "A text book of Higher Engineering Mathematics". 40 ed. Khanna Publishers, 2009
- T3.** B.V.Ramana, "A text book of Mathematics",Tata MC Graw Hill, 2009.

5. Reference Book(s):

R1: Kreyszig Erwin, "Advanced Engineering Mathematics", 9th Edition, John Wiley & Sons, 2006.

R2: Peter.V.O.Neil, Advanced Engineering Mathematics. Canada: Thomson, 2007.

R3: R.K.Jain and S.R.K.Iyengar, Advanced Engineering Mathematics. 3 ed, Narosa Publishers, 2009

R4: H. K Dass, "Advanced engineering mathematics", 8th Edition, S. Chand, 2008

R5: Jain Iyengar, "Advanced Engineering Mathematics", 3rd Edition, Narosa Publishers, 2007

6. Evaluation Scheme

Exam Type	Marks Breakup
Mid Semester Examination	15
End Semester Examination	60
Quiz	15
Assignment/Faculty Assessment/Class Participation	10
Total	100

Manish Goyal



School of Engineering & Technology

LESSON PLAN

COURSE OUTLINE

Course Title: Mathematics I

Course Code:- 23BTC-0MA11T

Term: I

Academic Year: 2024-25

Core/Elective:
Core

Credits:
LTP: 3-1-0

Course Designed by:- Dr. Manimala

Course Instructor: Dr. Manimala

Pre-requisites: Basic concept of set theory, permutation & combinations

1. Course Outcomes:

Upon successful completion of the course, the students should be able to

CO1: Describe matrix algebra to solving engineering problems. Determine the eigenvalues and eigenvectors of a matrix

CO2: Distinguish between the concepts of sequence and series. Determine convergence and divergence of series. Understand De Moivre's theorem and find the roots of complex numbers. Application of complex numbers for solving engineering problems

CO3: Understand application of Leibniz's theorem & Taylor's theorem in real life problems. Demonstrate Knowledge of maxima and minima of function of two variables, Understand Homogeneous Function, asymptotes and curve tracing.

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T2. Dr. B. S. Grewal, "A text book of Higher Engineering Mathematics".
40 ed. Khanna Publishers, 2009

T3. B.V.Ramana, "A text book of Mathematics", Tata MC Graw Hill, 2009.



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Reference Books:

- R1: Kreyszig Erwin, "Advanced Engineering Mathematics", 9th Edition, John Wiley & Sons, 2006.
- R2: Peter.V.O.Neil, Advanced Engineering Mathematics. Canada: Thomson, 2007.
- R3: R.K.Jain and S.R.K.Iyengar, Advanced Engineering Mathematics. 3 ed, Narosa Publishers, 2009
- R4: H. K Dass, "Advanced engineering mathematics", 8th Edition, S. Chand, 2008
- R5: Jain Iyengar, "Advanced Engineering Mathematics", 3rd Edition, Narosa Publishers, 2007.

1. Lecture Plan (Total hours -42)

Lectures number	Topics to be covered	UNIT No.	Planned on	Taken on	Methodology used (PPT, White Board, Audio/Video, Practical, Visit, Self Study based)	Deans/p Remarks with Date
1	Matrices and its types, Rank of a matrix	Unit 1	12/08/24	12/10/24	White board	
2	Elementary transformations, Echelon-form of a matrix	Unit 1	13/08/24	13/10/24	White board	
3	normal form of a matrix,	Unit 1	14/08/24	14/10/24	White board	
4	Inverse of a matrix by elementary transformations (Gauss— Jordan method).	Unit 1	15/08/24	15/10/24	White board	
5	Linear dependence and linear independence of vectors	Unit 1	20/08/24	20/10/24	White board	



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6	Solution of system of linear equations. Non-homogeneous linear equations	Unit 1	21/8/24	21/8/24	White board	
7	homogeneous linear equations	Unit 1	22/8/24	22/8/24	White board	
8	Characteristic equation – Eigen values – Eigen vectors	Unit 1	23/8/24	23/8/24	White board	
9	Properties of Eigen values	Unit 1	27/8/24	27/8/24	White board	
10	Cayley- Hamilton theorem (without proof)	Unit 1	28/8/24	28/8/24	White board	
11	Inverse of a matrix by using Cayley-Hamilton theorem.	Unit 1	29/8/24	29/8/24	White board	
12	Modal matrix.	Unit 1	30/8/24	30/8/24	White board	
13	Definition of Sequence and series	Unit 2	02/09/24	02/09/24	White board	
14	Convergence of series	Unit 2	31/9/24	03/09/24	White board	
15	Comparison test	Unit 2	04/09/24	04/09/24	White board	
16	D'Alemberts Ratio test	Unit 2	05/09/24	05/09/24	White board	
17	Cauchy's Root Test	Unit 2	09/09/24	09/09/24	White board	
18	Integral Test	Unit 2	10/09/24	10/09/24	White board	
19	Raabe's Test	Unit 2	11/09/24	11/09/24	White board	



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20	Logarithmic Test	Unit 2	12/9/24	12/9/24	White board
21	Gauss Test.	Unit 2	13/9/24	13/9/24	White board
22	Alternating series	Unit 2	17/9/24	17/9/24	White board
23	Absolute convergence	Unit 2	18/9/24	18/9/24	White board
24	Leibnitz's Rule (without Proof).	Unit 2	19/9/24	19/9/24	White board
25	De Moivre's theorem	Unit 3	23/9/24	23/9/24	White board
26	roots of complex numbers	Unit 3	24/9/24	24/9/24	White board
27	Expansion of $\sin n\theta$, $\cos n\theta$	Unit 3	25/9/24	25/9/24	White board
28	$\tan n\theta$ in powers of $\sin\theta$, $\cos\theta$, $\tan\theta$	Unit 3	26/9/24	26/9/24	White board
29	Complex trigonometry functions	Unit 3	29/9/24	29/9/24	White board
30	hyperbolic functions	Unit 3	30/9/24	30/9/24	White board
31	Inverse hyperbolic functions	Unit 3	1/10/24	01/10/24	White board
32	Logarithm of complex numbers	Unit 3	31/10/24	31/10/24	White board
33	Summation of trigonometric series.	Unit 3	41/10/24	01/10/24	White board

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34	Successive differentiation	Unit 4	9/10/24	9/10/24	White board
35	Leibnitz theorem	Unit 4	8/10/24	8/10/24	White board
36	Leibnitz theorem and applications	Unit 4	9/10/24	9/10/24	White board
37	Taylor's and Maclaurin's series (without Proof)	Unit 4	10/10/24	10/10/24	White board
38	Functions of two or more variables	Unit 4	11/10/24	11/10/24	White board
39	limit and continuity	Unit 4	10/10/24	16/10/24	White board
4 0	Partial derivatives.	Unit 4	12/10/24	12/10/24	White board
4 1	Total differential	Unit 4	13/11/24	13/11/24	White board
4 2	Differentiability	Unit 4	11/11/24	11/11/24	White board
4 3	Derivatives of composite	Unit 4	12/11/24	12/11/24	White board
4 4	implicit functions	Unit 4	13/11/24	12/11/24	White board
4 5	Higher order partial derivatives	Unit 5	13/11/24	13/11/24	White board
4 6	Homogeneous functions	Unit 5	14/11/24	14/11/24	White board
4 7	Homogeneous functions and applications	Unit 5	22/11/24	22/11/24	White board
4 8	Euler's Theorem	Unit 5	23/11/24	23/11/24	White board



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4 9	Jacobians	Unit 5	<i>26/11/24</i>	<i>27/11/24</i>	White board	
5 0	Maxima-minima of function of two variables	Unit 5	<i>26/11/24</i>	<i>26/11/24</i>	White board	
5 1	Lagrange's method of undetermined multipliers	Unit 5	<i>27/11/24</i>	<i>26/11/24</i>	White board	
5 2	Differentiation under integral sign (Leibnitz rule)	Unit 5	<i>28/11/24</i>	<i>28/11/24</i>	White board	
5 3	Curve tracing.	Unit 5	<i>29/11/24</i>	<i>27/11/24</i>	White board	
5 4	Curvature	Unit 5	<i>29/11/24</i>	<i>27/11/24</i>	White board	
55 56 5	Asymptotes	Unit 5	<i>30/11/24</i>	<i>28/11/24</i>	White board	

Total = 56 Lectures

Signature of faculty

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School of Engineering & Technology, Sushant University

Odd Semester (August-December) 2024

Students List

Program: B.Tech

Sem: I

Course Name: Mathematics I

Course Code: 23BTC-0MA11T

Faculty: Dr. Manimala

Total No. of Students enrolled in the course: 103

Student Name	Roll No
AARTI NEGI	240BTCCSE029
AARYAN KASHYAP	240BTCCSE033
AASHI THAKRAN	240BTCCSE020
ABHINAV RANGA	240BTCCSE087
ADITYA CHAUDHARY	240BTCCSE091
AKSHAT SHUKLA	240BTCCSE007
AKSHIT MATHUR	240BTCCSE079
ANKIT NAGAR	240BTCCSE081
Anuj kumar	240BTCCSE115
ANUPRIYA	240BTCCSE077
ARAV	240BTCCSE043
ARKISH DAHIYA	240BTCCSE032
ARMAAN SAIFI	240BTCCSE062
ARPIT KUMAR	240BTCCSE023
ARYAN KUMAR	240BTCCSE063
ARYAN NAPIT	240BTCCSE016
ASHANK SHARMA	240BTCCSE053
ASHISH KUMAR SHARMA	240BTCCSE047
ASTIK GUPTA	240BTCCSE008
ATHARV MALIK	240BTCCSE059
AVNISH	240BTCCSE054
AYESHA GUPTA	240BTCCSE009
BHAVIK	240BTCCSE038
BHAVIK CHAWLA	240BTCCSE038
DEEKSHA SORAJ	240BTCCSE080
DEEPAK PHOGAT	240BTCCSE109
DHRUV	240BTCCSE022
DHRUV YADAV	240BTCCSE108



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Dishant	240BTCCSE106
DIVYANSH Kaushik	240BTCCSE066
DIVYANSHU RANA	240BTCCSE057
DRISHIKA ANEJA	240BTCCSE003
FAIZAN KHAN	240BTCCSE044
HARSH SHARMA	240BTCCSE065
HARSHIT CHHILLAR	240BTCCSE026
HARSHIT KUMAR PANDEY	240BTCCSE018
HIMANSHU KUMAR CHAUDHARY	240BTCCSE030
JAI KUMAR JHA	240BTCCSE036
JATIN RANA	240BTCCSE089
JAYANT GAUR	240BTCCSE017
KANISHK GAUR	240BTCCSE013
KANISHKA	240BTCCSE042
KANISHKA SRIVASTAVA	240BTCCSE037
KAUSHAL YADAV	240BTCCSE078
KRISHNA GEMINI	240BTCCSE069
KRRISH SHARMA	240BTCCSE090
KUMAR ANKIT	240BTCCSE117
Kumar Aryan	240BTCCSE055
KUNAL JOON .	240BTCCSE050
KYATHIKA RAO SEELAM	240BTCCSE046
LAKSHITA	240BTCCSE119
MANAN KOCHAR	240BTCCSE113
MAYANK KAUSHIK	240BTCCSE012
MAYANK RATHORE	240BTCCSE051
MAYANK SHARMA	240BTCCSE070
MOHD HAMZA	240BTCCSE085
MOHIT	240BTCCSE014
NARESH KUMAR	240BTCCSE025
NEERAJ RANA	240BTCCSE118
NIHAL	240BTCCSE001
NIKHIL PATEL	240BTCCSE021
PALAK SHRIVASTAV	240BTCCSE024
PARINEETA	240BTCCSE048
Payal Yadav	240BTCCSE136
PIYUSH CHOUBEY	240BTCCSE005
POORAV YADAV	240BTCCSE076
PRAGYA	240BTCCSE071
PRASHANT SHARMA	240BTCCSE028
PRINCE BHARDWAJ	240BTCCSE004



Aman Patel

RAHUL SEHRAWAT	240BTCCSE107
RAJ ARYAN	240BTCCSE116
RISHI	240BTCCSE121
RITESH KUMAR	240BTCCSE060
RITESH MAAN	240BTCCSE052
ROSSANE HENRICK	240BTCCSE002
RUPESH	240BTCCSE088
SAARA TEWATHIA	240BTCCSE006
SAMEER PAHWA	240BTCCSE086
SAMEER VATS	240BTCCSE093
SANA GHOSH	240BTCCSE058
SANJEEV KUMAR	240BTCCSE074
SARTHAK MEHTA	240BTCCSE040
SARTHAK PANDAY	240BTCCSE056
Shiv Kumar Ray	240BTCCSE084
SHUBHAM LOHIA	#N/A
SHUBHAM TANWAR	240BTCCSE114
SOHAM VERMA	240BTCCSE010
SRITARA	240BTCCSE092
SUHANI	240BTCCSE039
TAKSH ROOP	240BTCCSE015
TANISHKA GUPTA	240BTCCSE049
TANIYA MALIK	240BTCCSE075
UNNATI	240BTCCSE067
VARSHA	240BTCCSE035
Vipin Singh Yadav	240BTCCSE083
YASH	240BTCCSE134
YASH KUMAR	240BTCCSE031
YASH YADAV	240BTCCSE034
YUVANSH	240BTCCSE011



Manusala

Study Material:- Mathematics - I (23BTC-OMA/IIT)

https://drive.google.com/drive/folders/1YmixQZiB-IQ7sXvBVZhKMtaghBPQQp8?usp=drive_link

1. Books
2. Recorded lectures
3. Class Notes
4. Assignment
5. Quiz.

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Eigenvalues & Eigenvectors

Let $A = [a_{ij}]_{n \times n}$ be a square matrix of order n , I an unit matrix of order n & λ an indeterminate. Then the matrix

$$A - \lambda I = \begin{vmatrix} a_{11} - \lambda & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} - \lambda & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nn} \\ a_{n1} & a_{n2} & \cdots & a_{nn} \end{vmatrix} - \lambda \begin{vmatrix} 1 & 0 & 0 & \cdots & 0 \\ 0 & 1 & 0 & \cdots & 0 \\ 0 & 0 & 1 & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & 0 & \cdots & 1 \end{vmatrix}$$

is called the characteristic matrix of A & the determinant

$$|A - \lambda I| = \begin{vmatrix} a_{11} - \lambda & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} - \lambda & \cdots & a_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nn} \end{vmatrix}$$

is called the characteristic

polynomial of λ .

Also the equation $|A - \lambda I| = 0$ is called the characteristic equation of A . The roots of this eqn. are called characteristic roots or characteristic values or eigen values or eigen roots or latent roots of the matrix.

If λ is a characteristic roots of a non matrix A , then the non zero soln.

of the eqn. $AX = \lambda X$ i.e. $(A - \lambda I)X = 0$ is called the characteristic vector or eigen vector of the

matrix A corresponding to the characteristic root).

Some Important properties of Eigenvalues :-

- (a) Any matrix A & its transpose both have the same eigen values.
- (b) The trace of the matrix equals to the sum of the eigen values of a matrix.

Note :- The sum of the elements on the principal diagonal of a matrix is called the trace of the matrix.

- (c) The determinant of the matrix A equals to the product of the eigen values of A .

(i) If $\lambda_1, \lambda_2, \dots, \lambda_n$ are n -eigen values of A , then

(ii) Eigen values of kA are $k\lambda_1, k\lambda_2, \dots, k\lambda_n$.

(iii) Eigen values of A^{-1} are $\frac{1}{\lambda_1}, \frac{1}{\lambda_2}, \dots, \frac{1}{\lambda_n}$.

(iv) Eigen values of A^m are $\lambda_1^m, \lambda_2^m, \dots, \lambda_n^m$.

(v) If λ is an eigen value of a matrix A , then $\frac{1}{\lambda}$ is the eigen value of A^{-1} .

(vi) If $\lambda_1, \lambda_2, \dots, \lambda_n$ are eigen values of a matrix A , then A^m has the eigen values $\lambda_1^m, \lambda_2^m, \dots, \lambda_n^m$, m being a non integer.

Ward



Q1 The matrix A is defined as $A = \begin{bmatrix} 1 & 2 & -3 \\ 0 & 3 & 2 \\ 0 & 0 & -2 \end{bmatrix}$
 Find the eigenvalues of $3A^3 + 5A^2 - 6A + 25$.
 To ch. eqn. of given matrix is
Soln $|A - \lambda I| = 0$

$$\begin{vmatrix} 1-\lambda & 2 & -3 \\ 0 & 3-\lambda & 2 \\ 0 & 0 & -2-\lambda \end{vmatrix} = 0$$

$$(1-\lambda)(5-\lambda)(2-\lambda) = 0 \Rightarrow \lambda = 1, 3, -2$$

eigenvalues of $A^3 = 1, 27, -8$

" " $A^2 = 1, 9, 4$

" " $A = 1, 3, -2$

" " $I = 1, 1, 1$

∴ eigenvalues of $3A^3 + 5A^2 - 6A + 25$

$$1^{\text{st}} \text{ eigenvalue} = 3(1)^3 + 5(1)^2 - 6 \cdot 1 + 2 \cdot 1 = 3 + 5 - 6 + 2 = 4$$

$$2^{\text{nd}} \text{ eigenvalue} = 3(27) + 5(9) - 6 \cdot 3 + 2 \cdot 1 = 110$$

$$3^{\text{rd}} \text{ eigenvalue} = 3(-8) + 5(4) - 6(-2) + 2 \cdot 1 = 10$$

∴ Required eigenvalues are 4, 110, 10

Q2 Show that for any square matrix A, the product of all the eigenvalues of A is equal to $\det(A)$, and the sum of all the eigenvalues of A is equal to the sum of the diagonal elements.

Soln Let $A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$ $|A - \lambda I| = \begin{vmatrix} a_{11} - \lambda & a_{12} & a_{13} \\ a_{21} & a_{22} - \lambda & a_{23} \\ a_{31} & a_{32} & a_{33} - \lambda \end{vmatrix}$

$$|A - \lambda I| = -\lambda^3 + \lambda^2(a_{11} + a_{22} + a_{33}) + \lambda \{-a_{11}a_{22} - a_{11}a_{33} + a_{22}a_{33}\} +$$

$$+ (a_{11}(a_{22}a_{33} - a_{23}a_{32}) + a_{12}(a_{11}a_{33} - a_{13}a_{31}) + a_{13}(a_{11}a_{22} - a_{12}a_{21}))$$

If $\lambda_1, \lambda_2, \lambda_3$ be the roots of eq: ① then
 Sum of roots = $\lambda_1 + \lambda_2 + \lambda_3 = a_{11} + a_{22} + a_{33} = \text{Sum of roots}$
 Product of roots
 $\lambda_1 \lambda_2 \lambda_3 = [a_{11}(a_{22}a_{33} - a_{23}a_{32}) - a_{12}(a_{21}a_{33} - a_{23}a_{31}) + a_{13}(a_{21}a_{32} - a_{31}a_{22})]$

Q Prove that a matrix A & its transpose A' have the same characteristic roots.

Soln Characteristic eqn of matrix A is

$$(A - \lambda I) = 0 \quad \text{--- ①}$$

Ch. eqn. of matrix A' is

$$(A' - \lambda I) = 0 \quad \text{--- ②}$$

Clearly both ① & ② are same as we know that $|IA| = |A'|$ & a determinant remains unchanged when rows are changed into columns & columns into rows.

Q Show that characteristic roots of triangular matrix are just the diagonal elements of the matrix.

Soln Let us consider 4×4 triangular matrix

$$A = \begin{bmatrix} a_{11} & 0 & 0 & 0 \\ a_{21} & a_{22} & 0 & 0 \\ a_{31} & a_{32} & a_{33} & 0 \\ a_{41} & a_{42} & a_{43} & a_{44} \end{bmatrix}$$

$$\text{Ch. eqn. is } (A - \lambda I) = 0 \quad \begin{vmatrix} a_{11} - \lambda & 0 & 0 & 0 \\ a_{21} & a_{22} - \lambda & 0 & 0 \\ a_{31} & a_{32} & a_{33} - \lambda & 0 \\ a_{41} & a_{42} & a_{43} & a_{44} - \lambda \end{vmatrix} = 0$$

On expansion it gives $(a_{11} - \lambda)(a_{22} - \lambda)(a_{33} - \lambda)(a_{44} - \lambda) = 0$
 which are diagonal elements of $a_{11}, a_{22}, a_{33}, a_{44}$.

Find the eigen values & eigenvectors of the matrix $A = \begin{bmatrix} 5 & 4 \\ 1 & 2 \end{bmatrix}$

Soln. - The characteristic eqn. of the given matrix is

$$A \cdot \lambda I - 0$$

$$\therefore \begin{vmatrix} 5-\lambda & 4 \\ 1 & 2-\lambda \end{vmatrix} = 0$$

$$\therefore (5-\lambda)(2-\lambda) - 4 = 0$$

$$\therefore 10 - 5\lambda - 2\lambda + \lambda^2 - 4 = 0$$

$$\therefore \lambda^2 - 7\lambda + 6 = 0 \Rightarrow (\lambda-6)(\lambda-1) = 0$$

$$\therefore \lambda = 6, 1$$

∴ eigen values of A are 1 & 6

If x_1, x_2 be the component of an eigen vector corresponding to the eigen value λ , then

$$[A - \lambda I]x = \begin{bmatrix} 5-\lambda & 4 \\ 1 & 2-\lambda \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = 0$$

(i) when $\lambda = 6$, the corresponding eigen vector is given by

$$\begin{bmatrix} 5-6 & 4 \\ 1 & 2-6 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = 0$$

$$\therefore \begin{bmatrix} -1 & 4 \\ 4 & -4 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = 0$$

which gives only one independent eqn.

$$\therefore -x_1 + 4x_2 = 0$$

$\therefore x_1 = 4x_2$ given the eigen vector $\begin{pmatrix} 4 \\ 1 \end{pmatrix}$

$$\frac{x_1}{4} = k \quad \text{eigen vector } \begin{pmatrix} 4k \\ k \end{pmatrix}$$

(ii) when $\lambda = 1$, the corresponding eigen vector is $\begin{pmatrix} 1 \\ 1 \end{pmatrix}$

$$\begin{bmatrix} 5-1 & 4 \\ 1 & 2-1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = 0$$

$$\begin{bmatrix} 4 & 4 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = 0$$

which gives only independent eqn.

$$x_1 + x_2 = 0$$

$$\frac{x_1}{1} = \frac{x_2}{-1} \text{ i.e. giving the}$$

or eigen vector $(1, -1)$

Q. Find the eigen values & eigen vector of matrix

$$A = \begin{bmatrix} 3 & 1 & 4 \\ 0 & 2 & 8 \\ 0 & 0 & 5 \end{bmatrix}$$

The characteristic eqn. of the given matrix is

$$|A - \lambda I| = 0$$

$$\begin{vmatrix} 3-\lambda & 1 & 4 \\ 0 & 2-\lambda & 6 \\ 0 & 0 & 5-\lambda \end{vmatrix} = 0$$

$$\lambda(3-\lambda)(2-\lambda)(5-\lambda) = 0$$

$$\lambda = 0, 2, 3, 5$$

Thus the eigen values of A are 0, 2, 3, 5.

(i) Corresponding to $\lambda = 2$ the

(ii) when $\lambda = 2$, the corresponding eigen vector is given by

$$\begin{bmatrix} 3-2 & 1 & 4 \\ 0 & 2-2 & 6 \\ 0 & 0 & 5-2 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

Assignment –Odd Semester (August-December) 2024

Program: B.Tech

Semester: I

Course Name: Mathematics I

Course Code: 23BTCCSE0MA11T

Faculty: Dr. Manimala

Maximum Marks: 10

Submission Deadline:

Course Outcomes

CO1: Describe matrix algebra to solving engineering problems. Determine the eigenvalues and eigenvectors of a matrix.

CO2: Distinguish between the concepts of sequence and series. Determine convergence and divergence of series. Understand De Moivre's theorem and find the roots of complex numbers. Application of complex numbers for solving engineering problems.

CO3: Understand application of Leibniz's theorem & Taylor's theorem in real life problems. Demonstrate Knowledge of maxima and minima of function of two variables, Understand Homogeneous Function.

Q1 (CO1).

Find the rank of matrix $A = [3 \ -1 \ 2 \ -6 \ 2 \ 4 \ -3 \ 1 \ 2]$ by reducing it in normal form.

Q (CO 2)

Define absolutely convergence & conditionally convergence of an infinite series .Test the following series for convergence and absolutely convergence:

$$\frac{1}{1.3} - \frac{1}{2.4} + \frac{1}{3.5} - \frac{1}{4.6} + \dots \dots \dots \infty$$

Q3 (CO 2)

Show that the nth roots of unity are given by $1, \gamma, \gamma^2, \gamma^3, \dots, \gamma^{n-1}$ where $\gamma = \cos \frac{2\pi}{n} + i \sin \frac{2\pi}{n}$ and

that the continued product of all the nth roots is $(-1)^{n+1}$.

Q4 (CO 3)

If $u = x^2 \sin \frac{y}{x}$, find $\frac{\partial u}{\partial x}$ & $\frac{\partial u}{\partial y}$.

Q5 (CO 1)

Solve the following system of equation by matrix method:

$$x + y + z = 1, \quad 2x - y + z = 4, \quad x - 3y - 2z = 2.$$

Q6 (CO 1)

Find the eigen values and the corresponding eigen vectors of the matrix $A = [3 \ 1 \ 4 \ 0 \ 2 \ 0 \ 0 \ 0 \ 5]$.

Q7 (CO 1)

Find the characteristic equation of the matrix $A = [2 \ 1 \ 1 \ 0 \ 1 \ 0 \ 1 \ 1 \ 2]$ and hence, find the matrix represented by $A^8 - 5A^7 + 7A^6 - 3A^5 + A^4 - 5A^3 + 8A^2 - 2A + I$.

Q8 (CO 3)

State Leibnitz's Theorem. If $y = (\sin^{-1} x)^2$, prove that $(1 - x^2)y_{n+2} - (2n + 1)xy_{n+1} - n^2 y_n = 0$.



Manimala

Q9 (CO 3)

If $u = \tan^{-1} \frac{x^3 + y^3}{x - y}$, prove that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \sin 2u$.

Q10(CO 2)

Test the convergence of the series : $\sum_{n=1}^{\infty} \frac{(n+1)^n x^n}{n^{n+1}}$.

Q11(CO 2)

Test the convergence of the series : $\frac{1}{2} + \frac{1}{3} + \frac{1}{5} + \dots + \frac{1}{2^{n-1} + 1} + \dots$

Q12 (CO1)

Use Gauss Jordan method to find the inverse of the matrix $A = [1 2 5 | 2 3 1 | - 1 1 1]$.

Q13 (CO2)

Find the different values of $(1 + i)^{\frac{1}{3}}$.

Mains



SUSHANT UNIVERSITY, GURGAON

QUIZ 1

15BTC-1MA12T: Engineering Mathematics I

Program: B. Tech (all branch)

Semester: 1st

Time: 40 min.

Max Marks: 15

Instructions: Question 1 is compulsory. Attempt any two questions from Q2 to Q4.

Q1. Find the eigen values and eigen vectors of the matrix $A = \begin{bmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{bmatrix}$. (5 marks) C01

Q2. Using Gauss Jordan method , find the inverse of the given matrix A, C02

where $A = \begin{bmatrix} 2 & 1 & -1 \\ 0 & 2 & 1 \\ 5 & 2 & -3 \end{bmatrix}$. (5 marks)

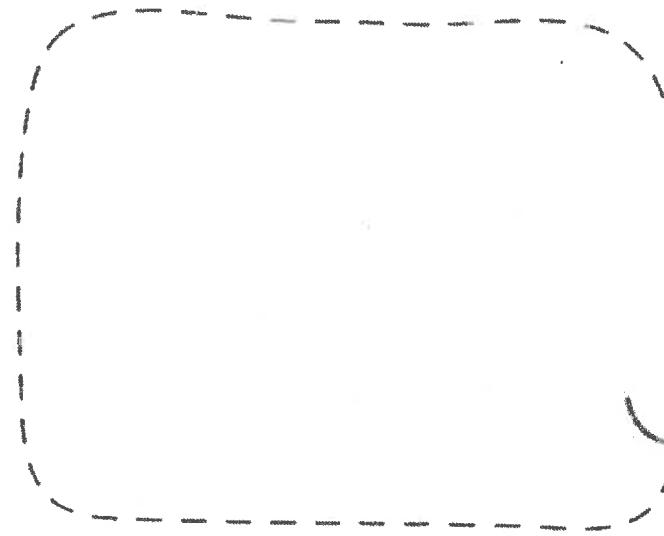
Q3. Find the rank of given matrix $\begin{bmatrix} 8 & 1 & 3 & 6 \\ 0 & 3 & 2 & 2 \\ -8 & -1 & -3 & 4 \end{bmatrix}$ reducing it in normal form (5 marks) C03

Q4. Are the following vectors linearly dependent? If so, find a relation between them C04

$x_1 = (1,2,1), \quad x_2 = (2,1,4), \quad x_3 = (4,5,6)$ (5 marks)

Answered





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NAME

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Sec - B

ADDRESS Roll No - 240BTCCSE067

MOBILE

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EMERGENCY CONTACT

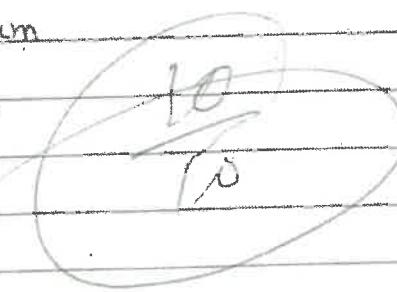
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Assignment - 1

Soln → Reduce to triangular form

i)
$$\left[\begin{array}{ccc} 3 & -4 & -5 \\ -9 & 1 & 4 \\ -5 & 3 & 1 \end{array} \right]$$



10
10

Soln $R_2 \rightarrow R_2 + 3R_1$

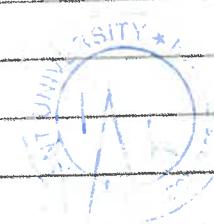
$$\left[\begin{array}{ccc} 3 & -4 & -5 \\ 0 & -11 & -11 \\ -5 & 3 & 1 \end{array} \right]$$

$R_3 \rightarrow R_3 + \frac{5}{3}R_1$

$$\left[\begin{array}{ccc} 3 & -4 & -5 \\ 0 & -11 & -11 \\ 0 & -11/3 & -22/3 \end{array} \right]$$

$R_3 \rightarrow R_3 - \frac{1}{3}R_2$

$$\left[\begin{array}{ccc} 3 & -4 & -5 \\ 0 & -11 & -11 \\ 0 & 0 & -11/3 \end{array} \right]$$



ii)
$$\left[\begin{array}{ccc} 2 & 3 & -1 \\ 0 & -3 & 2 \\ -5 & 3 & 7 \end{array} \right]$$

$R_3 \rightarrow R_3 + \frac{5}{2}R_1$



11

$$R_2 \rightarrow R_2 - R_1$$

$$\left[\begin{array}{ccc|c} 8 & 4 & 3 & \\ 0 & 0 & 1 & \\ 0 & 3 & 3 & \end{array} \right] = \left[\begin{array}{ccc|c} 1 & 0 & 0 & A \\ -1 & 4 & 0 & \\ 0 & -1 & 2 & \end{array} \right]$$

$$R_2 \rightarrow R_2 + R_3$$

$$R_3 \rightarrow R_3 - R_2$$

$$\left[\begin{array}{ccc|c} 8 & 4 & 3 & \\ 0 & 3 & 4 & \\ 0 & 0 & -1 & \end{array} \right] = \left[\begin{array}{ccc|c} 1 & 0 & 0 & A \\ -1 & 3 & 2 & \\ 1 & -4 & 0 & \end{array} \right]$$

$$R_1 \rightarrow R_1 + 3R_2$$

$$R_2 \rightarrow R_2 + 4R_3$$

$$\left[\begin{array}{ccc|c} 8 & 4 & 0 & \\ 0 & 3 & 0 & \\ 0 & 0 & -1 & \end{array} \right] = \left[\begin{array}{ccc|c} 4 & -12 & 0 & A \\ 3 & -13 & 2 & \\ 1 & -4 & 0 & \end{array} \right]$$

$$R_1 \rightarrow R_1 - \frac{4}{3} R_2$$

$$\left[\begin{array}{ccc|c} 8 & 0 & 0 & \\ 0 & 3 & 0 & \\ 0 & 0 & -1 & \end{array} \right] = \left[\begin{array}{ccc|c} 0 & 16/3 & -8/3 & A \\ 3 & -13 & 2 & \\ 1 & -4 & 0 & \end{array} \right]$$

$$R_1 \rightarrow 1/8 R_1, R_2 \rightarrow 1/3 R_2, R_3 = -R_3$$

$$\left[\begin{array}{ccc|c} 1 & 0 & 0 & \\ 0 & 1 & 0 & \\ 0 & 0 & 1 & \end{array} \right] = \left[\begin{array}{ccc|c} 0 & 2/3 & -1/3 & A \\ 1 & -13/3 & 2/3 & \\ -1 & 4 & 0 & \end{array} \right]$$

$$A^{-1} = \left[\begin{array}{ccc} 0 & 2/3 & -1/3 \\ 1 & -13/3 & 2/3 \\ -1 & 4 & 0 \end{array} \right]$$

— / /

$$A^{-1} = \begin{bmatrix} 3 & -1 & 1 \\ -15 & 6 & -5 \\ 5 & -2 & 2 \end{bmatrix}$$

iii)

$$\left[\begin{array}{ccc} 2 & 1 & -1 \\ 0 & 2 & 1 \\ 5 & 2 & 3 \end{array} \right]$$

$$\left[\begin{array}{ccc|c} 2 & 1 & -1 & 1 \\ 0 & 2 & 1 & 0 \\ 5 & 2 & 3 & 0 \end{array} \right] = \left[\begin{array}{ccc|c} 1 & 0 & 0 & A \\ 0 & 1 & 0 & \\ 0 & 0 & 1 & \end{array} \right]$$

$R_1 \rightarrow 1/R_1$

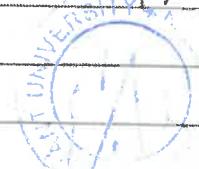
$R_3 \rightarrow R_3 - 5R_1$

$$\left[\begin{array}{ccc|c} 1 & 1/2 & -1/2 & 1 \\ 0 & 2 & 1 & 0 \\ 0 & -1/2 & -1/2 & -5/2 \end{array} \right] = \left[\begin{array}{ccc|c} 1/2 & 0 & 0 & A \\ 0 & 1 & 0 & \\ -5/2 & 0 & 1 & \end{array} \right]$$

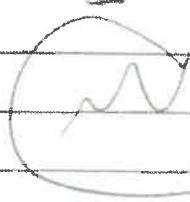
$R_2 \rightarrow 1/R_2, R_1 \rightarrow R_1 - 1/2 R_2, R_3 \rightarrow R_3 + 1/2 R_2$

$$\left[\begin{array}{ccc|c} 1 & 0 & -3/4 & 1/2 \\ 0 & 1 & 1/2 & 0 \\ 0 & 0 & -1/4 & -5/2 \end{array} \right] = \left[\begin{array}{ccc|c} 1/2 & -1/4 & 0 & A \\ 0 & 1/2 & 0 & \\ -5/2 & -1/4 & 1 & \end{array} \right]$$

$R_3 \rightarrow -4R_3$



$$\left[\begin{array}{ccc|c} 1 & 0 & -3/4 & 1/2 \\ 0 & 1 & 1/2 & 0 \\ 0 & 0 & 1 & 10 \end{array} \right] = \left[\begin{array}{ccc|c} 1/2 & -1/4 & 0 & A \\ 0 & 1/2 & 0 & \\ 10 & -1 & -4 & \end{array} \right]$$



— / /

$$R_3 \rightarrow -\frac{1}{4} R_3$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 3 \\ 0 & 1 & -3 \\ 0 & 0 & 1 \end{array} \right] = \left[\begin{array}{ccc|c} 1 & 0 & 0 \\ -\frac{1}{2} & \frac{1}{2} & 0 \\ -\frac{1}{4} & -\frac{1}{4} & -\frac{1}{4} \end{array} \right] A$$

$$R_1 \rightarrow R_1 - 3R_3, R_2 \rightarrow R_2 + 3R_3$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array} \right] = \left[\begin{array}{ccc|c} \frac{7}{4} & \frac{3}{4} & \frac{3}{4} \\ -\frac{5}{4} & -\frac{1}{4} & -\frac{3}{4} \\ -\frac{1}{4} & -\frac{1}{4} & -\frac{1}{4} \end{array} \right] A$$

$$R_1 \rightarrow R_1 - R_2$$

$$\left[\begin{array}{ccc|c} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array} \right] = \left[\begin{array}{ccc|c} 3 & 1 & \frac{3}{2} \\ -\frac{5}{4} & -\frac{1}{4} & -\frac{3}{4} \\ -\frac{1}{4} & -\frac{1}{4} & -\frac{1}{4} \end{array} \right]$$

$$A^{-1} = \left[\begin{array}{ccc|c} 3 & 1 & \frac{3}{2} \\ -\frac{5}{4} & -\frac{1}{4} & -\frac{3}{4} \\ -\frac{1}{4} & -\frac{1}{4} & -\frac{1}{4} \end{array} \right]$$

ii)

$$\left[\begin{array}{ccc|c} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{array} \right]$$



$$\left[\begin{array}{ccc|c} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{array} \right] = \left[\begin{array}{ccc|c} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array} \right] A$$

$$R_1 \rightarrow R_1 - R_2, R_2 \rightarrow R_2 - 4R_3$$

$$\left[\begin{array}{ccc|c} 1 & 2 & 5 \\ 0 & -1 & -9 \\ 0 & 3 & 6 \end{array} \right] = \left[\begin{array}{ccc|c} 1 & 0 & 0 \\ -2 & 1 & 0 \\ 1 & 0 & 1 \end{array} \right] A$$

$$R_2 \rightarrow -R_2$$

$$R_3 \rightarrow 1/3 R_3$$

$$\left[\begin{array}{ccc|c} 1 & 2 & 5 \\ 0 & 1 & 9 \\ 0 & 1 & 2 \end{array} \right] = \left[\begin{array}{ccc|c} 1 & 0 & 0 \\ 2 & -1 & 0 \\ 1/3 & 0 & 1/3 \end{array} \right] A$$

$$R_1 \rightarrow R_1 - 2R_2 \quad , \quad R_3 \rightarrow R_3 - R_2$$

$$\left[\begin{array}{ccc|c} 1 & 0 & -13 \\ 0 & 1 & 9 \\ 0 & 0 & -7 \end{array} \right] = \left[\begin{array}{ccc|c} -3 & 2 & 0 \\ 2 & -1 & 0 \\ -5/3 & 1 & 1/3 \end{array} \right] A$$

$$R_3 \rightarrow -1/7 R_3$$

$$\left[\begin{array}{ccc|c} 1 & 0 & -13 \\ 0 & 1 & 9 \\ 0 & 0 & 1 \end{array} \right] = \left[\begin{array}{ccc|c} -3 & 2 & 0 \\ 2 & -1 & 0 \\ -5/21 & -1/7 & 1/21 \end{array} \right] A$$

$$R_2 \rightarrow R_2 - 9R_3$$

$$R_1 \rightarrow R_1 + 13R_3$$

$$\left[\begin{array}{ccc|c} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array} \right] = \left[\begin{array}{ccc|c} 2/21 & 1/7 & -13/21 \\ -1/7 & 2/7 & 3/7 \\ 5/21 & -1/7 & -1/21 \end{array} \right] A$$

$$A^{-1} = \left[\begin{array}{ccc} 2/21 & 1/7 & -13/21 \\ -1/7 & 2/7 & 3/7 \\ 5/21 & -1/7 & -1/21 \end{array} \right]$$

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$$R_1 \rightarrow R_1 - R_3$$

0	0	0	2
3	9	12	3
1	3	4	1

$$R_2 \rightarrow R_2 - 3R_3$$

0	0	0	2
0	0	0	0
1	3	4	1

$$\rho(A) = 2$$

(no. of non-zero rows = 2)

iv)

1	4	5
2	6	8
3	7	22

$$R_2 \rightarrow R_2 - 2R_1$$

1	4	5
0	-2	-2
3	7	22

$$R_3 \rightarrow R_3 - 3R_1$$

1	4	5
0	-2	-2
0	-5	7

$$R_2 \rightarrow -1/2 R_2$$



$$R_3 \rightarrow R_3 - 2R_2$$

$$A = \begin{bmatrix} 3 & -1 & 2 \\ 0 & 0 & 4 \\ 0 & 0 & 0 \end{bmatrix}$$

$$R_1 \rightarrow 1/3 R_2 \quad , \quad R_2 \rightarrow 1/4 R_2$$

$$A = \begin{bmatrix} 1 & -1/3 & 2/3 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\boxed{|\rho(A)| = 2}$$

Ques \rightarrow

$$\begin{bmatrix} 3 & -1 & 2 \\ -6 & 2 & 4 \\ -3 & 1 & 2 \end{bmatrix}$$

Soln

$$\begin{aligned} R_3 &\rightarrow R_3 + R_1 \\ R_2 &\rightarrow R_2 + 2R_1 \end{aligned}$$

$$\begin{bmatrix} 3 & -1 & 2 \\ 0 & 0 & 8 \\ 0 & 0 & 4 \end{bmatrix}$$

$$R_3 \rightarrow 2R_3 - R_2$$

$$\begin{bmatrix} 3 & -1 & 2 \\ 0 & 0 & 8 \\ 0 & 0 & 0 \end{bmatrix}$$



Roll No. :

SUSHANT UNIVERSITY
SCHOOL OF ENGINEERING AND TECHNOLOGY
MID TERM EXAMINATION, OCTOBER 2024
23BTC-0MA11T: Engineering Mathematics I

Program: B.Tech

Semester: I

Time: 1½ Hr.

Max Mark: 30

Instructions:

1. Section A: Attempt all questions. Each question carries 4 marks.
2. Section B: Attempt any two (2) of three (3) questions. Each question carries 7 marks.

Upon successful completion of the course, the students should be able to:

- CO1: Describe matrix algebra to solving engineering problems. Determine the eigenvalues and eigenvectors of a matrix
- CO2: Distinguish between the concepts of sequence and series. Determine convergence and divergence of series. Understand De Moivre's theorem and find the roots of complex numbers. Application of complex numbers for solving engineering problems
- CO3: Understand application of Leibniz's theorem & Taylor's theorem in real life problems. Demonstrate Knowledge of maxima and minima of function of two variables, Understand Homogeneous Function, asymptotes and curve tracing.

SECTION A

Question 1 (CO 1)

Use Gauss Jordan method to find the inverse of matrix $A = [1 \ 3 \ 3 \ 1 \ 4 \ 3 \ 1 \ 3 \ 4]$.

Question 2 (CO 1)

Define Rank of a matrix. Find the rank of the matrix $A = [3 \ -1 \ 2 \ -6 \ 2 \ 4 \ -3 \ 1 \ 2]$ by reducing it to normal form.

Question 3 (CO 2)

Test the convergence of the series $\frac{2^n}{n^3}$.

Question 4 (CO 1)

Find eigen values and eigen vectors of the matrix $A = [1 \ 1 \ 3 \ 1 \ 5 \ 1 \ 3 \ 1 \ 1]$.



SECTION B

Manisha

Question 5 (CO 1)

Solve the system of equations by matrix method:

$$x + y + z = 3, \quad x + 2y + 3z = 4, \quad x + 4y + 9z = 6.$$

Question 6 (CO 2)

Define convergence and divergence of the series Also test the convergence of the following series

$$\sum \left(\sqrt{n^4 + 1} - \sqrt{n^4 - 1} \right).$$

Question 7 (CO 1)

Find the characteristic equation of the matrix $A = [2 \ -1 \ 1 \ -1 \ 2 \ -1 \ 1 \ -2 \ 2]$ & hence find A^{-1} by Cayley-Hamilton theorem. Find the value of $A^6 - 6A^5 + 9A^4 - 2A^3 - 12A^2 + 23A - 9I$.

Mansoor



SUSHANT UNIVERSITY, GURUGRAM
END TERM EXAMINATION, JANUARY 2022
15BTC-1MA11T: Engineering Mathematics I

Program:-B.Tech

Time: 2 Hrs.

Semester:-I

Max Marks: 60

Instructions:

1. Section A: Attempt any four (4) of five (5) question. Each question carries 7 marks
2. Section B: Attempt any two (2) of three (3) questions. Each question carries 10 marks.
3. Section C: Question is compulsory and carries 12 marks.

CO1: Describe matrix algebra to solving engineering problems. Determine the eigenvalues and eigenvectors of a matrix

CO2: Distinguish between the concepts of sequence and series. Determine convergence and divergence of series. Understand De Moivre's theorem and find the roots of complex numbers. Application of complex numbers for solving engineering problems.

CO3: Understand application of Leibniz's theorem & Taylor's theorem in real life problems. Demonstrate knowledge of maxima and minima of function of two variables, Understand homogeneous Function, asymptotes and curve fitting.

SECTION A

Question 1 (CO 1) (K2)

Find the inverse of the matrix $A = \begin{bmatrix} 1 & 0 & 4 \\ 2 & -2 & 1 \\ -1 & 1 & -1 \end{bmatrix}$ by Gauss-Jordan method.

Question 2 (CO 2) (K 3)

Discuss the convergence of the series: $\frac{1}{2} + \frac{1.3}{2.4} + \frac{1.3.5}{2.4.6} + \dots \dots \dots \dots \dots \dots \dots \dots \dots \dots$

Question 3 (CO 2) (K 5)

If α & β be the roots of $x^2 - 2x + 4 = 0$, prove that $\alpha^n + \beta^n = 2^{n+1} \cos \frac{n\pi}{3}$.

Question 4 (CO 3) (K 4)

If $y = \sin\{m \sin^{-1} x\}$, prove that $(1 - x^2)y_{n+2} - (2n + 1)xy_{n+1} + (m^2 - n^2)y_n = 0$.



Question 5 (CO 2) (K 5)
Define normal and Echelon form of matrix. Also find the rank of a matrix

Mam
S

$$A = \begin{bmatrix} 8 & 1 & 3 & 6 \\ 0 & 3 & 2 & 2 \\ -8 & -1 & -3 & 4 \end{bmatrix}$$

reducing it to normal form.

SECTION B

Question 6 (CO 2) (K 3)

Using matrix method, show that the equations $3x + 3y + 2z = 1, x + 2y = 4, 10y + 3z = -2, 2x - 3y - z = 5$ are consistent and hence obtain the solutions for $x, y, & z$.

Question 7 (CO 3) (K 4)

- (i) Test the convergence of the series : $\sum \left(\frac{n}{n+1} \right)^{n^2}$
- (ii) Test the convergence of the following series:-

$$\left(\frac{2^2}{1^2} - \frac{2}{1}\right)^{-1} + \left(\frac{3^3}{2^3} - \frac{3}{2}\right)^{-2} + \left(\frac{4^4}{3^4} - \frac{4}{3}\right)^{-3} + \dots \dots \dots \dots \dots \dots \dots$$

Question 8 (CO 1) (K 2)

- (i) If $i^{t^i} \stackrel{\infty}{=} A+iB$ prove that $\tan \frac{\pi A}{2} = \frac{B}{A}$ & $A^2 + B^2 = e^{-\pi B}$.
- (ii) If $u = \frac{y}{z} + \frac{z}{x} + \frac{x}{y}$ prove that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} + z \frac{\partial u}{\partial z} = 0$.

SECTION C

Question 9 (CO 3& CO 1) (K 5)

- (a) Define absolute & conditional convergence of an infinite series. Test the following Series for absolute convergence:

$$1 - \frac{1}{2^3}(1+2) + \frac{1}{3^3}(1+2+3) - \frac{1}{4^3}(1+2+3+4) + \dots \dots \dots$$

- (b) If $u = \log \frac{x^4+y^4}{x+y}$, show that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 3$.

Manal



SANTH UNIVERSITY
 School of Engineering and Technology
 Mid Term Examination, October 2024

Room No. D 411A

Student & Award List

Number : 1

Exam Date

Exam Type

Subject

Program : Electronics & Communication
 Semester : 1
 Exams Name :
 Max Marks : 100

S.No.	Application No.	Student Name	Signature	Mark Obtained	Mark Obtained (In Words)
1	2400790	ABHISHEK SINGH	Abhishek Singh	12	Twelve
2	2400791	ATHAR MATE	Athar Mate	10	Ten
3	2400792	AVINASH THAKUR	Avinash Thakur	18	Eighteen
4	2400793	AVINASH KUMAR SHARMA	Avinash Kumar Sharma	04	Four
5	2400794	AKSHAT SHUKLA	Akshat Shukla	12	Twelve
6	2400795	ANKIT NAGAR	Ankit Nagar	12	Twelve
7	2400796	ABHINAV RANGA	Abhinav Ranga	24	Twenty Four
8	2400797	AYUSH CHAUHAN	Ayush Chauhan	11	Eleven
9	2400798	ARYAN KUMAR	Aryan Kumar	11	Eleven
10	2400799	ADITYA KUMAR YADAV	Aditya Kumar Yadav	11	Eleven
11	2400799	DHRUV YADAV	Dhruv Yadav	19	Nineteen
12	2400920	ADITYA BHARTI	Aditya Bharti	17	Seventeen
13	2400950	IBHAVIK	Ibhavik	27	Thirty Seven
14	2401016	AYESHA GUPTA	Ayesha Gupta	05	Five
15	2401032	DHRUV	Dhruv	23	Twenty Three
16	2401058	ANUPRIYA	Anupriya	13	Thirteen
17	2401125	ARKISH DAHIA	Arkish Dahia	23	Twenty three
18	2401160	IDRISHIKA ANEJA	Idrishiaka Aneja	19	Nineteen
19	2401174	ANUJ KUMAR	Anuj Kumar	19	Nineteen
20	2401328	ASTIK GUPTA	Astik Gupta	22	Twenty two
21	2401369	ADITYA CHAUDHARY	Aditya Chaudhary	16	Sixteen
22	2401458	ARPIT KUMAR	Arpit Kumar	06	Six
23	2401489	DEEPAK PHOGAT	Deeprak Phogat	12	Twelve
24	2401514	AASHI THAKRAN	Aashi Thakran	12	Twelve
25	2401556	ARAV	Arav	23	Twenty three
26	2401557	ARMAAN SAIFI	Armaan Saifi	12	Twelve
27	2401622	ARYAN NAPIT	Aryan Napit	23	Twenty three
28	2401788	RAHUL SEHRAWAT	Rahul Sehrawat	10	Ten
29	2401811	AARTI NEGI	Aarti Negi	26	Twenty Six
30	2401841	SHUBHAM LOHIA	Shubham Lohia	07	Seven
31	2402309	DISHANT	Dishant	00	Zero
32	2400398	JAYANT GAUR	Jayant Gaur	06	Six
33	2400431	JATIN RANA	Jatin Rana	11	Eleven

Total number of students:

Student Present: 27

.32

Absent: 06

1. Invigilator's Name and Signature: Reena Shukla

Examiner's Signature: Reena Shukla

2. Invigilator's Name and Signature: Neetu Dahiya

Examiner's Name: _____

Reena Shukla

Neetu Dahiya



SUSHANT UNIVERSITY
School of Engineering and Technology
Mid Term Examination, October 2024

Room No.: D-322
 Attendance & Award List

Semester : I
 Course Title:
 Exam Date:
 Weightage:

Program : B.Tech (I)
 Course Code
 Faculty Name
 Merit Marks

Sl. No.	Application No.	Student Name	Signature	Mark Obtained	Mark Obtained (in Words)
1	2400578	KRISHNA GEMINI	✓ Naveen	19	Nineteen
2	2400555	HARSHIT	✓ Harshit	27	Twenty seven
3	2400559	HARSH SHARMA	✓ Harsh	29	Twenty nine
4	2401164	POOYAV YADAV	✓ P. Yadav	13	Thirteen
5	2400600	KYATHIKA RAO SEELAM	✓ Kyathi Rao	29	Twenty nine
6	2400720	HIMANSHU KUMAR CHAUDHARY	✓ Himanshu	19	Nineteen
7	2400733	MAYANK SHARMA	✓ Mayank	23	Twenty three
8	2400794	KANISHK GAUR	✓ Kanishk	20	Twenty
9	2400827	KUNAL JOON	✓ Kunal Joon	25	Twenty five
10	2400952	KANISHKA	✓ Kanishka	20	Twenty
11	2400972	HARSHIT CHHILLAR	✓ Harshit Chhillar	14	Fourteen
12	2400993	MAYANK KAUSHIK	✓ Mayank	23	Twenty three
13	2401097	KAUSHAL YADAV	✓ Kaushal	21	Twenty one
14	2401151	FAIZAN KHAN	✓ Faizan	11	Eleven
15	2401283	MANI SHANKAR JHA	✓ Mani	17	Seventeen
16	2401299	MAYANK RATHORE	✓ Mayank	11	Eleven
17	2401579	KRISHNA JANGID	✓ Krishna	02	TWO
18	2401604	KUSHAGRA	✓ Kushagra	13	Thirteen
19	2401728	KRISH SHARMA	✓ Krish	26	Twenty six
20	2401782	KUMAR ANKIT	✓ Ankit	07	Seven
21	2401820	KANISHKA SRIVASTAVA	✓ Kanishka	16	Sixteen
22	2401939	SARTHAK PANDAY	✓ Sarthak	11	Eleven
23	2401995	AKSHIT MATHUR	✓ Akshit	17	Seventeen
24	2402062	SANJEEV KUMAR	✓ Sanjeev	17	Seventeen
25	2402112	SHRI KUMAR RAJ	✓ Shri	19	Nineteen
26	2402253	VIRJIT SINGH YADAV	✓ Virjat	08	Eight
27	2402188	PRAGYA	✓ Pragya	05	Five

Total number of students:
 Student Present: 23

Absent: 04

1. Invigilator's Name and Signature: Supriya Verma

Examiner's Signature: Pravin Singh

2. Invigilator's Name and Signature: Supriya Verma

Examiner's Name: _____

Supriya Verma
24-10-24

Pravin Singh

1



SUSTHANT UNIVERSITY
School of Engineering and Technology
Mid Term Examination, October 2024

Room No.: D-303
Attendance & Award List

Semester : I
Exam Date
Weightage

Engg: Mathematics

Application No.
Enrolment No.
Full Name
Mat. Marks

	Application No.	Student Name	Signature	Marks Obtained	Marks Obtained (in Words)
1	2401357	TANISH ROOP	ROOP	16	Eighteen
2	2401360	YUVANSH YADAV	YUVANSH	06	SIX
3	2401364	YASH KUMAR	KUMAR	01	One
4	2401365	YASH	YASH	14	Fourteen
5	2401368	YASH	YASH	10	Ten
6	2401359	TANIYA MALIK	TANIYA	26	Twenty Six
7	2401363	SRITARA	SRITARA	25	Twenty Five
8	2401436	YASH YADAV	YADAV	20	Twenty
9	2401441	SHUBHAM TAWAR	TAWAR	17	Seventeen
10	2401443	VARSHA	VARSHA	22	Twenty Two
11	2401516	SARTHAK MEHTA	SARTHAK	14	Fourteen
12	2401640	SANA GHOSH	SANA	08	Eight
13	2401804	TANISHKA GUPTA	TANISHKA	21	Twenty One
14	2401872	SIHANI	SIHANI	26	Twenty Six
15	2401927	AVNISH	AVNISH	02	Two
16	2401992	DEEKSHA SORAJ	DEEKSHA	12	Twelve
17	2402003	ASHANK SHARMA	ASHANK	14	Fourteen
18	2402024	LAKSHITA	LAKSHITA	18	Eighteen
19	2402026	MOHAMED KHIL MOHAMED AHMED	MOHAMED	07	Seven
20	2402027	MOHAMOUD ALLAELDEEN ALI ABDELFATAH	MOHAMOUD	02	Two
21	2401175	NEERAJ RANA	NEERAJ	10	Ten
22	2401971	AARYAVEER SINGH RANA	AARYAVEER	06	Six
23	2402017	MANAN KOCHAR	MANAN	25	Twenty Five
24	2402070	DIVYANSH Kaushik	DIVYANSH	06	Six
25	2402073	SAMEER PAHWA	SAMEER	08	Eight
26	2402093	Sank Upadhyay	UPADHYAY	12	Twelve

Total number of students:
Student Present:

26

Absent: 03

1. Invigilator's Name and Signature: Munshi Kilram
2. Invigilator's Name and Signature: Utkarsh Kumar

Examiner's Signature: _____

Examiner's Name: _____

Maru



SUSHANT UNIVERSITY
School of Engineering and Technology
Mid Term Examination, October 2024

Room No.: D-320

Attendance & Award List

Program : B.Tech (CSE)

Session End : 2023-24

Results Status :

Visits Marks :

Semester : I

Course Title :

Exam Date :

Weightage :

No.	Application No.	Student Name	Signature	Marks Obtained	Marks Obtained (In Words)
1	2400324	SAMEER VATS	Sameer Vats	26	Twenty Six
2	2400400	MONIS NISHAT	Monis Nishat	26	Twenty Six
3	2400432	NITIN	Nitin	26	Twenty Six
4	2400510	SAARA TEWATHIA	Saara Tewathia	26	Twenty Six
5	2400569	PALAK SHRIVASTAV	Palak Srivastav	26	Twenty Six
6	2400673	NIKHIL PATEL	Nikhil Patel	27	Twenty Seven
7	2400726	RAJ ARYAN	Raj Aryan	27	Twenty Seven
8	2400866	PRINCE	Prince	22	Twenty Two
9	2400966	PRINCE BHARDWAJ	Prince Bhardwaj	09	Nine
10	2401101	NARESH KUMAR	Naresh Kumar	15	Fifteen
11	2401119	MIHAL	MIHAL	15	Fifteen
12	2401216	MOHD HAMZA	MoHD Hamza	15	Fifteen
13	2401304	RITESH KUMAR	Ritesh Kumar	15	Fifteen
14	2401350	RUPESH	Rupesh	08	Eight
15	2401422	PREET YADAV	Preet Yadav	08	Eight
16	2401437	PARINEETA	Parineeta	11	Eleven
17	2401455	NAITIK PRATEEK	Naitik Prateek	05	Five
18	2401493	RISHI	Rishi	09	Four
19	2401525	PIYUSH CHOURBAY	Piyush Chourbey	19	Nineteen
20	2401586	MOHIT	Mohit	04	Four
21	2401692	RITESH MAAN	Ritesh Maan	21	Twenty One
22	2401812	PRASHANT SHARMA	Prashant Sharma	19	Nineteen
23	2402006	DIVYANSHU RANA	Divyanshu Rana	18	Eighteen
24	2401833	PUSHKAR SHARMA	Pushkar Sharma	18	Eighteen
25	2401921	PREET BHADANA	Preet Bhadana	10	Ten
26	2402256	Payal Yadav	Payal Yadav	07	Seven
27	2401102	AADITYA JHA	Aaditya Jha	07	Seven
28	2400599	JAI KUMAR JHA	Jai Kumar Jha	01	One
29	2402277	Yash Raj Kaushik	Yash Raj Kaushik	08	Eight
30	2400214	SOHAM VERMA	Soham Verma	05	Five
31	2400372	UNNATI	Unnati	16	Sixteen

Total number of students:
Student Present: 18

31

Absent: 13

1. Invigilator's Name and Signature:

2. Invigilator's Name and Signature:

Examiner's Signature:

Examiner's Name:



Marked
Mars

SUSHIANT UNIVERSITY
School of Engineering and Technology
Mid Term Examination, October 2024

Room No.: D-301

Attendance & Award List

Semester : I
 Course Title:
 Exam Date :
 Weightage:

Program : B.Tech (Sec-B)
 Course Code:
 Faculty Name:
 Max. Marks:

X.No.	Application No.	Student Name	Signature	Marks Obtained	Marks Obtained (In Words)
1	2401457	AARYAN KASHYAP	<i>Aaryan</i>	07	Seven
2	2402074	Kumar Aryan	<i>Aryan</i>	09	Nine

Total number of students: 02
 Student Present: 02 Absent: 01

1. Invigilator's Name and Signature: Invigilator 24/10/24
 2. Invigilator's Name and Signature: Aryan

Examiner's Signature: _____

Examiner's Name: _____

Mansoor



SUSHANT UNIVERSITY
School of Engineering and Technology
Mid Term Examination, October 2024

Room No.: D-322

Attendance & Award List

Program : B.Tech (Sec-B)
Course Code:
Faculty Name:
Max. Marks:

Semester : I
Course Title:
Exam Date :
Weightage:

S.No.	Application No.	Student Name	Signature	Marks Obtained	Marks Obtained (In Words)
1	2400447	ROSSANE HENRICK			

Total number of students: 01
Student Present: 01 Absent: 00

1. Invigilator's Name and Signature: Suraj

Examiner's Signature: _____

2. Invigilator's Name and Signature: Suraj

Examiner's Name: _____

Suraj
24-10-24

Manoj



SUSHANT UNIVERSITY
School of Engineering and Technology
Special Mid Term Theory Examination, October 2024

Attendance & Award List

Program : B.Tech 1st Year(A & B)
Course Code: 23BTC-0 MA11T
Faculty Name: Dr. Mawale
Max. Marks:

Room No. D 305
Semester : I
Course Title: Mathematics I
Exam Date : 25/11/24
Weightage:

S.No.	Application No/Roll No	Student Name	Signature	Marks Obtained	Marks Obtained (In Words)
1	240BTC13001	Rossone Henry	R. Henrich	12	
2	240BTCSE040	Gorthak Meena	Saranya	12	
3	240BTCSE065	Hosah Tharina	Hosath	18	
4	240BTCSE07	Ashish Sharma	A. Sharm	21	
5	240BTCSE024	Patalk Shrinivas	P. Patalk	12	
6	240BTCSE116	Patil Aryan	A. Patil	14	
7	240BTCSE04	Dan Mesta	Dan Mesta	15	

Total number of students: 6
Student Present: 6 Absent: 0

1. Invigilator's Name and Signature: _____
2. Invigilator's Name and Signature: _____

Examiner's Signature: _____

Examiner's Name: _____

Mawale



ANNEXURE-II

School of Engineering & Technology, Sushant University

Course Title: Mathematics I

Semester: I

Course Code: 23BTC-0MA11T

Course Faculty: Dr. Manimala

Programme: B.Tech

Sir/Madam,

Following students mentioned in the list are identified as Slow learner/ learner based on guidelines issued by IQAC after second assessment (declaration of Mid-term marks).

S No	Roll No	Student Name
1	240BTCCSE033	AARYAN KASHYAP
2	240BTCCSE081	ANKIT NAGAR
3	240BTCCSE054	AVNISH
4	240BTCCSE038	BHAVIK CHAWLA
5	240BTCCSE066	DIVYANSH Kaushik
6	240BTCCSE106	Dishant
7	240BTCCSE044	FAIZAN KHAN
8	240BTCCSE036	JAI KUMAR JHA
9	240BTCCSE017	JAYANT GAUR
10	240BTCCSE117	KUMAR ANKIT
11	240BTCCSE055	Kumar Aryan
12	240BTCCSE051	MAYANK Rathor
13	240BTCCSE014	MOHIT
14	240BTCCSE025	NARESH KUMAR
15	240BTCCSE118	Neeraj Rana
16	240BTCCSE136	Payal Yadav
17	240BTCCSE071	Pragya
18	240BTCCSE107	Rahul Sehrawat
19	240BTCCSE121	RISHI
20	240BTCCSE088	RUPESH
21	240BTCCSE086	Sameer Pahwa
22	240BTCCSE058	SANA GHOSH
23	240BTCCSE058	Sarthak Panday
24	240BTCCSE083	Vipin
25	240BTCCSE011	YUVANSH

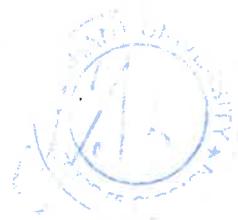
Manimala



Mamta
Signature of Course Coordinator/Faculty

J.S.
Programme Coordinator

Sushant
University
Dean



Teacher Dr. Marimala

Amsai University, Sector 55, Golf Course Road, Gurgaon, Haryana - 122003

Timetable w.e.f. 06/November, 2024

		9:10 - 10:00 1	10:05 - 10:55 2	11:00 - 11:50 3	11:55 - 12:45 4	12:45 - 13:25 5	13:25 - 14:15 6	14:20 - 15:10 7	15:15 - 16:05 8	16:10 - 17:00 9
Mo	Mathematics-I	Discrete Mathematics	B.Tech CSE - AI/ML (Irrd Sem)	B.Tech CSE - Cyber (Irrd Sem)	Discrete Mathematics	B.Tech CSE - Cyber (Irrd Sem)	Discrete Mathematics	B.Tech CSE - Cyber (Irrd Sem)	Discrete Mathematics	Mathematics-I
	D-322	D-413A	D-306	D-413A	D-306	D-413A	D-311	D-301	D-312C	
Tu	Mathematics-I	Mathematics-I	B.Tech CSE - Section B (1st Sem)	B.Tech CSE - Section A (1st Sem)	Discrete Mathematics	B.Tech CSE - All ML (Irrd Sem)	Discrete Mathematics	B.Tech CSE - Cyber (Irrd Sem)	Discrete Mathematics	Mathematics-I
	D-305	D-301	D-413A	D-301	D-413A	D-301	D-311	D-301	D-301	Mathematics-I
We	Mathematics-I	Discrete Mathematics	B.Tech CSE - Section B (1st Sem)	B.Tech CSE - All ML (Irrd Sem)	Discrete Mathematics	B.Tech CSE - Cyber (Irrd Sem)	Discrete Mathematics	B.Tech CSE - Cyber (Irrd Sem)	Discrete Mathematics	Mathematics-I
	D-322	D-413A	D-301	D-413A	D-301	D-301	D-301	D-301	D-301	Mathematics-I
Th	Discrete Mathematics	Mathematics-I	B.Tech CSE - All ML (Irrd Sem)	B.Tech CSE - Section B (1st Sem)	Discrete Mathematics	B.Tech CSE - Cyber (Irrd Sem)	Discrete Mathematics	B.Tech CSE - Cyber (Irrd Sem)	Discrete Mathematics	Mathematics-I
	D-413A	D-322	D-301	D-311	D-301	D-301	D-301	D-301	D-301	Mathematics-I
Fr										

SCHOOL OF ENGINEERING & TECHNOLOGY, SUSHANT UNIVERSITY
ATTENDANCE SHEET - Slow Learners
REMEDIAL CLASSES SCHEDULE QM ATTENDANCE SHEET FOR SLOW LEARNERS

Sushant
University

Program/Batch: B.Tech
 Course Code: 23BTC-0MA11T
 Course Title: Mathematics I
 Date:

Semester: I
 Faculty Name: Dr. Manimala

S.no	Enrollment No.	Student name	Date: 1/1/25 Time: 2:12pm-3:10pm	Date: 1/1/25 Time: 2:12pm-3:10pm	Date: 1/1/25 Time: 2:12pm-3:10pm	Date: 1/1/25 Time: 2:12pm-3:10pm	Remarks (Outcome)
1	240BTCCSE033	AARYAN KASHYAP					
2	240BTCCSE081	ANKIT NAGAR					
3	240BTCCSE054	AVINISH					
4	240BTCCSE038	BHAVIK CHAWLA					
5	240BTCCSE066	DIVYANSH Kaushik					
6	240BTCCSE106	Dishtant					
7	240BTCCSE044	FAIZAN KHAN					
8	240BTCCSE036	JAI KUMAR JHA					
9	240BTCCSE017	JAYANT GAUR					
10	240BTCCSE117	KUMAR ANKIT					
11	240BTCCSE055	Kumar Aryan					
12	240BTCCSE051	MAYANK Rathor					
13	240BTCCSE014	MOHIT					
14	240BTCCSE025	NARESH KUMAR					
15	240BTCCSE118	Neeraj Rana					
16	240BTCCSE136	Pavai Yadav					
17	240BTCCSE071	Pravega					
18	240BTCCSE107	Rahul Srivastav					
19	240BTCCSE121	RISHI					
20	240BTCCSE088	RUPESH					
21	240BTCCSE086	Sameer Pathwa					
22	240BTCCSE058	SANA GHOSH					
23	240BTCCSE058	Sarthak Panday					
24	240BTCCSE083	Vipin					
25	240BTCCSE011	YUVANSH					

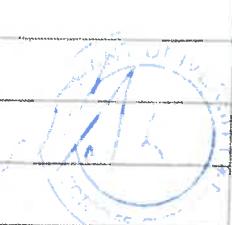
Faculty Signature:

Mani



Name	Sana Gihosh	Year	2024
Subject	Math	Class	B Tech
Semester	1st	Roll No.	240BTCSSE058

INDEX

Sr. No.	Experiment Description	Experiment Date	Submission Date	Remarks / Signature
				<p>Remedial Assignment</p> 

Matrices

Assignment - 1

CLASSMATE
Date : _____
Page : _____

1. Reduce - triangular form.

$$A = \begin{bmatrix} 3 & -4 & -5 \\ -9 & 1 & 4 \\ -5 & 3 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} 3 & -4 & -5 \\ -9 & 1 & 4 \\ -5 & 3 & 1 \end{bmatrix}$$

$$R_2 \rightarrow 3R_1 + R_2 \text{ or } R_2 \rightarrow R_2 + 3R_1$$

$$A \sim \begin{bmatrix} 3 & -4 & -5 \\ 0 & -11 & -11 \\ -5 & 3 & 1 \end{bmatrix}$$

$$R_3 \rightarrow R_3 + 5R_1$$

$$A \sim \begin{bmatrix} 3 & -4 & -5 \\ 0 & -11 & -11 \\ 0 & -14/3 & -22/3 \end{bmatrix}$$

$$R_3 \rightarrow R_3 + (-1/3)R_2$$

$$A \sim \begin{bmatrix} 3 & -4 & -5 \\ 0 & -11 & -11 \\ 0 & -14/3 & 0 \end{bmatrix}$$

2. $A = \begin{bmatrix} 2 & 3 & -1 \\ 0 & -3 & 2 \\ -5 & 3 & 7 \end{bmatrix}$

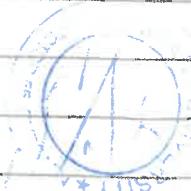
$$R_3 \rightarrow R_3 + \frac{5}{2}R_2$$

$$A \sim \begin{bmatrix} 2 & 3 & -1 \\ 0 & -3 & 2 \\ -5 & 3 & 7 \end{bmatrix}$$

$$R_3 \rightarrow R_3 + 5/2R_1$$

$$A \rightarrow \begin{bmatrix} 2 & 3 & -1 \\ 0 & -3 & 2 \\ 0 & 21/2 & 9/2 \end{bmatrix}$$

$$\begin{bmatrix} 2 & 3 & -1 \\ 0 & -3 & 2 \\ 0 & 0 & 23/2 \end{bmatrix}$$



$$R_2 \rightarrow R_2 - 2R_1$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1/3 & 2/3 & -4/3 \\ 4/3 & -5/3 & 2/3 \\ -1 & 4 & 0 \end{bmatrix}$$

proved.

(Q3) by using elementary transformation that the inverse of each of the following.

$$(i) \begin{bmatrix} 1 & 1 & 3 \\ 1 & 3 & 3 \\ -2 & -4 & -4 \end{bmatrix}$$

$$A = \begin{bmatrix} 1 & 1 & 3 \\ 1 & 3 & 3 \\ -2 & -4 & -4 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

$$R_2 \rightarrow R_2 - R_1$$

$$\begin{bmatrix} 1 & 1 & 3 \\ 0 & 2 & -6 \\ 0 & -2 & 2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 0 \\ 2 & 0 & 1 \end{bmatrix} A$$

$$R_2 \rightarrow (R_2/2)$$

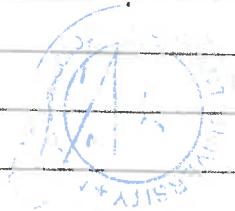
$$\begin{bmatrix} 1 & 1 & 3 \\ 0 & 1 & -3 \\ 0 & 0 & -4 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ -1/2 & 1/2 & 0 \\ 1 & 1 & 1 \end{bmatrix} A$$

$$R_3 \rightarrow -\frac{1}{4}R_3$$

$$\begin{bmatrix} 1 & 1 & 3 \\ 0 & 1 & -3 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ -1/2 & 1/2 & 0 \\ -1/4 & -1/4 & -1/4 \end{bmatrix} A$$

$$R_1 \rightarrow R_1 - 3R_3, R_2 \rightarrow R_2 + 3R_3$$

$$\begin{bmatrix} 1 & 1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} -1/4 & 3/4 & 3/4 \\ -5/4 & -1/4 & -3/4 \\ -1/4 & -1/4 & -1/4 \end{bmatrix} A$$



$$\begin{bmatrix} 3 & 4 & 5 \\ 2 & 6 & 7 \\ 5 & 0 & 10 \end{bmatrix} = 3(60-0) - 4(20-30) + 5(-30) \\ = 70 \neq 0 \\ P = 3$$

(iv) $\begin{bmatrix} 2 & -4 & 6 \\ -1 & 2 & -3 \\ 3 & -6 & 9 \end{bmatrix} = 2(18-18) + 4(-9+9) + 6(6-6) \\ = 0$
Rank is 0.

(v) $\begin{bmatrix} 3 & -1 & 2 \\ -6 & 2 & 4 \\ -3 & 1 & 2 \end{bmatrix}$

~~C2 ↔ C3~~
 $C_2 \leftrightarrow C_3$

$C_1 \rightarrow Y_3 C_1, C_3 \rightarrow Y_2 C_2$

$$\begin{bmatrix} -1 & -1 & 1 \\ -2 & 2 & 2 \\ -1 & 1 & 1 \end{bmatrix}$$

$R_2 \rightarrow Y_2 R_2$

$$\begin{bmatrix} 1 & -1 & 1 \\ 1 & 1 & 1 \\ -1 & 1 & 1 \end{bmatrix}$$

$R_2 \rightarrow R_1 + R_2$

$$\begin{bmatrix} 1 & -1 & 1 \\ 0 & 0 & 2 \\ 0 & 0 & 0 \end{bmatrix}$$

$C_2 \rightarrow Y_2 C_2$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

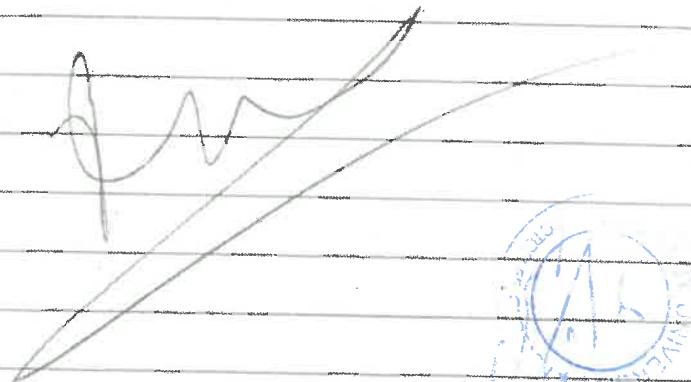
$\begin{array}{c} \textcircled{2} \\ \hookrightarrow \end{array} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 0 \end{bmatrix}$

$$\begin{bmatrix} 1 & -1 & 1 \\ 0 & 0 & 2 \\ -1 & 1 & 1 \end{bmatrix}$$

$R_3 \rightarrow R_3 - R_2$

$$\begin{bmatrix} 1 & -1 & 1 \\ 0 & 0 & 2 \\ 0 & 0 & 2 \end{bmatrix}$$

$P(A) = 2$



$$\left[\begin{array}{cccc} -1 & -1 & -1 & -1 \\ 6 & 7 & 8 & 9 \\ 5 & 5 & 5 & 8 \\ 10 & 10 & 10 & 10 \end{array} \right] \quad \begin{array}{l} R_2 \rightarrow R_2 + 6R_1 \\ R_3 \rightarrow R_3 + 5R_1 \\ R_4 \rightarrow R_4 + 10R_1 \\ R_1 \rightarrow -R_1 \end{array}$$

$$\left[\begin{array}{cccc} 1 & 1 & 1 & 1 \\ 0 & 1 & 2 & 3 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{array} \right] \Rightarrow P(A) = 2$$

Q) 7) a) $\left[\begin{array}{cccc} 1 & -4 & -1 & 2 \\ 1 & 7 & 3 & 1 \\ 5 & -2 & 5 & 4 \\ 0 & -3 & 7 & 2 \end{array} \right]$

$$R_2 \rightarrow R_2 - R_1, \quad R_3 \rightarrow R_3 - 5R_1, \quad R_4 \rightarrow R_4 - 4R_1$$

$$\left[\begin{array}{cccc} 1 & -4 & -1 & 2 \\ 0 & 11 & 4 & -1 \\ 0 & 18 & 10 & -6 \\ 0 & 33 & 16 & -11 \end{array} \right] \quad |A| = -112 \neq 0$$

$$P(A) = 3$$

b) $\left[\begin{array}{cccc} -1 & 2 & 3 & -2 \\ 2 & -5 & 1 & 2 \\ 3 & -8 & 5 & 2 \\ 5 & 12 & 7 & 6 \end{array} \right]$

$$R_1 \rightarrow -R_1, \quad R_2 \rightarrow R_2 - 2R_1$$

$$\left[\begin{array}{cccc} 1 & -2 & -3 & 2 \\ 0 & -1 & 7 & -2 \\ 0 & -2 & 14 & -4 \\ 0 & -2 & 4 & -4 \end{array} \right]$$



$$R_1 \rightarrow -R_1, R_2 \rightarrow R_2 - 2R_1$$

$$\left[\begin{array}{cccc|c} 1 & -2 & -3 & 2 & 7 \\ 0 & -1 & 7 & -2 & \\ 0 & -2 & 14 & -4 & \\ 0 & -2 & 4 & -4 & \end{array} \right]$$

$$R_3 \rightarrow -R_3, R_4 \rightarrow R_4 + R_3, R_3 \rightarrow R_3 + 2R_2$$

$$\left[\begin{array}{cccc|c} 1 & -2 & -3 & 2 & 7 \\ 0 & -1 & 7 & -2 & \\ 0 & 0 & 0 & 0 & \\ 0 & 0 & 0 & 0 & \end{array} \right] \quad P(A) = 2$$

(b)

$$\left[\begin{array}{cccc|c} 2 & 4 & 3 & -2 & 7 \\ -3 & -2 & -1 & -4 & \\ 6 & -1 & 7 & 2 & \end{array} \right]$$

$$R_3 \rightarrow R_3 + 2R_2$$

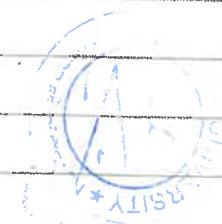
$$\left[\begin{array}{cccc|c} 2 & 4 & 3 & -2 & 7 \\ 3 & -2 & -1 & -4 & \\ 6 & -1 & 7 & 2 & \end{array} \right] \quad P(A) = 3$$

d)

$$\left[\begin{array}{cccc|c} 1 & 2 & 3 & 4 & 7 \\ 2 & 3 & 4 & 5 & \\ 3 & 4 & 5 & 6 & \\ 4 & 5 & 0 & 7 & \end{array} \right]$$

$$R_3 \rightarrow R_3 - R_4, R_2 \rightarrow R_2 - R_3$$

$$\left[\begin{array}{cccc|c} 1 & 1 & 1 & 1 & 7 \\ 0 & 0 & 0 & 0 & \\ 0 & 0 & 0 & 0 & \\ 4 & 5 & 6 & 7 & \end{array} \right]$$



(ii)

$$x + y + z = 1$$

$$2x - y + z = 4$$

$$x - 3y - 2z = 2$$

$$R_3 \rightarrow R_3/5$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 1 \\ 0 & -1 & -2 & -1 \\ 0 & 0 & 1 & 1 \end{array} \right]$$

$$\Rightarrow \left[\begin{array}{ccc|c} 1 & 1 & 1 & 1 \\ 2 & -1 & -1 & 4 \\ 1 & -3 & 2 & 2 \end{array} \right]$$

$$R_2 \rightarrow R_2$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 1 \\ 1 & -3 & -2 & 2 \\ 2 & -1 & 1 & 4 \end{array} \right]$$

$$R_2 \rightarrow R_2 - R_1$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 1 \\ 0 & -4 & -3 & 1 \\ 0 & -3 & -1 & 2 \end{array} \right]$$

$$R_3 \rightarrow R_3 - 2R_1$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 1 \\ 0 & -4 & -3 & 1 \\ 0 & -3 & -1 & 2 \end{array} \right]$$

$$R_2 \rightarrow R_2 - R_3$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 1 \\ 0 & -1 & -2 & 4 \\ 0 & -3 & -1 & 2 \end{array} \right]$$

$$R_3 \rightarrow R_3 - 3R_2$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 1 \\ 0 & -1 & -2 & 4 \\ 0 & 0 & 5 & 5 \end{array} \right]$$

$$z = 1$$

$$-y - 2z = -1$$

$$y = -1$$

$$x - (-1) = 1$$

$$x = 1$$



(Q) 3) Solve the following system of eqn by matrix method.

$$(1) \quad x + y + z = 8$$

$$x - y + 2z = 6$$

$$3x + 5y - 7z = 14$$

$$\rightarrow \left[\begin{array}{ccc|c} 1 & 1 & 1 & 8 \\ 1 & -1 & 2 & 6 \\ 3 & 5 & -7 & 14 \end{array} \right]$$

$$R_2 \rightarrow R_2 - R_1$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 8 \\ 0 & -2 & 1 & -2 \\ 0 & 2 & -10 & -10 \end{array} \right]$$

$$R_3 \rightarrow R_3 + R_2$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 8 \\ 0 & 1 & -\frac{1}{2} & -2 \\ 0 & 0 & 1 & -13 \end{array} \right]$$

$$z = \frac{-13}{3}$$

$$y = 5$$

$$x = 5$$

(4) Show that the eqn $x + 2y - z = 3$

$$3x - y + 2z = 1$$

$$2x - 2y + 3z = 2$$

$$x - y + 2z = -1$$

$$\rightarrow \left[\begin{array}{ccc|c} 1 & 2 & -1 & 3 \\ 3 & -1 & 2 & 1 \\ 2 & -2 & 3 & 2 \\ 1 & 1 & 1 & -1 \end{array} \right]$$



(5) 5)

Test for consistency and solve →

$$\begin{aligned} 5x + 3y + 7z &= 4 \\ 3x + 26y + 22z &= 9 \\ 7x + 24y + 10z &= 5 \end{aligned}$$

$$\left[\begin{array}{ccc|c} 5 & 3 & 7 & 4 \\ 3 & 26 & 22 & 9 \\ 7 & 24 & 10 & 5 \end{array} \right]$$

$\rightarrow R_1 \rightarrow 1/5R_1$

$$\left[\begin{array}{ccc|c} 1 & 3/5 & 7/5 & 4/5 \\ 3 & 26 & 22 & 9 \\ 7 & 24 & 10 & 5 \end{array} \right]$$

$\rightarrow R_2 \rightarrow R_3 - 3R_1$ and $R_3 \rightarrow R_3 - 7R_1$

$$\left[\begin{array}{ccc|c} 1 & 3/5 & 7/5 & 4/5 \\ 0 & 12/5 & 89/5 & 33/5 \\ 0 & -11/5 & 10 & -3/5 \end{array} \right]$$

$\rightarrow R_3 \rightarrow 1/5 R_3$

$$\left[\begin{array}{ccc|c} 1 & 3/5 & 7/5 & 4/5 \\ 0 & 12/5 & 89/5 & 33/5 \\ 0 & 0 & 12/5 & 8/5 \end{array} \right]$$

$$\frac{12}{5} z = 8/5$$

$$z = -\frac{113}{5}$$

$$y = \frac{-56}{121}$$

$$x = 4/5$$



b) $x + y + 5z = 0$
 $x + 2y + 3az = b$
 $x + 3y + az = 1$

$$\left[\begin{array}{ccc|c} 1 & 1 & 5 & 0 \\ 1 & 2 & 3a & b \\ 1 & 3 & a & 1 \end{array} \right]$$

$R_2 \rightarrow R_2 - R_1$

$$\left[\begin{array}{ccc|c} 1 & 1 & 5 & 0 \\ 0 & 1 & 3a-5 & b \\ 1 & 3 & a & 1 \end{array} \right]$$

$R_3 \rightarrow R_3 - R_1$

$$\left[\begin{array}{ccc|c} 1 & 1 & 5 & 0 \\ 0 & 1 & 3a-5 & b \\ 0 & 2 & a-5 & 1 \end{array} \right]$$

$R_3 \rightarrow R_3 - 2R_2$

$$\left[\begin{array}{ccc|c} 1 & 1 & 5 & 0 \\ 0 & 1 & 3a-5 & b \\ 0 & 0 & a-5 & 1 \end{array} \right]$$

(i) No solution

$P(A) \neq P(A:B)$

$a \neq 1 \cdot P(A) = 3, b \neq 4 \cdot P(A:B) = 4$

(ii) A unique soln

$P(A) = P(A:B) = n \quad n=3$

If $a \neq 1$ and $b \in \mathbb{Z}$ b may have any value.

Assignment - 4

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Infinite Series

Q) Discuss the nature of series.

$$1 + 4 + 7 + 10 + \dots + \infty$$

Here, $a = 1$; $d = 3$

$$S_n = n/2 [2a + (n-1)d]$$

$$= n/2 [2 + (n-1)3]$$

$$= n/2 (3n-1)$$

$$\lim_{n \rightarrow \infty} S_n = n/2 (3n-1) \\ = \infty$$

∴ the given series is divergent.

$$1 + 5/4 + 6/4 + 7/4 + \dots + \infty$$

by omitting first term.

$$a = 5/4, d = 1$$

$$S_n = n/2 [5/4 + (n-1)1] \\ = n/2 [5/2 + n - 1] \\ = n/2 (n + 3/2)$$

$$\lim_{n \rightarrow \infty} S_n = n/2 [n + 3/2] = \infty$$

∴ the given series is convergent.

$$3 + 3/2 + 3/2^2 + \dots + \infty$$

Hence, the series is G.P

$$a = 3, r = 1/2$$

$$\text{Sum of G.P} \rightarrow S_n = \frac{a(1-r^n)}{1-r} \quad \text{if } r < 1 \\ = \frac{3(1-(1/2)^n)}{1-1/2}$$



$$\lim_{n \rightarrow \infty} S_n = \frac{2}{3} + \left(\frac{1}{3} \cdot \frac{1}{2^n} \right)$$

$\frac{1}{3} \neq 0$ - a finite quantity (c.f.)

7) $\frac{1}{1^2} + \frac{2}{1^3} + \frac{3}{1^4} + \dots \infty$

$$u_n = \frac{n}{1 \cdot 2 \cdot 3 \dots + (1 + (n-1))1}$$

$$= \frac{n}{1 \cdot 2 \cdot 3 \dots n}$$

$$u_{n+1} = \frac{(n+1)}{1 \cdot 2 \cdot 3 \dots n(n+1)}$$

$$\frac{u_{n+1}}{u_n} = \frac{1}{1 \cdot 2 \cdot 3 \dots n} \times \frac{1 \cdot 2 \cdot 3 \dots n}{n+1}$$

$$= \frac{1}{n+1}$$

$$\lim_{n \rightarrow \infty} \frac{u_{n+1}}{u_n} = \frac{1}{n+1} = \frac{1}{\infty} = 0$$

So, $0 < 1$, Hence given Series is Convergent.

8) $\sum \log \frac{n}{n+1}$

$$\ln n = \log n - \log(n+1)$$

$$= \log n - \left\{ 1 + n + \frac{n^2}{2} - \frac{n^3}{3} \dots \right\}$$

$$u_n = \frac{\log n}{n+1}, u_{n+1} = \log \frac{n+1}{n+2}$$



9) $\sum (\sqrt{n+1} - \sqrt{n})$

$$u_n = \sqrt{n+1} - \sqrt{n}$$

Dividing num and denominator by Conjugate of

Here $P = (2-0)$

$$P = 2$$

$$V_n = \frac{1}{n^2}$$

$$\frac{U_n}{V_n} = \frac{1}{n(n+2)} \times n^{2n}$$

$$= \frac{n^2}{n^2 + 2n}$$

$$\lim_{n \rightarrow \infty} \frac{U_n}{V_n} = \frac{n^2}{n(n+2)} = \frac{n}{n+2} = \frac{n}{n(1+2/n)} = \frac{1}{1+2/n} = 1 \text{ a finite quantity.}$$

Now, $\sum U_n$ is p series as $P = 2 > 1$

$\therefore V_n$ is convergent.

So, U_n is also convergent.

$$44. \sum \frac{1}{n(n+1)(n+2)(n+3)}$$

By Solving denominator

$$= (n^2+n)(n+2)(n+3)$$

$$= (n^3 + 2n^2 + n^2 + 2n)(n+3)$$

$$= (n^3 + 3n^2 + 2n)(n+3)$$

$$= n^4 + 3n^3 + 3n^3 + 9n^2 + 2n^2 + 6n$$

$$= n^4 + 6n^3 + 11n^2 + 6n$$

$$\therefore V_n = \frac{1}{n^4 + 6n^3 + 11n^2 + 6n}$$

$$V_n = \frac{1}{n^4} P = \frac{1}{n^4}$$

$$\frac{U_n}{V_n} = \frac{n^4}{n^4 + 6n^3 + 11n^2 + 6n}$$

dividing num and denominator by n^4

Assignment-5

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(1) $2 + \frac{3}{2} \cdot \frac{1}{4} + \frac{4}{3} \cdot \frac{1}{4^2} + \frac{5}{4} \cdot \frac{1}{4^3} + \dots \dots \infty$

$$U_n = \left[\frac{n+1}{n} \cdot \frac{1}{4^{n-1}} \right]$$

$$U_{n+1} = \left[\frac{n+2}{n+1} \cdot \frac{1}{4^n} \right]$$

$$\begin{aligned} \frac{U_{n+1}}{U_n} &= \frac{n+2}{n+1} \cdot \frac{1}{4^n} \times \frac{4^n}{4^{n-1}} \times \frac{n}{n+1} \\ &= \frac{n(n+2)}{4(n+2)} \\ &= \frac{n^2+2n}{4n^2+8n+4} \end{aligned}$$

$$\lim_{n \rightarrow \infty} \frac{1+2n}{4+8n+4/n^2} = 1/4$$

$1/4 < 1$, given series is Cgt.

2. $1 + \frac{1 \cdot 2}{1 \cdot 3} + \frac{1 \cdot 2 \cdot 3}{1 \cdot 3 \cdot 5} + \dots \dots \infty$

$$U_n = \frac{1 \cdot 2 \cdot 3 \dots n}{1 \cdot 3 \cdot 5 \dots (2n+1)}$$

$$U_{n+1} = \frac{1 \cdot 2 \cdot 3 \dots n(n+1)}{1 \cdot 3 \cdot 5 \dots (2n+1)(2n+3)}$$

$$\begin{aligned} \frac{U_{n+1}}{U_n} &= \frac{1 \cdot 2 \cdot 3 \dots n(n+1)}{1 \cdot 3 \cdot 5 \dots (2n+1)(2n+3)} \times \frac{1 \cdot 3 \cdot 5 \dots (2n+1)}{1 \cdot 2 \cdot 3 \dots n} \\ &= \frac{n+1}{2n+1} \end{aligned}$$

$$\lim_{n \rightarrow \infty} \frac{U_{n+1}}{U_n} = \lim_{n \rightarrow \infty} \frac{n+1}{2n+1}$$

$$\lim_{n \rightarrow \infty} \frac{1+y_n}{2+y_n} = 1/2$$

$$= \frac{1 \times 2 \times 2}{2 \times 2} \\ = 4/4 = 1$$

So, ratio test fails.

Now, Apply Rubbe's test on it

5. $1 + \frac{2^2}{2!} + \frac{3^2}{3!} + \frac{4^2}{4!} + \dots \dots \infty$

$$U_n = \frac{n^2}{2^n}$$

$$U_{n+1} = \frac{(n+1)^2}{(n+1)^2}$$

$$\frac{U_{n+1}}{U_n} = \frac{(n+1)^2}{(n+1)2^n} \times \frac{2^n}{n^2} \\ = \frac{(n+1)(n+1)}{(n+1)n^2}$$

$$\lim_{n \rightarrow \infty} \frac{n+1}{n^2} \\ = \frac{1+1/n}{n} \\ \underset{\rightarrow 0}{\approx}$$

$\therefore 0 < 1$

\therefore The given series cgt.

6. $\frac{1}{1+2} + \frac{2}{1+2^2} + \frac{3}{1+2^3} + \dots \dots$

$$U_n = \frac{n}{1+2^n}$$

$$U_{n+1} = \frac{n+1}{1+2^{n+1}}$$



$$\lim_{n \rightarrow \infty} \frac{U_{n+1}}{U_n} = \lim_{n \rightarrow \infty} (1+y_n)^n \cdot \left(\frac{1+y_n}{1+2y_n}\right)^{n+2}$$

$$= e \cdot 1 = e$$

ex1

\therefore So the given series is divergent.

8) $1/3 + \frac{2!}{3^2} + \frac{3!}{3^3} + \dots \infty$

 $U_n = \frac{1^n}{3^n}$

$$U_{n+1} = \frac{(n+1)}{3^{n+1}}$$

$$\frac{U_{n+1}}{U_n} = \frac{(n+1)/n}{3^{n+1}/3^n} \times \frac{3^n}{1/n}$$

$$\frac{U_{n+1}}{U_n} = \frac{1}{3}(n+1)$$

$$\lim_{n \rightarrow \infty} \frac{U_{n+1}}{U_n} = 1/3 \lim_{n \rightarrow \infty} n+1$$

$$= \infty$$

\therefore The give series is divergent.

9) $\sum \frac{2n^3+5}{4n^5+1} = U_n$

By comparison test

$$V_n = 1/n^p$$

$$= 1/n^3$$

$$P = [5-3]$$

$$P \geq 2$$

$$\frac{U_n}{V_n} = \frac{2n^3+5}{4n^5+1} \times n^3$$



① Reduce the triangular form

$$\textcircled{1} \quad \begin{bmatrix} 3 & -4 & -5 \\ -9 & 1 & 4 \\ -5 & 3 & 1 \end{bmatrix}$$

$$R_2 \rightarrow R_2 + 3R_1$$

$$\begin{bmatrix} 3 & -4 & 5 \\ 0 & -11 & -11 \\ -5 & 3 & 1 \end{bmatrix}$$

$$R_3 \rightarrow 3R_3 + 5R_1$$

$$\begin{bmatrix} 3 & -4 & -5 \\ 0 & -11 & -11 \\ 0 & -11 & -22 \end{bmatrix}$$

$$R_3 \rightarrow R_3 - R_2$$

$$\begin{bmatrix} 3 & -4 & -5 \\ 0 & -11 & -11 \\ 0 & 0 & -11 \end{bmatrix}$$

$$\textcircled{2} \quad \begin{bmatrix} 2 & 3 & -1 \\ 0 & -3 & 2 \\ -5 & 3 & 7 \end{bmatrix}$$

$$R_3 \rightarrow 5R_1 + 2R_3$$

$$\begin{bmatrix} 2 & 3 & -1 \\ 0 & -3 & 2 \\ 0 & 21 & 9 \end{bmatrix}$$

$$R_3 \rightarrow R_3 + 7R_2$$

$$\begin{bmatrix} 2 & 3 & -1 \\ 0 & -3 & 2 \\ 0 & 0 & -12 \end{bmatrix}$$

$$R_1 \rightarrow 3R_1 + 4R_3$$

$$\begin{bmatrix} -11 & 0 & -11 \\ -3 & 1 & 4 \\ -5 & 3 & 1 \end{bmatrix}$$

$$R_1 \rightarrow \frac{R_1}{11}$$

$$\begin{bmatrix} -1 & 0 & -1 \\ -3 & 1 & 4 \\ -5 & 3 & 1 \end{bmatrix}$$

$$R_1 \rightarrow R_1 + R_3$$

$$\begin{bmatrix} -6 & 3 & 0 \\ -3 & 1 & 4 \\ -5 & 3 & 1 \end{bmatrix}$$

$$R_2 \rightarrow R_2 - 4R_3$$

$$\begin{bmatrix} -6 & 3 & 0 \\ 11 & -11 & 0 \\ 5 & 3 & 1 \end{bmatrix}$$

$$R_1 \rightarrow 11R_1 + 3R_2$$

$$\begin{bmatrix} -33 & 0 & 0 \\ 11 & -11 & 0 \\ -5 & 3 & 1 \end{bmatrix}$$



$$\therefore : R_3 \rightarrow R_3 + R_1$$

$$\left[\begin{array}{ccc} 2 & 4 & 0 \\ 0 & 2 & -10 \\ 0 & 4 & -24 \end{array} \right] = \left[\begin{array}{ccc} 1 & 1 & 0 \\ 0 & 2 & 1 \\ 1 & 5 & 3 \end{array} \right] A$$

$$R_1 \rightarrow \frac{1}{2} R_1$$

$$R_2 \rightarrow \frac{1}{2} R_2$$

$$R_3 \rightarrow \frac{1}{4} R_3$$

$$\left[\begin{array}{ccc} 1 & 2 & 0 \\ 0 & 1 & -5 \\ 0 & 1 & -6 \end{array} \right] = \left[\begin{array}{ccc} 1/2 & 1/2 & 0 \\ 0 & 1 & 1/2 \\ 1/4 & 6/4 & 3/4 \end{array} \right] A$$

$$R_3 \rightarrow R_3 - R_2$$

$$\left[\begin{array}{ccc} 1 & 2 & 0 \\ 0 & 1 & -5 \\ 0 & 0 & -1 \end{array} \right] = \left[\begin{array}{ccc} 1/2 & 1/2 & 0 \\ 0 & 1 & 1/2 \\ 1/4 & 1/4 & 1/4 \end{array} \right] A$$

$$R_2 \rightarrow R_2 - 5R_3$$

$$\left[\begin{array}{ccc} 1 & 2 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{array} \right] = \left[\begin{array}{ccc} 1/2 & 1/2 & 0 \\ -5/4 & -1/4 & -3/4 \\ 1/4 & 1/4 & 1/4 \end{array} \right] A$$

$$A^{-1} = \left[\begin{array}{ccc} 3 & 1 & 3/2 \\ -5/4 & -1/4 & -3/4 \\ -1/4 & -1/4 & -1/4 \end{array} \right]$$



$$\textcircled{11} \quad \left[\begin{array}{ccc} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{array} \right] \text{ we have}$$

$$A = IA$$

$$\left[\begin{array}{ccc} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{array} \right] = \left[\begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array} \right] A$$

$$R_1 \rightarrow R_1 - R_2$$

$$\left[\begin{array}{ccc} 1 & 0 & 0 \\ 0 & -3 & 4 \\ 0 & -1 & 1 \end{array} \right] = \left[\begin{array}{ccc} 1 & -1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array} \right] A$$

$$R_2 \rightarrow R_2 + 4R_3$$

$$\left[\begin{array}{ccc} 1 & 0 & 0 \\ 2 & 1 & 0 \\ 0 & -1 & 1 \end{array} \right] = \left[\begin{array}{ccc} 1 & -1 & 0 \\ 0 & 1 & -4 \\ 0 & 0 & 1 \end{array} \right] A$$

$$R_2 \rightarrow R_2 - 2R_1$$

$$\left[\begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & -1 & 1 \end{array} \right] = \left[\begin{array}{ccc} 1 & -1 & 0 \\ -2 & 3 & -4 \\ 0 & 0 & 1 \end{array} \right] A$$

$$A^{-1} = \left[\begin{array}{ccc} 1 & -1 & 0 \\ 2 & 3 & -4 \\ -2 & 3 & -3 \end{array} \right]$$

$$\textcircled{11} \quad \left[\begin{array}{ccc} 1 & 2 & 5 \\ 2 & 3 & 1 \\ -1 & 1 & 1 \end{array} \right]$$

we have

$$\left[\begin{array}{ccc} 1 & 2 & 5 \\ 2 & 3 & 1 \\ -1 & 1 & 1 \end{array} \right] = \left[\begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array} \right]$$

$$R_2 \rightarrow R_2 + 2R_3$$

$$\left[\begin{array}{ccc} 1 & 2 & 5 \\ 0 & 5 & 3 \\ -1 & 1 & 1 \end{array} \right] = \left[\begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{array} \right] A$$

Ex-2.1

4. Find rank of the matrix

$$\textcircled{1} \quad \begin{bmatrix} 2 & -1 & 0 & 5 \\ 0 & 3 & 1 & 7 \end{bmatrix}$$

$$\begin{vmatrix} 2 & -1 \\ 0 & 3 \end{vmatrix} = (6 - 0) = 6 \neq 0 \quad f(A) = 2$$

$$\textcircled{2} \quad \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 7 \\ 3 & 6 & 10 \end{bmatrix}$$

$$R_2 \rightarrow R_2 - 2R_1$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 0 & 0 & 1 \\ 3 & 6 & 10 \end{bmatrix}$$

$$R_3 \rightarrow R_3 - 3R_1$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 0 & 0 & 1 \\ 0 & 0 & 1 \end{bmatrix}$$

$$R_3 \rightarrow R_3 - R_2$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 0 & 0 & 1 \\ 0 & 0 & 0 \end{bmatrix}$$

or continue

$$C_2 \rightarrow C_3$$

$$\begin{bmatrix} 1 & 3 & 2 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$C_3 \rightarrow C_3 - 2C_1$$

$$\begin{bmatrix} 1 & 3 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$C_2 \rightarrow C_2 - 3C_1$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\rightarrow \begin{vmatrix} 1 & 2 \\ 0 & 0 \end{vmatrix} = 0 - 0 = 0$$

$$\begin{vmatrix} 2 & 3 \\ 0 & 1 \end{vmatrix} = 2 - 0 = 2 \neq 0 \quad f(A) = 2$$

$$\begin{bmatrix} I_2 & 0 \\ 0 & 0 \end{bmatrix} = f(A)$$

$$\textcircled{V} \quad \begin{bmatrix} 1 & 4 & 3 \\ 2 & 6 & 8 \\ 3 & 7 & 22 \end{bmatrix}$$

$$= 1(82 - 56) - 4(44 - 24) + 5(14 - 18)$$

$$76 - 80 - 20$$

$$f(A) = 3$$

$$\textcircled{VI} \quad \begin{bmatrix} 2 & -4 & 6 \\ 1 & 2 & -3 \\ 3 & -6 & 3 \end{bmatrix}$$

$$R_3 \rightarrow \frac{1}{3} R_3$$

$$\begin{bmatrix} 2 & -4 & 6 \\ -1 & 2 & -3 \\ 1 & -2 & 3 \end{bmatrix}$$

$$R_3 \rightarrow R_3 + R_2$$

$$\begin{bmatrix} 2 & -4 & 6 \\ -1 & 2 & -3 \\ 0 & 0 & 0 \end{bmatrix}$$

$$R_1 \rightarrow \frac{1}{2} R_1$$

$$\begin{bmatrix} 1 & -2 & 3 \\ -1 & 2 & -3 \\ 0 & 0 & 0 \end{bmatrix}$$

$$R_2 \rightarrow R_2 + R_1$$

$$\begin{bmatrix} 1 & -2 & 3 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} = f(A) = 1$$



$$\textcircled{11} \quad \left[\begin{array}{cccc} 6 & 1 & 3 & 8 \\ 4 & 2 & 6 & -1 \\ 10 & 3 & 9 & 7 \\ 14 & 4 & 12 & 15 \end{array} \right]$$

$$C_3 \rightarrow \frac{1}{3} C_3$$

$$\left[\begin{array}{cccc} 6 & 1 & 1 & 3 \\ 4 & 2 & 2 & -1 \\ 10 & 3 & 3 & 7 \\ 14 & 4 & 4 & 15 \end{array} \right]$$

$$C_1 \rightarrow \frac{1}{2} C_1$$

$$C_3 \rightarrow C_3 - C_2$$

$$\left[\begin{array}{cccc} 3 & 1 & 0 & 8 \\ 2 & 2 & 0 & -1 \\ 5 & 3 & 0 & 7 \\ 8 & 4 & 0 & 15 \end{array} \right]$$

$$C_3 \rightarrow C_4$$

$$\left[\begin{array}{cccc} 3 & 1 & 8 & 0 \\ 2 & 2 & -1 & 0 \\ 5 & 3 & 7 & 0 \\ 3 & 4 & 15 & 0 \end{array} \right]$$

$$R_3 \rightarrow R_3 - R_2$$

$$\left[\begin{array}{cccc} 5 & 1 & 8 & 0 \\ 2 & 2 & -1 & 0 \\ 3 & 1 & 8 & 0 \\ 8 & 4 & 15 & 0 \end{array} \right]$$

$$R_3 \leftarrow R_3 - R_1$$

$$\left[\begin{array}{cccc} 3 & 1 & 8 & 0 \\ 2 & 2 & -1 & 0 \\ 0 & 0 & 0 & 0 \end{array} \right]$$

$$= \boxed{f(C) = 0}$$



Q7: find the rank of the matrix

$$\textcircled{1} \quad \begin{bmatrix} 3 & -4 & -1 & 2 \\ 1 & 7 & 3 & 1 \\ 5 & -2 & 5 & 4 \\ 4 & -3 & 7 & 7 \end{bmatrix}$$

$$R_1 \rightarrow \frac{1}{3} R_1$$

$$\begin{bmatrix} 1 & -1/3 & -1/3 & 2/3 \\ 1 & 7 & 3 & 1 \\ 5 & -2 & 5 & 4 \\ 4 & -3 & 7 & 7 \end{bmatrix}$$

$$R_2 \leftarrow R_2 - R_1 \quad \text{and}$$

$$R_3 \rightarrow R_3 - 5R_1$$

$$\begin{bmatrix} 1 & -4/3 & -1/3 & 2/3 \\ 0 & 25/3 & 10/3 & 1/3 \\ 0 & 14/3 & 20/3 & 2/3 \\ 4 & -3 & 7 & 7 \end{bmatrix}$$

$$R_4 \rightarrow R_4 - 4R_1$$

$$R_2 \rightarrow \frac{3R_2}{25}$$

$$\begin{bmatrix} 1 & -4/3 & 1/3 & 2/3 \\ 0 & 14/25 & 21/25 & 1/25 \\ 0 & 14/3 & 20/3 & 2/3 \\ 0 & 9 & 16 & 1 \end{bmatrix}$$

$$R_3 \rightarrow R_3 - \frac{14}{3} R_2$$

$$R_4 \rightarrow R_4 - 9R_2$$

$$\begin{bmatrix} 1 & -4/3 & 1/3 & 2/3 \\ 0 & 1 & 2/5 & 1/25 \\ 0 & 0 & 24/25 & 12/25 \\ 0 & 0 & 32/25 & 16/25 \end{bmatrix}$$



$$\begin{aligned} R_2 &\rightarrow R_2 \\ R_3 &\rightarrow R_3 - R_4 \end{aligned}$$

$$\left[\begin{array}{cccc} 1 & -2 & -3 & 2 \\ 0 & 1 & -7 & 12 \\ 0 & 0 & 0 & 0 \\ 0 & -2 & 4 & -4 \end{array} \right]$$

$$R_4 \rightarrow R_4 + 2R_1$$

$$\left[\begin{array}{cccc} 1 & -2 & -3 & 2 \\ 0 & 1 & -7 & 2 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{array} \right]$$

$$f(A) = 2$$

(iii)

$$\left[\begin{array}{cccc} 2 & 4 & 3 & -2 \\ -3 & -2 & -1 & 4 \\ 6 & -1 & 7 & 2 \end{array} \right]$$

$$R_2 \rightarrow \frac{1}{2} R_1$$

$$\left[\begin{array}{cccc} 1 & 2 & 3/2 & -1 \\ -3 & -2 & -1 & 4 \\ 6 & -1 & 7 & 2 \end{array} \right]$$

$$R_2 \rightarrow R_2 + 3R_1$$

$$R_3 \rightarrow R_3 - 6R_1$$

$$\left[\begin{array}{cccc} 1 & 2 & 3/2 & -1 \\ 0 & 4 & 7/2 & 1 \\ 0 & -5 & -2 & 8 \end{array} \right]$$

$$R_2 \rightarrow \frac{1}{4} R_2$$



To reduce the each of the following matrix to normal form and find their ranks.

① $\begin{bmatrix} 0 & 2 & 3 & 4 \\ 2 & 3 & 5 & 4 \\ 4 & 8 & 13 & 12 \end{bmatrix}$

$$R_1 \rightarrow R_2$$

$$\begin{bmatrix} 8 & 3 & 5 & 4 \\ 0 & 2 & 3 & 4 \\ 4 & 8 & 13 & 12 \end{bmatrix}$$

$$R_1 \rightarrow \frac{1}{2} R_1$$

$$\begin{bmatrix} 1 & 3/2 & 5/2 & 2 \\ 0 & 2 & 3 & 4 \\ 4 & 8 & 13 & 12 \end{bmatrix}$$

$$R_3 \rightarrow R_3 - 4R_1$$

$$\begin{bmatrix} 1 & 3/2 & 5/2 & 2 \\ 0 & 2 & 3 & 4 \\ 0 & 2 & 3 & 9 \end{bmatrix}$$

$$C_2 \rightarrow C_2 - C_3$$

$$C_4 \rightarrow \frac{1}{2} C_4$$

$$\begin{bmatrix} 1 & -1 & 5/2 & 1 \\ 0 & -1 & 3 & 2 \\ 0 & -1 & 3 & 2 \end{bmatrix}$$

$$C_2 \rightarrow C_2$$

$$\begin{bmatrix} 1 & 1 & 5/2 & 1 \\ 0 & 1 & 3 & 2 \\ 0 & 1 & 3 & 2 \end{bmatrix}$$



$$f(A) = 3$$

$$\begin{bmatrix} 0 & I_3 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Ex

$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$R_3 \rightarrow \frac{1}{2} R_3$$

$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$C_4 \rightarrow C_4 - \frac{1}{2} C_2$$

$$C_3 \rightarrow C_3 + \frac{1}{2} C_2$$

$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \end{bmatrix}$$

$$C_4 \rightarrow C_4 - C_1$$

$$C_2 \rightarrow C_2 - 2C_1$$

$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 2 & 0 & 0 \end{bmatrix}$$

$$R_3 \rightarrow -\frac{1}{2} R_2$$

$$R_2 \rightarrow -\frac{1}{2} R_2$$

$$\begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & -2 & 0 & 0 \\ 1 & 5 & 0 & 0 \\ 1 & 2 & 0 & 0 \end{bmatrix}$$



Ex 2.2

3. solve the following systems of equation by

$$① \quad x + y + z = 8$$

$$x - y + 2z = 6$$

$$3x + 5y - 7z = 14$$

so

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 8 \\ 1 & -1 & 2 & 6 \\ 3 & 5 & -7 & 14 \end{array} \right]$$

$$R_2 \rightarrow R_2 + (-R_1)$$

$$R_3 \rightarrow R_3 + (-3R_1)$$

$$\left[\begin{array}{ccc|c} 1 & 1 & 1 & 8 \\ 0 & -2 & 1 & 2 \\ 0 & 2 & -10 & 70 \end{array} \right]$$

$$R_3 \rightarrow \frac{1}{2}R_3 \text{ and } R_1 \rightarrow R_1 + (-R_2)$$

$$\left[\begin{array}{ccc|c} 1 & 3 & 0 & 10 \\ 0 & -2 & 1 & -2 \\ 0 & 1 & -5 & -5 \end{array} \right]$$

$$R_3 \rightarrow R_3 + 5R_2$$

$$\left[\begin{array}{ccc|c} 1 & 3 & 0 & 10 \\ 0 & -2 & 1 & -2 \\ 0 & -9 & 0 & -15 \end{array} \right]$$

$$R_3 \rightarrow -\frac{1}{9}R_3$$

$$\left[\begin{array}{ccc|c} 1 & 3 & 0 & 10 \\ 0 & -2 & 1 & -2 \\ 0 & 1 & 0 & 5/3 \end{array} \right]$$

$$R_1 \rightarrow R_1 + (-3R_3)$$

$$R_2 \rightarrow R_2 + 2R_3$$

$$\left[\begin{array}{ccc|c} 1 & 0 & 0 & 5 \\ 0 & 0 & 1 & 4/3 \\ 0 & 1 & 0 & 5/3 \end{array} \right]$$

Here $x = 5$
 $y = 5/3$
 $z = -4/3$

W



5) Ans

It can be written $\frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots + \frac{1}{n^2}$

Here

it represent the P series and $P = -2$

Here

$$P < 1$$

\therefore So the given is divergent.

6) Ans

$$GP \rightarrow 1 + \left(-\frac{1}{2}\right) + \left(-\frac{1}{2}\right)^2 + \left(-\frac{1}{2}\right)^3 + \left(-\frac{1}{2}\right)^4 + \dots$$

$$a = 1 \quad r = -\frac{1}{2}$$

$$S_n = \frac{a(1 - r^n)}{1 - r}$$
$$= \frac{1(1 - (-1/2)^n)}{1 + \frac{1}{2}}$$

$$\frac{2}{3} (1 - (-1/2)^n)$$

$$\frac{2}{3} - \frac{2}{3} \left(-\frac{1}{2}\right)^n$$

$$\lim_{n \rightarrow \infty} S_n = \frac{2}{3} + \left(\frac{1}{3} \cdot \frac{1}{2^{n-1}}\right)$$

$$\frac{2}{3} + 0$$

(given series is convgt.)



$$\frac{u_{n+1}}{u_n} = \frac{1}{\cancel{1+2+3+\dots+n}} \times \frac{\cancel{1+2+3+\dots+n}}{n}$$

$$= \frac{1}{n}$$

$$\lim_{n \rightarrow \infty} \frac{u_{n+1}}{u_n} = \frac{1}{\infty}$$

$$= \frac{1}{\infty} = 0$$

$$0 < 1$$

\therefore Hence given series is convergent.

(ii) Ans $\sum (\sqrt{n+1} - \sqrt{n})$

$$u_n = \sqrt{n+1} - \sqrt{n}$$

Dividing Num and denominator by Conjugate of $\sqrt{n+1} + \sqrt{n}$

$$\sqrt{n+1} - \sqrt{n} \times \frac{\sqrt{n+1} + \sqrt{n}}{\sqrt{n+1} + \sqrt{n}}$$

$$= \frac{(n+1) - n}{\sqrt{n+1} + \sqrt{n}} \Rightarrow \frac{1}{\sqrt{n+1} + \sqrt{n}}$$

$$u_n = \frac{1}{np} \quad \text{Here } P \left(\frac{1}{2} - 0 \right)$$

$$= \frac{1}{\sqrt{n}} \quad = \frac{1}{\sqrt{2}}$$



$$\therefore v_n = \frac{1}{n}$$

Here $\rho = (\alpha - 0)$

$$\rho = \alpha$$

$$v_n = \frac{1}{n^2}$$

$$\frac{v_{n+1}}{v_n} = \frac{1}{\alpha(n+2)} \times \alpha^2$$
$$= \frac{n}{n+2}$$

$$\lim_{n \rightarrow \infty} \frac{v_n}{v_{n+1}} \frac{\alpha}{\alpha(1 + \alpha/n)}$$

$$= \frac{1}{1}$$

a finite quantity

Now $\sum v_n$ is ρ series as

$$\rho = \alpha > 1$$

$\therefore v_n$ is convergent

so, a_n is also convergent.

13) Ans

$$= (n^2 + n)(n+2)(n+3)$$

$$= (n^3 + 2n^2 + n^2 + 2n)(n+3)$$

$$= (n^3 + 3n^2 + 2n)(n+3)$$

$$= n^4 + 3n^3 + 3n^3 + 9n^2 + 2n^2 + 6n$$

$$= n^4 + 6n^3 + 11n^2 + 6n$$



$$\text{So: } u_n = \frac{n}{n^3 + 6n^2 + 11n + 6}$$

$$u_n = \frac{1}{n^p} \quad p = [3-1]$$

$$p > 2$$

$$= \frac{1}{n^2}$$

$$\frac{u_n}{v_n} = \frac{n^3}{n^3 + 6n^2 + 11n + 6}$$

Dividing Num & by n^3

$$\lim_{n \rightarrow \infty} \frac{u_n}{v_n} = \frac{1}{1 + \frac{6}{n} + \frac{11}{n^2} + \frac{6}{n^3}}$$

= 1, a finite quantity

Here $p = \alpha > 1$

~~v_n is convergent $\Rightarrow u_n : v_n$ is also convergent.~~



Assignment - 5

① Ans $U_n = \left[\frac{n+1}{n} \cdot \frac{1}{q^{n-1}} \right]$

$$U_{n+1} = \left[\frac{n+2}{n+1} \cdot \frac{1}{q^n} \right]$$

$$\frac{U_{n+1}}{U_n} = \frac{n+2}{n+1} \cdot \frac{1}{q^n} \times \frac{q^n}{q} \times \frac{n}{n+1}$$

$$= \frac{n(n+2)}{q(n+1)^2}$$

$$= \frac{n^2 + 2n}{qn^2 + 8n + 4}$$

$$\lim_{n \rightarrow \infty} \frac{1 + 2n}{qn^2 + 8/n + 4/n^2}$$

$$= \frac{1}{q}$$

$\frac{1}{q} < 1$ is given series gt.



② Ans

$$U_n = \frac{1 \cdot 2 \cdot 3 \cdots n}{1 \cdot 3 \cdot 5 \cdots (1 + (n+1)2)}$$

$$= \frac{1 \cdot 2 \cdot 3 \cdots n}{1 \cdot 3 \cdot 5 \cdots (2n-1)}$$

$$= \frac{2n+1}{2n^2 - n + dn - 1}$$

$$\lim_{n \rightarrow \infty} \frac{n(2 + 1/n)}{n^2(2 + 1/n - 1/n^2)}$$

$$= \frac{d}{\infty} = 0$$

$0 < 1$ and hence series is gt

q/Hnq

$$u_n = \frac{n}{(2n-1)(2n)}$$

$$u_{n+1} = \frac{n+1}{(2n+1)(2n+2)}$$

$$\frac{u_{n+1}}{u_n} = \frac{u_{n+1}}{(2n+1)(2n+2)} \times \frac{(2n+1)(2n)}{n}$$

$$\frac{n(1 + 1/n) \times n(2 - 1/n) \times n(2)}{n(2 + 1/n) \times n(2 + 2/n) \times n}$$

$$\lim_{n \rightarrow \infty} \left(\frac{(1 + 1/n) \times (2 - 1/n) \times (2)}{(2 + 1/n) \times (2 + 2/n) \times (2)} \right)$$

$$\frac{(1) \times (2) \times (2)}{(2) \times (2) \times (2)} = \frac{4}{8} = 1$$

ratio test fails.



so by Raabe's Test

$$\begin{aligned} n \left(\frac{u_{n+1}}{u_n} - 1 \right) &= n \left(\frac{4n^3 + 6n^2 + 2n + 3n - 1}{4n^3 + 4n^2 - n - 1} \right) \\ &= n \left(\frac{4n^3 + 6n^2 + 2n + 3n - 4n^3 - 4n^2 + n + 1}{4n^3 + 4n^2 - n - 1} \right) \\ &= n \left(\frac{2n^2 + 6n + 1}{4n^3 + 4n^2 - n - 1} \right) \\ &= \frac{2n^3 + 6n^2 + 1/n}{4n^3 + 4n^2 - n - 1} \end{aligned}$$

$$\lim_{n \rightarrow \infty} \left[n \left(\frac{u_{n+1}}{u_n} - 1 \right) \right] = \frac{2 + 6/b + 1/n^2}{4 + 4/a - 1/n^2 - 1/n^3}$$
$$= \frac{2}{4} = \frac{1}{2}$$

$$\text{so } \frac{1}{\alpha} < 1$$

The given series is divergent

Ques

$$u_n = \frac{n^2}{[n]}$$

$$u_{n+1} = \frac{(n+1)^2}{[n+1]}$$

$$\frac{u_{n+1}}{u_n} = \frac{(n+1)^2}{(n+1)[n]} \times \frac{[n]}{n^2}$$



Q) Ans By omitting

$$u_n = \frac{n^n}{(n+1)^{n+1}}$$

$$u_{n+1} = \frac{(n+1)^{n+1}}{(n+2)^{n+2}}$$

$$\frac{u_{n+1}}{u_n} = \frac{(n+1)^{n+1}}{(n+2)^{n+2}} \vee \frac{(n+1)^{n+1}}{n^n}$$

$$= \frac{(n+1)^{2n+2}}{n^n(n+2)^{n+2}}$$

$$\frac{u_{n+1}}{u_n} = \frac{(n+1)^n(n+1)^{n+2}}{n^n(n+2)^{n+2}} = \left(\frac{n+1}{n}\right)^n \cdot \left(\frac{n+1}{n+2}\right)^{n+2}$$

$$\lim_{n \rightarrow \infty} \frac{u_{n+1}}{u_n} = \lim_{n \rightarrow \infty} \underbrace{\left(1 + \frac{1}{n}\right)^n}_{\approx e} \cdot \underbrace{\left(\frac{1 + 1/n}{1 + 2/n}\right)^{n+2}}_{\approx 1} \\ = e \cdot 1 \\ = e$$

$$e > 1$$

∴ The given series is divergent

7) Ans

$$u_n = \frac{n}{3^n}$$

$$u_{n+1} = \frac{n+1}{3^{n+1}}$$



Assignment - 6

1) Ans $\frac{\sum n^2}{3^n}$

$$u_n = \frac{n^2}{3^n}$$

$$u_{n+1} = \frac{(n+1)^2}{3^{n+1}}$$

$$\frac{u_{n+1}}{u_n} = \frac{(n+1)^2}{3^{n+1}} \times \frac{3^n}{n^2}$$

$$= \frac{n^2 + 2n + 1}{3^{n+1}}$$

$$\lim_{n \rightarrow \infty} \frac{u_{n+1}}{u_n} = \frac{n^2}{n^2} \left(\frac{1 + 2/n + 1/n^2}{3} \right)$$

$$= \frac{1}{3} < 1$$

$$-\frac{1}{3} < 1$$

so given series is convergent.

1) Ans

$$u_n = \left(\frac{1 \cdot 3 \cdot 5 \cdots n}{3 \cdot 5 \cdot 7 \cdots (2n+1)} \right)^2$$

$$u_{n+1} = \left(\frac{1 \cdot 2 \cdot 3 \cdots n(n+1)}{3 \cdot 5 \cdot 7 \cdots (2n+1)(2n+3)} \right)^2$$

$$\frac{u_{n+1}}{u_n} = \frac{1 \cdot 2 \cdot 3 \cdots n(n+1)}{3 \cdot 5 \cdot 7 \cdots (2n+1)(2n+3)} \times \frac{3 \cdot 5 \cdot 7 \cdots (2n+1)}{1 \cdot 2 \cdot 3 \cdots n}$$



$$= \frac{1}{e}.$$

$$\frac{1}{e} < 1$$

\therefore The given series is convergent.

Q) Ans

$$\sum \frac{(n \cdot 2^n)}{n^n}$$

$$u_{n+1} = \frac{(n+1) \cdot 2^{n+1}}{(n+1)^{n+1}}$$

$$\begin{aligned} &= \frac{(n+1) (n (2^1 \cdot 2))}{(n+1)^2 (n+1)} + \frac{n^2}{2^{2n}} \\ &= 2 \left(\frac{n}{n+1} \right)^n \end{aligned}$$

$$\lim_{n \rightarrow \infty} = d' \frac{1}{\left(1 + 1/n\right)^n}$$

$$= \frac{d}{e}$$

$$\frac{d}{e} < 1$$

Ans

\therefore The given series is convergent.

Ans



Assignment - 2

Q Discuss the nature of following series.

1) Ans Here $a = 1, d = 3$

$$S_n = \frac{n}{2} [2a + (n-1)d]$$

$$= \frac{n}{2} [2 + (n-1)3]$$

$$= \frac{n}{2} (2n+3n-3)$$

$$= \frac{n}{2} (3n-1)$$

$$\lim_{n \rightarrow \infty} S_n \frac{n}{2} (3n-1)$$

$$= \infty$$

\therefore Divergent Series.

2) Ans Omitting First term

$$a = \frac{5}{4}, d = 1$$

$$S_n = \frac{n}{2} [2 + (n-1)1]$$

$$\frac{n}{2} \left[\frac{5}{2} + n - 1 \right]$$

$$\frac{n}{2} \left[n + \frac{3}{2} \right]$$

(Answer)

$$\lim_{n \rightarrow \infty} S_n \frac{n}{2} \left[n + \frac{3}{2} \right]$$

$$= \infty$$

\therefore divergent.



ANNEXURE-II

School of Engineering & Technology, Sushant University

Course Title: Mathematics I

Semester: I

Course Code: 23BTC-OMA11T

Course Faculty: Dr. Manimala

Programme: B.Tech

Sir/Madam,

Following students mentioned in the list are identified as Advanced learner based on guidelines issued by IQAC after second assessment (declaration of Mid-term marks).

S No	Roll No	Student Name
1	240BTCCSE01 8	Harshit Kumar Pandey
2	240BTCCSE04 6	KYATHIKA RAO SEELAM

Signature of Course Coordinator/Faculty

Manimala

Programme Coordinator

Dean



Q1. Find the characteristic equation of the matrix, $A = \begin{bmatrix} 2 & 1 & 1 \\ 0 & 1 & 0 \\ 1 & 1 & 2 \end{bmatrix}$ and hence compute A^{-1} . Also find the matrix represented by $A^8 - 5A^7 + 7A^6 - 3A^5 + A^4 - 5A^3 + 8A^2 - 2A + I$.

Q2. Verify Cayley-Hamilton theorem for the matrix $A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix}$ and hence find the inverse of A . Find A^4 . Express $B = A^8 - 11A^7 - 4A^6 + A^5 + A^4 - 11A^3 - 3A^2 + 2A + I$, as a quadratic polynomial. Find B .

Q3. Discuss the convergence of the hypergeometric series

$$1 + \frac{\alpha \cdot \beta x}{1 \cdot \sqrt{}} + \frac{\alpha(\alpha+1) \beta(\beta+1)}{1 \cdot 2 \cdot \sqrt{(\sqrt{+1})}} x^2 + \frac{\alpha(\alpha+1)(\alpha+2) \beta(\beta+1)(\beta+2)}{1 \cdot 2 \cdot 3 \cdot \sqrt{(\sqrt{+1})(\sqrt{+2})}} x^3 + \dots \infty$$

Q4. Separate $\tan^{-1}(x+iy)$ into real and imaginary parts.

Q5. If Z is a homogeneous function, of degree n in x and y , show that, $x^2 \frac{\partial^2 Z}{\partial x^2} + 2xy \frac{\partial^2 Z}{\partial x \partial y} + y^2 \frac{\partial^2 Z}{\partial y^2} = n(n-1)Z$.



Answers

1. The characteristic eqn of the matrix A is

$$\begin{vmatrix} 2-\lambda & 1 & 1 \\ 0 & 1-\lambda & 0 \\ 1 & 1 & 2-\lambda \end{vmatrix} = 0$$

$\Rightarrow \lambda^3 - 5\lambda^2 + 7\lambda - 3 = 0.$

Acc. to Cayley-Hamilton Theorem, we have $A^3 - 5A^2 + 7A - 3I = 0$.
 Multiplying eq ① by A^{-1} , — ①

$$A^2 - 5A + 7I - 3A^{-1} = 0$$

$$A^{-1} = \frac{1}{3} (A^2 - 5A + 7I).$$

$$A^2 = \begin{bmatrix} 2 & 1 & 1 \\ 0 & 1 & 0 \\ 1 & 1 & 2 \end{bmatrix} \begin{bmatrix} 2 & 1 & 1 \\ 0 & 1 & 0 \\ 1 & 1 & 2 \end{bmatrix} = \begin{bmatrix} 4+0+1 & 2+1+1 & 2+0+2 \\ 0+0+0 & 0+1+0 & 0+0+0 \\ 2+0+2 & 1+1+2 & 1+0+4 \end{bmatrix}$$

$$= \begin{bmatrix} 5 & 4 & 4 \\ 0 & 1 & 0 \\ 4 & 4 & 5 \end{bmatrix}.$$

$$A^2 - 5A + 7I = \begin{bmatrix} 5 & 4 & 4 \\ 0 & 1 & 0 \\ 4 & 4 & 5 \end{bmatrix} - 5 \begin{bmatrix} 2 & 1 & 1 \\ 0 & 1 & 0 \\ 1 & 1 & 2 \end{bmatrix} + 7 \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & -1 & -1 \\ 0 & 3 & 0 \\ -1 & -1 & 2 \end{bmatrix}.$$

$$\Rightarrow A^{-1} = \frac{1}{3} \begin{bmatrix} 2 & -1 & -1 \\ 0 & 3 & 0 \\ -1 & -1 & 2 \end{bmatrix}.$$



$$A^3 = A \cdot A^2 = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix} \begin{bmatrix} 14 & 25 & 31 \\ 25 & 45 & 56 \\ 31 & 56 & 70 \end{bmatrix}$$

$$= \begin{bmatrix} 157 & 283 & 353 \\ 283 & 510 & 636 \\ 353 & 636 & 793 \end{bmatrix},$$

Verification :-

$$A^3 - 11A^2 - 4A + I = \begin{bmatrix} 157 & 283 & 353 \\ 283 & 510 & 636 \\ 353 & 636 & 793 \end{bmatrix} - 11 \begin{bmatrix} 14 & 25 & 31 \\ 25 & 45 & 56 \\ 31 & 56 & 70 \end{bmatrix}$$

$$- 4 \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix} + \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix},$$

To find A^{-1} :-

$$A^3 - 11A^2 - 4A + I = 0 \quad \textcircled{1}$$

Multiplying eq. ① by A^{-1} ,

$$A^2 - 11A - 4I + A^{-1} = 0.$$

$$A^{-1} = -A^2 + 11A + 4I$$

$$\Rightarrow A^{-1} = - \begin{bmatrix} 14 & 25 & 31 \\ 25 & 45 & 56 \\ 31 & 56 & 70 \end{bmatrix} + 11 \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix} + 4 \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & -3 & 2 \\ -3 & 3 & -1 \\ 2 & -1 & 0 \end{bmatrix},$$

To find A^4 :- From Cayley - Hamilton Theorem.

~~$$A^3 - 11A^2 - 4A + I = 0$$~~

$$A^3 = 11A^2 + 4A - I$$

Multiplying both sides by A

$$A^4 = 11A^3 + 4A^2 - A.$$

$$= \lim_{n \rightarrow \infty} \frac{(1+1/n)(1+\sqrt{n})}{(1+\alpha/n)(1+\beta/n)} \cdot \frac{1}{\alpha^n} = \frac{1}{\alpha}.$$

∴ By Ratio test,

the series converges for $\frac{1}{\alpha} > 1$, i.e., $\alpha < 1$,

and diverges for $\alpha > 1$.

it fails for $\alpha = 1$.

Let us try Raabe's Test,

$$\begin{aligned} \lim_{n \rightarrow \infty} n \left(\frac{u_n}{u_{n+1}} - 1 \right) &= \lim_{n \rightarrow \infty} n \left\{ \frac{(n+1)(n+r)}{(n+\alpha)(n+\beta)} - 1 \right\} \\ &= \lim_{n \rightarrow \infty} \left\{ \frac{n(1+r-\alpha) + r - \alpha\beta}{n^2 + n(\alpha+\beta) + \alpha\beta} \right\} \\ &= \lim_{n \rightarrow \infty} \left\{ \frac{1+r-\alpha-\beta + (r-\alpha\beta)\frac{1}{n}}{1+(\alpha+\beta)\frac{1}{n} + \alpha\beta\frac{1}{n^2}} \right\} \\ &= \underline{\underline{1+r-\alpha-\beta}}. \end{aligned}$$

Thus, the series converges for $1+r-\alpha-\beta > 1$, i.e., for $r > \alpha+\beta$,
and diverges for $r < \alpha+\beta$. But it fails for $r = \alpha+\beta$.

Since, $\frac{u_n}{u_{n+1}}$ does not involve n as an exponent or a logarithm, the series $\sum u_n$ diverges for $r = \alpha+\beta$.

Hence the series converges for $\alpha < 1$ and diverges for $\alpha > 1$,
when $\alpha = 1$, the series converges for $r > \alpha+\beta$ and
diverges for $r \leq \alpha+\beta$.

Differentiating Partially w.r.t. y ,

$$\frac{\partial}{\partial y} \left(x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} \right) = \frac{\partial}{\partial y} (nz)$$

$$\frac{\partial z}{\partial y} + x \frac{\partial^2 z}{\partial y \partial x} + y \frac{\partial^2 z}{\partial y^2} = n \frac{\partial z}{\partial y}$$

$$\Rightarrow x \frac{\partial^2 z}{\partial x \partial y} + y \frac{\partial^2 z}{\partial y^2} = (n-1) \frac{\partial z}{\partial y} \quad \text{--- (5)}$$

Multiplying eq. (3) by x and (5) by y , then add,

$$x^2 \frac{\partial^2 z}{\partial x^2} + xy \frac{\partial^2 z}{\partial x \partial y} + xy \frac{\partial^2 z}{\partial x \partial y} + y^2 \frac{\partial^2 z}{\partial y^2} = x(n-1) \frac{\partial z}{\partial x} + y(n-1) \frac{\partial z}{\partial y}.$$

$$x^2 \frac{\partial^2 z}{\partial x^2} + 2xy \frac{\partial^2 z}{\partial x \partial y} + y^2 \frac{\partial^2 z}{\partial y^2} = (n-1) \left(x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} \right).$$

From, eq. ①,

$$x \frac{\partial z}{\partial x} + y \frac{\partial z}{\partial y} = nz.$$

$$x^2 \frac{\partial^2 z}{\partial x^2} + 2xy \frac{\partial^2 z}{\partial x \partial y} + y^2 \frac{\partial^2 z}{\partial y^2} = (n-1)nz.$$

Hence, Proved.



Exercise 2.1

Remedial Assignment-1

NAME - SANA GHOSH

Ques Reduces to triangular form.

$$(i) \begin{bmatrix} 3 & -4 & -5 \\ -9 & 1 & 4 \\ -5 & 3 & 1 \end{bmatrix}$$

$$R_2 \rightarrow 3R_1 + R_2$$

$$\begin{bmatrix} 3 & -4 & -5 \\ 0 & -11 & -11 \\ -5 & 3 & 1 \end{bmatrix}$$

$$R_3 \rightarrow 3R_3 + R_1$$

$$\begin{bmatrix} 3 & -4 & -5 \\ 0 & -11 & -11 \\ 0 & -11/5 & -22/5 \end{bmatrix}$$

$$R_3 \rightarrow \frac{R_2}{5} - R_3$$

$$\begin{bmatrix} 3 & -4 & -5 \\ 0 & -11 & -11 \\ 0 & 0 & 11/5 \end{bmatrix}$$

upper triangular form

$$(ii) \begin{bmatrix} 2 & 3 & -1 \\ 0 & -3 & 2 \\ -5 & 3 & 7 \end{bmatrix}$$

$$R_2 \rightarrow 2R_3 + SR_1$$

$$\begin{bmatrix} 2 & 3 & -1 \\ 0 & -3 & 2 \\ 0 & 2 & 9 \end{bmatrix}$$

$$R_3 \rightarrow R_3 + 7R_2$$

$$\begin{bmatrix} 2 & 3 & -1 \\ 0 & -3 & 2 \\ 0 & 0 & -5 \end{bmatrix}$$

upper triangular form.

$$R_1 \rightarrow R_1 + 5R_3$$

$$\begin{bmatrix} -22 & 11 & 0 \\ -9 & 1 & 4 \\ -5 & 3 & 1 \end{bmatrix}$$

$$R_2 \rightarrow R_2 - 4R_3$$

$$\begin{bmatrix} -22 & 11 & 0 \\ 11 & -11 & 0 \\ -5 & 3 & 1 \end{bmatrix}$$

$$R_1 \rightarrow R_1 + R_2$$

$$\begin{bmatrix} -11 & 0 & 0 \\ 11 & -11 & 0 \\ -5 & 3 & 1 \end{bmatrix}$$

lower triangular form.

$$R_1 \rightarrow 2R_1 + R_2$$

$$\begin{bmatrix} 4 & 3 & 0 \\ 0 & -3 & 2 \\ -5 & 3 & 7 \end{bmatrix}$$

$$R_2 \rightarrow 7R_2 - 2R_3$$

$$\begin{bmatrix} 4 & 3 & 0 \\ 10 & -27 & 0 \\ -5 & 3 & 7 \end{bmatrix}$$

$$R_1 \rightarrow 9R_1 + R_2$$

$$\begin{bmatrix} 46 & 0 & 0 \\ 10 & -27 & 0 \\ -5 & 3 & 7 \end{bmatrix}$$

lower triangular form.

$$2(ii) \begin{bmatrix} 2 & 0 & -1 \\ 5 & 1 & 0 \\ 0 & 1 & 3 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

$$R_1 \rightarrow R_1/2$$

$$\begin{bmatrix} 1 & 0 & -\frac{1}{2} \\ 5 & 1 & 0 \\ 0 & 1 & 3 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

$$R_2 \rightarrow R_2 - 5R_1$$

$$\begin{bmatrix} 1 & 0 & -\frac{1}{2} \\ 0 & 1 & \frac{5}{2} \\ 0 & 1 & 3 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ -\frac{5}{2} & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

$$R_3 \rightarrow R_3 - R_2$$

$$\begin{bmatrix} 1 & 0 & -\frac{1}{2} \\ 0 & 1 & \frac{5}{2} \\ 0 & 0 & \frac{1}{2} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ -\frac{5}{2} & 1 & 0 \\ \frac{5}{2} & -1 & 1 \end{bmatrix} A$$

$$R_3 \rightarrow R_3 - 2R_3$$

$$\begin{bmatrix} 1 & 0 & -\frac{1}{2} \\ 0 & 1 & \frac{5}{2} \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ -\frac{5}{2} & 1 & 0 \\ 5 & -2 & 2 \end{bmatrix} A$$

$$R_1 \rightarrow R_1 + R_3/2 \quad \& \quad R_2 \rightarrow R_2 - 5R_3/2$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 3 & -1 & 1 \\ -15 & 6 & -5 \\ 5 & -2 & 2 \end{bmatrix} A$$

$$\therefore A^{-1} = \begin{bmatrix} 3 & -1 & 1 \\ -15 & 6 & -5 \\ 5 & -2 & 2 \end{bmatrix}$$

$$2(iii) \begin{bmatrix} 2 & 1 & -1 \\ 0 & 2 & 1 \\ 5 & 2 & -3 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

$$R_1 \leftrightarrow R_3$$

$$\begin{bmatrix} 5 & 2 & -3 \\ 0 & 2 & 1 \\ 2 & 1 & -1 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} A$$

$$R_1 \rightarrow R_1 - 2R_3$$

$$\begin{bmatrix} 1 & 0 & -1 \\ 0 & 2 & 1 \\ 2 & 1 & -1 \end{bmatrix} = \begin{bmatrix} -2 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} A$$

$$R_3 \rightarrow R_3 - 2R_1$$

$$\begin{bmatrix} 1 & 0 & -1 \\ 0 & 2 & 1 \\ 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} -2 & 0 & 1 \\ 0 & 1 & 0 \\ 5 & 0 & -2 \end{bmatrix} A$$

$$R_2 \rightarrow R_2 - R_3$$

$$\begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & 0 \\ 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} -2 & 0 & 1 \\ -5 & 1 & 2 \\ 5 & 0 & -2 \end{bmatrix} A$$

$$R_3 \rightarrow R_3 - R_2$$

$$\begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} -2 & 0 & 1 \\ -5 & 1 & 2 \\ 10 & -1 & -4 \end{bmatrix} A$$

$$R_1 \rightarrow R_1 + R_3$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 8 & -1 & -3 \\ -5 & 1 & 2 \\ 10 & -1 & -4 \end{bmatrix} A$$

$$A^{-1} = \begin{bmatrix} 8 & -1 & -3 \\ -5 & 1 & 2 \\ 10 & -1 & -4 \end{bmatrix}$$



Ques 3 Find inverses by elementary row transformation.

$$(i) \begin{bmatrix} 1 & 1 & 3 \\ 1 & 3 & -3 \\ -2 & -4 & -4 \end{bmatrix}$$

$$(ii) \begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix}$$

$$(iii) \begin{bmatrix} 1 & 2 & 5 \\ 2 & 3 & 1 \\ -1 & 1 & 1 \end{bmatrix}$$

$$3(i) R_2 \rightarrow R_2 - R_1 \text{ & } R_3 \rightarrow R_3 + 2R_1$$

$$\begin{bmatrix} 1 & 1 & 3 \\ 0 & 2 & -6 \\ 0 & -2 & 2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ -1 & 1 & 0 \\ 2 & 0 & 1 \end{bmatrix} A$$

$$R_2 \rightarrow R_2/2$$

$$\begin{bmatrix} 1 & 1 & 3 \\ 0 & 1 & -3 \\ 0 & -2 & 2 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ -\frac{1}{2} & \frac{1}{2} & 0 \\ 2 & 0 & 1 \end{bmatrix} A$$

$$R_1 \rightarrow R_1 - R_2 \text{ & } R_3 \rightarrow R_3 + 2R_2$$

$$\begin{bmatrix} 1 & 0 & 6 \\ 0 & 1 & -3 \\ 0 & 0 & -4 \end{bmatrix} = \begin{bmatrix} 3/2 & -\frac{1}{2} & 0 \\ \frac{1}{2} & \frac{1}{2} & 0 \\ 1 & 1 & 1 \end{bmatrix} A$$

$$R_3 \rightarrow -R_3/4$$

$$\begin{bmatrix} 1 & 0 & 6 \\ 0 & 1 & -3 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 3/2 & -\frac{1}{2} & 0 \\ \frac{1}{2} & \frac{1}{2} & 0 \\ \frac{1}{4} & -\frac{1}{4} & -\frac{1}{4} \end{bmatrix} A$$

$$R_1 \rightarrow R_1 - 6R_3 \text{ & } R_2 \rightarrow R_2 + 3R_3$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 3 & 1 & 3/2 \\ -1 & \frac{1}{4} & 3/4 \\ \frac{1}{4} & -\frac{1}{4} & -\frac{1}{4} \end{bmatrix} A$$

$$\therefore A^{-1} = \begin{bmatrix} 3 & 1 & 3/2 \\ -1 & \frac{1}{4} & 3/4 \\ \frac{1}{4} & -\frac{1}{4} & -\frac{1}{4} \end{bmatrix}$$

$$3(ii) \begin{bmatrix} 3 & -3 & 4 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

$$R_1 \rightarrow R_1 - R_2$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 2 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

$$R_2 \rightarrow R_2 - 2R_1$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & -3 & 4 \\ 0 & -1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 3 & 0 \\ 0 & 0 & 1 \end{bmatrix} A$$

$$R_3 \rightarrow 3R_3 - R_2 \text{ and } R_2 \rightarrow R_2 + 4R_3$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & -3 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & -1 & 0 \\ 6 & -9 & 12 \\ 2 & -3 & 3 \end{bmatrix} A$$

$$R_2 \rightarrow -R_2/3$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & -1 & 0 \\ -2 & 3 & -4 \\ -2 & 3 & -3 \end{bmatrix} A$$

$$\therefore A^{-1} = \begin{bmatrix} 1 & -1 & 0 \\ -2 & 3 & -4 \\ -2 & 3 & -3 \end{bmatrix}$$



Ques & Find rank of matrices.

$$4(i) \begin{bmatrix} 2 & -1 & 0 & 5 \\ 0 & 3 & 1 & 4 \end{bmatrix}_{2 \times 4}$$

$$\begin{vmatrix} 2 & -1 \\ 0 & 3 \end{vmatrix} = 6 \neq 0$$

$$\therefore \rho(A) = 2$$

$$4(ii) \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 7 \\ 3 & 6 & 10 \end{bmatrix}_{3 \times 3} = A$$

$$|A| = 0$$

$$\begin{vmatrix} 1 & 2 \\ 2 & 4 \end{vmatrix} = 0 \quad \begin{vmatrix} 2 & 3 \\ 4 & 7 \end{vmatrix} = 2 \neq 0$$

$$\therefore \rho(A) = 2.$$

$$4(iii) \begin{bmatrix} 1 & 3 & 4 & 5 \\ 1 & 2 & 6 & 7 \\ 1 & 5 & 0 & 10 \end{bmatrix}_{3 \times 4}$$

$$\begin{vmatrix} 1 & 3 & 4 \\ 1 & 2 & 6 \\ 1 & 5 & 0 \end{vmatrix} = 0$$

$$\begin{vmatrix} 3 & 4 & 5 \\ 2 & 6 & 7 \\ 5 & 0 & 10 \end{vmatrix} \neq 0 \quad \therefore \rho(A) = 3$$

$$4(iv) \begin{bmatrix} 1 & 3 & 4 & 3 \\ 3 & 9 & 12 & 3 \\ 1 & 3 & 4 & 1 \end{bmatrix} \Rightarrow \begin{vmatrix} 1 & 3 & 4 \\ 3 & 9 & 12 \\ 1 & 3 & 4 \end{vmatrix} = 0$$

$$\begin{vmatrix} 3 & 4 & 3 \\ 1 & 2 & 3 \\ 3 & 4 & 1 \end{vmatrix} = 0 \quad \begin{vmatrix} 1 & 3 & 3 \\ 3 & 9 & 3 \\ 1 & 3 & 1 \end{vmatrix} = 0 \quad \begin{vmatrix} 1 & 4 & 3 \\ 3 & 12 & 3 \\ 1 & 4 & 1 \end{vmatrix} = 0$$

$$\begin{vmatrix} 1 & 3 \\ 3 & 9 \end{vmatrix} = 0 \quad \begin{vmatrix} 3 & 4 \\ 9 & 12 \end{vmatrix} = 0 \quad \begin{vmatrix} 4 & 3 \\ 12 & 3 \end{vmatrix} \neq 0 \quad \therefore \rho(A) = 2$$

$$4(v) \begin{bmatrix} 1 & 4 & 5 \\ 2 & 6 & 8 \\ 3 & 7 & 22 \end{bmatrix}_{3 \times 3} = A$$

$$\therefore |A| = 21 \neq 0 \quad \therefore \rho(A) = 3.$$

$$4(vi) \begin{bmatrix} 2 & -4 & 6 \\ -1 & 2 & -3 \\ 3 & -6 & 9 \end{bmatrix}_{3 \times 3} = A \quad |A| = 0 \quad \begin{vmatrix} 2 & -4 \\ -1 & 2 \end{vmatrix} = 0 \quad \begin{vmatrix} -4 & 6 \\ 2 & -3 \end{vmatrix} = 0$$

$$\begin{vmatrix} 2 & 6 \\ -1 & -3 \end{vmatrix} = 0 \quad \begin{vmatrix} -1 & 2 \\ 3 & -6 \end{vmatrix} = 0 \quad \begin{vmatrix} 2 & -3 \\ -6 & 9 \end{vmatrix} = 0 \quad \begin{vmatrix} -1 & -3 \\ 3 & 9 \end{vmatrix} = 0$$

$$\therefore \rho(A) = 1$$

Reducing in normal form.



$$5(ii) \begin{bmatrix} 6 & 1 & 3 & 8 \\ 4 & 2 & 6 & -1 \\ 10 & 3 & 9 & 7 \\ 16 & 4 & 12 & 15 \end{bmatrix}$$

$$R_1 \rightarrow R_1/6$$

$$\begin{bmatrix} 1 & 1/6 & 1/2 & 4/3 \\ 4 & 2 & 6 & -1 \\ 10 & 3 & 9 & 7 \\ 16 & 4 & 12 & 15 \end{bmatrix}$$

$$R_2 \rightarrow R_2 - 4R_1$$

$$R_3 \rightarrow R_3 - 10R_1$$

$$R_4 \rightarrow R_4 - 16R_1$$

$$\begin{bmatrix} 1 & 1/6 & 1/2 & 4/3 \\ 0 & 4/3 & 4 & -19/3 \\ 0 & 4/3 & 4 & -19/3 \\ 0 & 4/3 & 4 & -19/3 \end{bmatrix}$$

$$R_2 \rightarrow 3R_2/4$$

$$C_3 \rightarrow C_3 - R_4$$

$$\begin{bmatrix} 1 & 1/6 & 1/2 & 4/3 \\ 0 & 1 & 3 & -19/4 \\ 0 & 0 & 0 & 0 \\ 0 & 4/3 & 4 & -19/3 \end{bmatrix}$$

$$R_3 \leftrightarrow R_4$$

$$\begin{bmatrix} 1 & 1/6 & 1/2 & 4/3 \\ 0 & 1 & 3 & -19/4 \\ 0 & 4/3 & 4 & -19/3 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$R_3 \rightarrow R_3 - 4R_2/3$$

$$\begin{bmatrix} 1 & 1/6 & 1/2 & 4/3 \\ 0 & 1 & 3 & -19/4 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$C_2 \rightarrow C_2 - C_1/6$$

$$C_3 \rightarrow C_3 - C_1/2$$

$$\begin{bmatrix} 1 & 0 & 0 & 4/3 \\ 0 & 1 & 5/2 & -19/4 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$C_3 \rightarrow C_3 - 5C_1/2$$

$$C_4 \rightarrow C_4 - 4C_1/3$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & -19/4 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$C_4 \rightarrow C_4 + 19C_1/4$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} I_2 & 0 \\ 0 & 0 \end{bmatrix}$$

$$\therefore J(A)^{2 \times 2}$$



$$6(\text{iii}) \begin{bmatrix} 1 & -1 & 2 & -3 \\ 4 & 1 & 0 & 2 \\ 0 & 3 & 1 & 4 \\ 0 & 1 & 0 & 2 \end{bmatrix}$$

$R_2 \leftrightarrow R_4$

$$\begin{bmatrix} 1 & -1 & 2 & -3 \\ 0 & 1 & 0 & 2 \\ 0 & 3 & 1 & 4 \\ 4 & 1 & 0 & 2 \end{bmatrix}$$

$R_1 \rightarrow R_1 + R_2$

$$\begin{bmatrix} 1 & 0 & 2 & -1 \\ 0 & 1 & 0 & 2 \\ 0 & 3 & 1 & 4 \\ 4 & 1 & 0 & 2 \end{bmatrix}$$

$R_3 \rightarrow R_3 - R_2$

$$\begin{bmatrix} 1 & 0 & 2 & -1 \\ 0 & 1 & 0 & 2 \\ 0 & 2 & 1 & 2 \\ 4 & 1 & 0 & 2 \end{bmatrix}$$

$R_4 \rightarrow R_4 - R_2$

$$\begin{bmatrix} 1 & 0 & 2 & -1 \\ 0 & 1 & 0 & 2 \\ 0 & 1 & 1 & 0 \\ 4 & 0 & 0 & 0 \end{bmatrix}$$

$R_2 \rightarrow R_4/4, R_1 \rightarrow R_1 - R_4$

$$\begin{bmatrix} 0 & 0 & 2 & -1 \\ 0 & 1 & 0 & 2 \\ 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 0 \end{bmatrix}$$

$R_1 \leftrightarrow R_4, R_3 \rightarrow R_3 - R_2$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & -2 \\ 0 & 0 & 2 & -1 \end{bmatrix}$$

$R_4 \rightarrow R_4 - 2R_3$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & -2 \\ 0 & 0 & 0 & 3 \end{bmatrix}$$

$R_2 \rightarrow R_4/3 \& R_3 \rightarrow R_3 - 2R_4, R_3 \rightarrow R_3 + 2R_4$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \rightarrow [I_4]$$

$$\therefore \rho(A) = 4$$

$$6(\text{iv}) \begin{bmatrix} 0 & 1 & -3 & -1 \\ 1 & 0 & 1 & 1 \\ 3 & 1 & 0 & 2 \\ 1 & 1 & -2 & 0 \end{bmatrix}$$

$R_1 \leftrightarrow R_2$

$$\begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & -3 & -1 \\ 3 & 1 & 0 & 2 \\ 1 & 1 & -2 & 0 \end{bmatrix}$$

$R_3 \rightarrow R_3 - R_1$

$$\begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & -3 & -1 \\ 2 & 1 & -1 & 1 \\ 1 & 1 & -2 & 0 \end{bmatrix}$$

$R_3 \rightarrow R_3 - R_4$

$$\begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & -3 & -1 \\ 1 & 0 & 1 & 1 \\ 1 & 1 & -2 & 0 \end{bmatrix}$$

$R_4 \rightarrow R_4 - R_3$

$$\begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & -3 & -1 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & -3 & -1 \end{bmatrix}$$

$R_4 \rightarrow R_4 - R_2$

$$\begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & -3 & -1 \\ 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$R_3 \rightarrow R_3 - R_1$

$$\begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & -3 & -1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$\therefore \rho(A) = 2$$



$$(vi) \begin{bmatrix} 1^2 & 2^2 & 3^2 & 4^2 \\ 2^2 & 3^2 & 4^2 & 5^2 \\ 3^2 & 4^2 & 5^2 & 6^2 \\ 4^2 & 5^2 & 6^2 & 7^2 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 4 & 9 & 16 \\ 4 & 9 & 16 & 25 \\ 9 & 16 & 25 & 36 \\ 16 & 25 & 36 & 49 \end{bmatrix}$$

$$R_2 \rightarrow R_2 - 4R_1$$

$$R_3 \rightarrow R_3 - 9R_1$$

$$\begin{bmatrix} 1 & 4 & 9 & 16 \\ 0 & -7 & -20 & -39 \\ 0 & -20 & -56 & -108 \\ 7 & 25 & 36 & 49 \end{bmatrix}$$

$$R_4 \rightarrow R_4 - 16R_1$$

$$R_2 \rightarrow -R_2/7$$

$$\begin{bmatrix} 1 & 4 & 9 & 16 \\ 0 & 1 & 20/7 & 39/7 \\ 0 & -20 & -56 & -108 \\ 0 & -39 & -108 & -207 \end{bmatrix}$$

$$R_3 \rightarrow R_3 + 20R_1$$

$$R_2 \rightarrow R_2 + 39R_1$$

$$\begin{bmatrix} 1 & 4 & 9 & 16 \\ 0 & 1 & 20/7 & 39/7 \\ 0 & 0 & 8/7 & 24/7 \\ 0 & 0 & 24/7 & 72/7 \end{bmatrix}$$

$$R_3 \rightarrow 7R_3/8$$

$$\begin{bmatrix} 1 & 4 & 9 & 16 \\ 0 & 1 & 20/7 & 39/7 \\ 0 & 0 & 1 & 3 \\ 0 & 0 & 24/7 & 72/7 \end{bmatrix}$$

$$R_4 \rightarrow R_4 - 24R_1/7$$

$$\begin{bmatrix} 1 & 4 & 9 & 16 \\ 0 & 1 & 20/7 & 39/7 \\ 0 & 0 & 1 & 3 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

$$r(A) = 3$$

$$7(iii) \begin{bmatrix} -1 & 2 & 3 & -2 \\ 2 & -5 & 1 & 2 \\ 3 & -8 & 5 & 2 \\ 5 & -12 & -1 & 6 \end{bmatrix}$$

$$R_1 \rightarrow -R_1$$

$$\begin{bmatrix} 1 & -2 & -3 & 2 \\ 2 & -5 & 1 & 2 \\ 3 & -8 & 5 & 2 \\ 5 & -12 & -1 & 6 \end{bmatrix}$$

$$R_2 \rightarrow R_2 - 2R_1$$

$$R_3 \rightarrow R_3 - 3R_1$$

$$R_4 \rightarrow R_4 - 5R_1$$

$$\begin{bmatrix} 1 & -2 & -3 & 2 \\ 0 & 1 & 7 & -2 \\ 0 & -2 & 14 & -4 \\ 0 & -2 & 14 & -4 \end{bmatrix}$$

$$R_2 \leftrightarrow -R_2$$

$$R_3 \rightarrow R_3 - R_4$$

$$\begin{bmatrix} 1 & -2 & -3 & 2 \\ 0 & 1 & -7 & 2 \\ 0 & 0 & 0 & 0 \\ 0 & -2 & 14 & -4 \end{bmatrix}$$

$$R_4 \rightarrow R_4 - 2R_1$$

$$\begin{bmatrix} 1 & -2 & -3 & 2 \\ 0 & 1 & -7 & 2 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Two no zero terms.

$$\therefore \rho(A) = 2$$



$$A(iv) \begin{bmatrix} 1 & 2 & 3 & 4 \\ 2 & 3 & 4 & 5 \\ 3 & 4 & 5 & 6 \\ 4 & 5 & 6 & 7 \end{bmatrix}$$

$$R_4 \rightarrow R_4 - R_3$$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 2 & 3 & 4 & 5 \\ 3 & 4 & 5 & 6 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$R_1 \leftrightarrow R_2$$

$$\begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 2 & 3 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Two non-zero rows.

$$\therefore \rho(A) = 2$$

$$R_3 \rightarrow R_3 - R_4$$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 2 & 3 & 4 & 5 \\ 2 & 3 & 4 & 5 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$R_3 \rightarrow R_3 - R_2$$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \\ 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$R_2 \rightarrow R_2 - R_3$$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 1 & 2 & 3 & 4 \\ 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$R_2 \rightarrow R_2 - R_4$$

$$\begin{bmatrix} 1 & 2 & 3 & 4 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$R_1 \rightarrow R_1 - R_4$$

$$\begin{bmatrix} 0 & 1 & 2 & 3 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 \end{bmatrix}$$

$$R_2 \leftrightarrow R_4$$

$$\begin{bmatrix} 0 & 1 & 2 & 3 \\ 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$



$$8(ii) \begin{bmatrix} 1 & 2 & 0 & -1 \\ 3 & 4 & 1 & 2 \\ -2 & 3 & 2 & 5 \end{bmatrix}$$

$$R_2 \rightarrow R_2 - 3R_1$$

$$\begin{bmatrix} 1 & 2 & 0 & -1 \\ 0 & -2 & 1 & 5 \\ -2 & 3 & 2 & 5 \end{bmatrix}$$

$$R_3 \rightarrow R_3 + 2R_1$$

$$\begin{bmatrix} 1 & 2 & 0 & -1 \\ 0 & -2 & 1 & 5 \\ 0 & 5 & 2 & 4 \end{bmatrix}$$

$$C_2 \rightarrow C_2 + C_3$$

$$\begin{bmatrix} 1 & 2 & 0 & -1 \\ 0 & -1 & 1 & 5 \\ 0 & 7 & 2 & 4 \end{bmatrix}$$

$$C_2 \leftrightarrow C_3$$

$$\begin{bmatrix} 1 & 0 & 2 & -1 \\ 0 & 1 & -1 & 5 \\ 0 & 2 & 7 & 4 \end{bmatrix}$$

$$R_3 \rightarrow R_3 - 2R_2$$

$$\begin{bmatrix} 1 & 0 & 2 & -1 \\ 0 & 1 & -1 & 5 \\ 0 & 0 & 9 & -6 \end{bmatrix}$$

$$R_4 \rightarrow R_4 / 3$$

$$\begin{bmatrix} 1 & 0 & 2 & -1 \\ 0 & 1 & -1 & 5 \\ 0 & 0 & 3 & -2 \end{bmatrix}$$

$$R_1 \rightarrow R_1 - R_3$$

$$\begin{bmatrix} 1 & 0 & -1 & 1 \\ 0 & 1 & -1 & 5 \\ 0 & 0 & 3 & -2 \end{bmatrix}$$

$$C_3 \rightarrow C_3 + C_4$$

$$\begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & -1 & 5 \\ 0 & 0 & 3 & -2 \end{bmatrix}$$

$$C_3 \rightarrow C_3 + C_2$$

$$\begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 5 \\ 0 & 0 & 3 & -2 \end{bmatrix}$$

$$C_2 \rightarrow C_4 - C_3$$

$$\begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 5 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

$$C_4 \rightarrow C_4 - C_1$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 5 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

$$C_4 \rightarrow C_4 - 5C_2$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

$$C_4 \rightarrow C_4 / 5$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 3 & 1 \end{bmatrix}$$

$$C_3 \rightarrow C_3 / 3$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix}$$

$$C_4 \rightarrow C_4 - C_3$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

$$\Leftrightarrow \begin{bmatrix} I_3 & 0 \end{bmatrix}$$

$$\therefore \rho(A) = 3$$

Subject Code	Subject Name	Exam Type	Maximum Marks	Student Batch	Student S	Student C	Student Semester	Student Roll No.	Student Name	40.00	Obtained	Row Total	Row Total	Row Total	Row Total
B.Tech-CSE (Computer Science Engineering							CLASS - 3 - 4	230BTCCSE157	HARSHITA KAKKAR	0	0				
								240BTCCSE003	Drishika Aneja	35.50	35.50				
								240BTCCSE007	Akshit Shukla	30.00	30.00				
								240BTCCSE008	Astik Gupta	34.00	34.00				
								240BTCCSE009	Ayesha Gupta	37.50	37.50				
								240BTCCSE016	Aryan Napit	32.50	32.50				
								240BTCCSE019	Aditya Jha	0	0				
								240BTCCSE020	Aashi Thakran	27.00	27.00				
								240BTCCSE022	Dhruv Yadav	21.50	21.50				
								240BTCCSE023	Arpit Kumar	27.00	27.00				
								240BTCCSE029	Aarti Negi	36.00	36.00				
								240BTCCSE032	Arkish Dahiya	28.50	28.50				
								240BTCCSE038	Bhavik Shankar	28.50	28.50				
								240BTCCSE041	Bhavik Chawla	27.00	27.00				
								240BTCCSE043	Arav	28.00	28.00				
								240BTCCSE047	Ashish Kumar Sharma	32.50	32.50				
								240BTCCSE059	Atharv Malik	28.00	28.00				
								240BTCCSE062	Arman Saffi	34.50	34.50				
								240BTCCSE063	Aryan Kumar	35.00	35.00				
								240BTCCSE065	Harsh Sharma	29.00	29.00				
								240BTCCSE077	Anupriya	37.00	37.00				
								240BTCCSE081	Ankit Nagar	20.00	20.00				
								240BTCCSE087	Abhinav Ranga	28.00	28.00				
								240BTCCSE091	Aditya chaudhary	18.00	18.00				
								240BTCCSE106	Dishant	20.00	20.00				
								240BTCCSE107	Rahul sehrawat	26.00	26.00				
								240BTCCSE108	Dhruv Yadav	31.50	31.50				
								240BTCCSE109	Deepak Phogat	22.00	22.00				
								240BTCCSE115	Anuj Kumar	31.50	31.50				
								240BTCCSE112	Mayank Kaushik	33.50	33.50				

CLASS - 1

Manu Singh

240BTCCSE013	Kanishk Gaur	32.00	32.00
240BTCCSE017	Jayant Gaur	24.00	24.00
240BTCCSE018	Harshit Kumar Pandey	38.50	38.50
240BTCCSE026	Harshit Chhillar	27.00	27.00
240BTCCSE030	Himanshu Kumar Cha	32.50	32.50
240BTCCSE037	Kanishka Srivastava	30.00	30.00
240BTCCSE042	Kanishka Yadav	32.00	32.00
240BTCCSE044	Faizan Khan	25.50	25.50
240BTCCSE046	Kyathika Rao Seelam	38.50	38.50
240BTCCSE050	Kunal Joon	35.50	35.50
240BTCCSE051	Mayank Rathore	20.00	20.00
240BTCCSE056	Sarthak Panday	26.50	26.50
240BTCCSE069	Krishna Gemini	29.50	29.50
240BTCCSE070	Mayank Sharma	33.50	33.50
240BTCCSE071	Pragya	22.50	22.50
240BTCCSE074	Sanjeev Kumar	29.50	29.50
240BTCCSE076	Poorav Yadav	26.50	26.50
240BTCCSE078	Kaushal Yadav	32.50	32.50
240BTCCSE079	Akshit Mathur	29.50	29.50
240BTCCSE083	Vipin Singh Yadav	22.00	22.00
240BTCCSE084	Shiv Kumar Ray	31.50	31.50
240BTCCSE089	Jatin Rana	24.50	24.50
240BTCCSE090	Krrish Sharma	36.00	36.00
240BTCCSE001	Nihal Pandey	28.50	28.50
240BTCCSE002	Rossane Henrick	28.00	28.00
240BTCCSE004	Prince Bhardwaj	34.00	34.00
240BTCCSE005	Piyush Choubey	30.50	30.50
240BTCCSE006	Saara Tewathia	36.00	36.00
240BTCCSE014	Mohit Naharwa	23.00	23.00
240BTCCSE021	Nikhil Patel	36.50	36.50
240BTCCSE024	Palak Shrivastav	27.00	27.00
240BTCCSE025	Naresh Kumar	25.50	25.50
240BTCCSE028	Prashant Sharma	30.50	30.50
240BTCCSE036	Jai Kumar Jha	21.50	21.50
240BTCCSE045	Nitin Sehrawat	0	0

CLASS - 1



CLASS - 1				
240BTCSE048	Parineeta	25.50	25.50	
240BTCSE052	Ritesh Maan	32.50	32.50	
240BTCSE057	Divyanshu Rana	31.00	31.00	
240BTCSE060	Ritesh Kumar	28.50	28.50	
240BTCSE068	Yashraj Kaushik	0		
240BTCSE085	Mohd Hamza	28.50	28.50	
240BTCSE088	Rupesh Singh	25.00	25.00	
240BTCSE093	Sameer Vats	37.00	37.00	
240BTCSE010	Soham Verma	33.00	33.00	
240BTCSE011	Yuvansh Yadav	23.00	23.00	
240BTCSE015	Taksh Roop Srivastava	32.00	32.00	
240BTCSE031	Yash Kumar	32.50	32.50	
240BTCCSE033	Aaryan Kashyap	22.50	22.50	
240BTCCSE034	Yash Yadav	32.00	32.00	
240BTCCSE035	Varsha	34.00	34.00	
240BTCCSE039	Suhani Gupta	37.00	37.00	
240BTCCSE040	Sarthak Mehta	26.00	26.00	
240BTCCSE049	Tanishka Gupta	34.50	34.50	
240BTCCSE053	Ashank Sharma	27.00	27.00	
240BTCCSE054	Avnish	22.00	22.00	
240BTCCSE055	Kumar Aryan	23.50	23.50	
240BTCCSE058	Sana Ghosh	26.00	26.00	
240BTCCSE061	Mohamoud Allaeldin	22.00	22.00	
240BTCCSE064	Mohamed Khlid Khlid	24.50	24.50	
240BTCCSE066	Divyansh Kaushik	23.00	23.00	
240BTCCSE067	Unnati	31.00	31.00	
240BTCCSE075	Taniya Malik	37.00	37.00	
240BTCCSE080	Deeksha Soraj	27.00	27.00	
240BTCCSE086	Sameer Pahwa	25.00	25.00	
240BTCCSE092	Sritara pasricha	36.50	36.50	
240BTCCSE113	Manan Kochar	34.50	34.50	
240BTCCSE114	Shubham Tanwar	28.50	28.50	
240BTCCSE116	RAJ ARYAN	28.00	28.00	
240BTCCSE118	Neeraj Rana	26.00	26.00	
240BTCCSE119	Lakshita	31.00	31.00	





B.Tech-CSE (Computer Science Engineering) Semester CLASS - 1				
240BTCCSE120	Satvik Upadhyay	27.00	27.00	
240BTCCSE121	Rishi Jaiswal	21.00	21.00	
240BTCCSE134	Yash Tanwar	28.50	28.50	
240BTCCSE136	payal Yadav	22.50	22.50	



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CO1 Attainment Level

Asstg	Level 1	Less than 60% students
name	Level 2	60% to less than 60%

Year	0	0-3	4-6	7-10	9
2017	0	0	0	0	9

Year	Max Marks	Min Marks	Passion	Less than 45% (-)	More than 90%	0.00%	100.0%
2017	14	5	11.2	0	0	0	100.0%

88	Z00BTCCS0801	Sai Kumar Ray	Shiv Kumar Ray	2	5	5	12	12
89	Z00BTCCS114	Sushil Kumar Tewari	Shivam Tewari	4	5	5	11	11
90	Z00BTCCS110	Soham Vinita	Soham Vinita	4	4	4	11	11
91	Z00BTCCS092	Sneha Parbatika	Sneha Parbatika	4	4	4	11	11
92	Z00BTCCS039	Suniti Gupta	Suniti Gupta	4	5	5	13	13
93	Z00BTCCS039	Tanusha Gupta	Tanusha Gupta	4	5	5	13	13
94	Z00BTCCS049	Tanya Malhotra	Tanya Malhotra	4	5	5	13	13
95	Z00BTCCS065	Umaan	Umaan	4	5	5	13	13
96	Z00BTCCS065	Vanya Malhotra	Vanya Malhotra	4	5	5	13	13
97	Z00BTCCS065	Vishal Malhotra	Vishal Malhotra	4	5	5	13	13
98	Z00BTCCS065	Vipin Singh Rawat	Vipin Singh Rawat	4	5	5	13	13
99	Z00BTCCS063	Vishal Kumar	Vishal Kumar	3	3	3	10	10
100	Z00BTCCS114	Yash Tiwari	Yash Tiwari	3	3	3	10	10
101	Z00BTCCS043	Yash Tiwari	Yash Tiwari	3	3	3	10	10
102	Z00BTCCS068	Yash Tiwari	Yash Tiwari	3	3	3	10	10
103	Z00BTCCS011	Yuvansh Vaidya	Yuvansh Vaidya	4	4	4	10	10
104	Z00BTCCS063	Yuvansh Vaidya	Yuvansh Vaidya	4	4	4	10	10
105	Z00BTCCS063	Zarifa	Zarifa	4	4	4	10	10
106	Z00BTCCS063	Zarifa	Zarifa	4	4	4	10	10
107	Z00BTCCS063	Zarifa	Zarifa	4	4	4	10	10
108	Z00BTCCS063	Zarifa	Zarifa	4	4	4	10	10
109	Z00BTCCS063	Zarifa	Zarifa	4	4	4	10	10
110	Z00BTCCS063	Zarifa	Zarifa	4	4	4	10	10
111	Z00BTCCS117	Total Students	Total Students	11	13	13	30	30
112	Z00BTCCS117	Average	Average	11.0	11.0	11.0	30.0	30.0
113	Z00BTCCS117	Total Students	Total Students	11	13	13	30	30
114	Z00BTCCS117	Number of Students Scored Average % and above marks (%)	Number of Students Scored Average % and above marks (%)	10	10	10	30	30
115	Z00BTCCS117	CD Standard (PNL) (%)	CD Standard (PNL) (%)	95	95	95	30	30

S. No.	Barometer No.	Student Name	Seat No.	C01 (1)	C02 (2)	C03 (3)	C04 (4)	C05 (5)	C06 (6)	Total Marks
1	2408TCSE029	Aarti Negi	2	2	3	3	CO1 (25)	CO2 (25)	CO3 (25)	(10)
2	2408TCSE033	Ananya Ashayap	2	2	2	3	CO3 (25)	CO2 (25)	CO1 (25)	(10)
3	2408TCSE020	Aashni Thakran	2	2	2	2	2	2	2	10
4	2408TCSE007	Aishwarya Ranjana	2	2	2	3	3	2	2	8
5	2408TCSE091	Aishwarya Thakur	2	2	2	2	2	2	2	8
6	2408TCSE007	Aishwarya Thakur	2	2	2	2	2	2	2	8
7	2408TCSE028	Aishwarya Thakur	2	2	2	3	3	2	2	8
8	2408TCSE015	Aishwarya Thakur	2	2	2	2	2	2	2	8
9	2408TCSE077	Aishwarya Thakur	2	2	2	2	2	2	2	8
10	2408TCSE077	Aishwarya Thakur	2	2	2	3	3	2	2	8
11	2408TCSE004	Akavya	2	2	3	3	CO3 (25)	CO2 (25)	CO1 (25)	(10)
12	2408TCSE032	Akshitha Dhalia	2	2	3	3	3	2	2	10
13	2408TCSE062	Amman Suri	2	2	3	3	2	2	2	10
14	2408TCSE023	Amrit Kumar	2	2	3	3	2	2	2	10
15	2408TCSE003	Anjali Kumar	2	2	2	3	3	2	2	9
16	2408TCCE016	Anjali Negi	2	2	2	3	3	2	2	10
17	2408TCSE03	Anjali Sharma	2	2	2	3	3	2	2	10
18	2408TCSE008	Anjali Sharma	2	2	2	3	3	2	2	10
19	2408TCSE008	Anjali Sharma	2	2	2	3	3	2	2	10
20	2408TCSE059	Arthi Malik	2	2	2	3	3	2	2	10
21	2408TCSE054	Arvishi Negi	2	2	2	3	3	2	2	10
22	2408TCSE009	Avyasha Gupta	2	2	2	3	3	2	2	10
23	2408TCSE041	Bhanu Chawla	2	2	2	3	3	2	2	10
24	2408TCSE038	Bhanuk Sharker	2	2	2	2	2	2	2	8
25	2408TCSE026	Bhanuk Sharker	2	2	2	2	2	2	2	8
26	2408TCSE09	Deepika Pragati	2	2	2	3	3	2	2	10
27	2408TCSE022	Dhruvi Patel	2	2	2	2	2	2	2	8
28	2408TCSE008	Dhruvi Patel	2	2	2	2	2	2	2	8
29	2408TCSE106	Dhruvi Patel	2	2	2	3	3	2	2	10
30	2408TCSE066	Divyanshu Kastrik	2	2	2	2	2	2	2	8
31	2408TCSE057	Divyanshu Rana	2	2	2	3	3	2	2	10
32	2408TCSE003	Divyanshu Rana	2	2	2	3	3	2	2	10
33	2408TCSE044	Fazlara Khan	2	2	2	2	2	2	2	10
34	2408TCSE055	Fazlara Khan	2	2	2	2	2	2	2	10
35	2408TCSE025	Gauri Gauri	2	2	2	3	3	2	2	10
36	2408TCSE018	Harshti Kumar Patel	2	2	2	2	2	2	2	10
37	2408TCSE157	Harshti Kumar Patel	2	2	2	2	2	2	2	8
38	2408TCSE030	Himashu Kumar Chaudhary	2	2	2	3	3	2	2	10
39	2408TCSE036	Jai Kumar Ma	2	2	3	3	2	2	2	10
40	2408TCSE049	Jasini Rana	2	2	2	3	3	2	2	10
41	2408TCSE071	Jayanti Gauri	2	2	2	3	3	2	2	10
42	2408TCSE033	Kanishka Gur	2	2	2	3	3	2	2	10
43	2408TCSE077	Kanishka Patel	2	2	2	3	3	2	2	10
44	2408TCSE042	Kanishka Patel	2	2	2	3	3	2	2	10
45	2408TCSE078	Kashish Patel	2	2	2	3	3	2	2	10
46	2408TCSE069	Krishna Gauri	2	2	2	3	3	2	2	10
47	2408TCSE093	Krishna Patel	2	2	2	3	3	2	2	10
48	2408TCSE055	Krunal Aryan	2	2	2	2	2	2	2	8
49	2408TCSE053	Krunal Patel	2	2	2	2	2	2	2	8
50	2408TCSE066	Kyathika Patel	2	2	2	3	3	2	2	10
51	2408TCSE119	Kyathika Patel	2	2	2	3	3	2	2	10
52	2408TCSE171	Lakshmi	2	2	2	3	3	2	2	10
53	2408TCSE133	Mahan Kocchar	2	2	2	3	3	2	2	10
54	2408TCSE051	Meyarik Asuthik	2	2	2	3	3	2	2	10
55	2408TCSE070	Meyarik Asuthik	2	2	2	2	2	2	2	8
56	2408TCSE044	Mihamed Khil Khil	2	2	2	3	3	2	2	10
57	2408TCSE061	Mohanad Alhaldeen	2	2	2	3	3	2	2	10
58	2408TCSE085	Mohit Nehru	2	2	2	3	3	2	2	10
59	2408TCSE14	Mohit Nehru	2	2	2	3	3	2	2	10
60	2408TCSE25	Naresh Kumar	2	2	2	3	3	2	2	10
61	2408TCSE118	Nilesh Arya	2	2	2	3	3	2	2	10
62	2408TCSE001	Nilesh Patel	2	2	2	3	3	2	2	10
63	2408TCSE21	Nikhil Patel	2	2	2	3	3	2	2	10
64	2408TCSE45	Nitin Schwartz	AB	AB	AB	AB	AB	AB	AB	AB
65	2408TCSE024	Palak Shrivastav	2	2	2	3	3	2	2	8
66	2408TCSE048	Parmeeeti	2	2	2	2	2	2	2	8
67	2408TCSE139	Pavay Patel	2	2	2	3	3	2	2	10
68	2408TCSE055	Piyush Shubra	2	2	2	3	3	2	2	10
69	2408TCSE076	Poochy Yadev	2	2	2	3	3	2	2	10
70	2408TCSE071	Priyanka Sharma	2	2	2	3	3	2	2	10
71	2408TCSE028	Priyanka Sharma	2	2	2	3	3	2	2	9
72	2408TCSE04	Prince Bhawali	2	2	2	3	3	2	2	10

SUSTHANT UNIVERSITY
School of Engineering and Technology





CO ₁	Attachment Level
CO ₂	3
CO ₃	3
CO ₄	3

Assignment Level	Assignment Level 3	Assignment Level 2	Assignment Level 1
Level 3	Highly technical, requires extensive research and analysis.	Technical, requires some research and analysis.	Basic, requires minimal research and analysis.
Level 2	Technical, requires some research and analysis.	Technical, requires some research and analysis.	Basic, requires minimal research and analysis.
Level 1	Basic, requires minimal research and analysis.	Basic, requires minimal research and analysis.	Basic, requires minimal research and analysis.

9	10	8	6	5	4	3	2	1
Average Marks	Max Marks	Min Marks	Std Deviation	Less than	More than	90%	80%	75.2%
89.00%	92.85	86.00%	8.00	89.00%	90.00%	90%	80%	75.2%

Assignment

SUSHANT UNIVERSITY

School of Engineering and Technology
Mid-Term Examination (Odd Semester 2024-25)

Program: BTech
Semester: I

Course Code: 2BETC-MA11T

S.No.	Examination No.	Student Name	Course Name Mathematics I	Mid Term Date: 24/10/2024
			Final Year Name Mathematics I	
1	2408TCSE029	Amit Negi	Mathematics I	
2	2408TCSE033	Aryana Kasyap	Mathematics I	
3	2408TCSE020	Aashish Thakur	Mathematics I	
4	2408TCSE087	Aishwarya Ranje	Mathematics I	
5	2408TCSE091	Aishwarya Shukla	Mathematics I	
6	2408TCSE007	Aishwarya Shukla	Mathematics I	
7	2408TCSE079	Aishwarya Shukla	Mathematics I	
8	2408TCSE081	Aishwarya Shukla	Mathematics I	
9	2408TCSE115	Anju Kumar	Mathematics I	
10	2408TCSE077	Anupriya	Mathematics I	
11	2408TCSE033	Arav	Mathematics I	
12	2408TCSE022	Arikhan Dholayia	Mathematics I	
13	2408TCSE062	Arman Sait	Mathematics I	
14	2408TCSE023	Arpan Kumar	Mathematics I	
15	2408TCSE053	Arpan Kumar	Mathematics I	
16	2408TCSE016	Aryana Negi	Mathematics I	
17	2408TCSE053	Aryank Sharma	Mathematics I	
18	2408TCSE008	Arshik Gupta	Mathematics I	
19	2408TCSE077	Arshish Kumar Sharma	Mathematics I	
20	2408TCSE059	Arshir Malik	Mathematics I	
21	2408TCSE054	Arvita Gupta	Mathematics I	
22	2408TCSE009	Avyasha Gupta	Mathematics I	
23	2408TCSE041	Babuvi Shukla	Mathematics I	
24	2408TCSE038	Bhavika Shukla	Mathematics I	
25	2408TCSE108	Dhruv Vadev	Mathematics I	
26	2408TCSE066	Dhivya Shukla	Mathematics I	
27	2408TCSE022	Dhruv Vadev	Mathematics I	
28	2408TCSE109	Dheeksha Patel	Mathematics I	
29	2408TCSE106	Dishaani	Mathematics I	
30	2408TCSE057	Dhivya Shukla	Mathematics I	
31	2408TCSE036	Dhruv Vadev	Mathematics I	
32	2408TCSE003	Dhruv Vadev	Mathematics I	
33	2408TCSE077	Dhruv Vadev	Mathematics I	
34	2408TCSE037	Dhruv Vadev	Mathematics I	
35	2408TCSE022	Dhruv Vadev	Mathematics I	
36	2408TCSE065	Dhruv Vadev	Mathematics I	
37	2408TCSE157	Dhruv Vadev	Mathematics I	
38	2408TCSE030	Dhruv Vadev	Mathematics I	
39	2408TCSE056	Dhruv Vadev	Mathematics I	
40	2408TCSE077	Dhruv Vadev	Mathematics I	
41	2408TCSE073	Dhruv Vadev	Mathematics I	
42	2408TCSE027	Dhruv Vadev	Mathematics I	
43	2408TCSE037	Dhruv Vadev	Mathematics I	
44	2408TCSE062	Dhruv Vadev	Mathematics I	
45	2408TCSE028	Dhruv Vadev	Mathematics I	
46	2408TCSE069	Dhruv Vadev	Mathematics I	
47	2408TCSE090	Dhruv Vadev	Mathematics I	
48	2408TCSE055	Dhruv Vadev	Mathematics I	
49	2408TCSE050	Dhruv Vadev	Mathematics I	
50	2408TCSE026	Dhruv Vadev	Mathematics I	
51	2408TCSE119	Dhruv Vadev	Mathematics I	
52	2408TCSE113	Dhruv Vadev	Mathematics I	
53	2408TCSE022	Dhruv Vadev	Mathematics I	
54	2408TCSE027	Dhruv Vadev	Mathematics I	
55	2408TCSE070	Dhruv Vadev	Mathematics I	
56	2408TCSE041	Dhruv Vadev	Mathematics I	
57	2408TCSE061	Dhruv Vadev	Mathematics I	
58	2408TCSE085	Dhruv Vadev	Mathematics I	
59	2408TCSE114	Dhruv Vadev	Mathematics I	
60	2408TCSE25	Dhruv Vadev	Mathematics I	
61	2408TCSE021	Dhruv Vadev	Mathematics I	
62	2408TCSE001	Dhruv Vadev	Mathematics I	
63	2408TCSE021	Dhruv Vadev	Mathematics I	
64	2408TCSE045	Dhruv Vadev	Mathematics I	
65	2408TCSE028	Dhruv Vadev	Mathematics I	
66	2408TCSE088	Dhruv Vadev	Mathematics I	
67	2408TCSE198	Dhruv Vadev	Mathematics I	
68	2408TCSE005	Dhruv Vadev	Mathematics I	
69	2408TCSE076	Dhruv Vadev	Mathematics I	
70	2408TCSE071	Dhruv Vadev	Mathematics I	
71	2408TCSE028	Dhruv Vadev	Mathematics I	
72	2408TCSE004	Dhruv Vadev	Mathematics I	





M. R. M. S.

CO2	Administrative Level
CO1	

Avg. All-inclusive Marks	
Mid-Term	
(Level 1)	Less than 50% students scoring more than average % marks.
(Level 2)	50% to less than 60% students scoring more than average % marks.
(Level 3)	More than 60% students scoring more than average % marks.

Prts	Ents	G-10	11-12	21-20	12-20	0-10	21-30	0	10	20	30	40	50
Mid-Term		26	1	15	0	0	0	0	0	0	0	0	0

Roll No	Name	Matr. Marks	Min Marks	Sid	Loss	Drops	More than 90%	Avg. %	Total Students	Average	Total Subjects	Total Students Appeared in Mid-term (N)	No. of students scored average% and above marks (P)	CD Strainment (PN=100)	60.00%	44.00%
103	2408TCCSE011	Triyanshi Yadav	2	AB	AB	AB	AB	AB	1	0	1	109	95	44	109	109
102	2408TCCSE010	Vanshika Kausik	4	1	3	4	1	4	4	4	4	12	8	8	13	13
101	2408TCCSE014	Vanshika Kausik	4	2	4	2	6	2	2	2	2	21	8	8	22	22
100	2408TCCSE013	Vanshika Kausik	4	1	0	2	2	2	2	2	2	22	8	8	22	22
99	2408TCCSE013	Vanshika Kausik	4	3	4	1	7	4	4	4	4	14	8	8	16	16
98	2408TCCSE03	Vanshika Kausik	3	3	4	1	7	4	4	4	4	12	4	4	16	16
97	2408TCCSE03	Vanshika Kausik	3	3	4	1	7	4	4	4	4	12	4	4	16	16
96	2408TCCSE06	Uma	4	3	4	4	7	4	4	4	4	18	8	8	21	21
95	2408TCCSE07	Tanushka Gupta	4	4	4	1	4	4	4	4	4	13	5	5	18	18
94	2408TCCSE049	Tanushka Gupta	2	3	1	1	7	4	4	4	4	17	9	9	26	26
93	2408TCCSE015	Soham Gupta	4	3	3	3	7	5	5	5	5	17	9	9	25	25
92	2408TCCSE039	Soham Gupta	4	4	4	1	7	5	5	5	5	16	9	9	25	25
91	2408TCCSE092	Soham Gupta	4	3	4	4	4	4	4	4	4	15	9	9	20	20
90	2408TCCSE101	Soham Gupta	4	3	4	4	4	4	4	4	4	12	5	5	17	17
89	2408TCCSE114	Soham Gupta	4	2	4	1	7	1	1	1	1	14	5	5	19	19
88	2408TCCSE04	Soham Gupta	3	0	3	1	7	2	7	7	7	12	5	5	12	12
87	2408TCCSE120	Soham Gupta	4	2	4	1	7	1	1	1	1	11	0	0	11	11
86	2408TCCSE056	Soham Gupta	4	2	4	1	7	1	1	1	1	6	0	0	12	12
85	2408TCCSE040	Soham Gupta	1	3	3	1	4	4	4	4	4	9	8	8	17	17
84	2408TCCSE074	Soham Gupta	2	3	4	2	2	2	2	2	2	9	8	8	18	18
83	2408TCCSE089	Soham Gupta	4	3	4	2	2	2	2	2	2	9	8	8	18	18
82	2408TCCSE093	Soham Gupta	2	3	4	2	2	2	2	2	2	9	8	8	18	18
81	2408TCCSE086	Soham Gupta	3	4	4	4	7	4	4	4	4	18	8	8	26	26
80	2408TCCSE066	Soham Gupta	2	3	0	1	0	0	0	0	0	6	2	2	8	8
79	2408TCCSE088	Soham Gupta	2	3	0	2	3	4	4	4	4	17	9	9	21	21
78	2408TCCSE002	Rossanne Henrie	4	3	4	1	5	4	4	4	4	13	8	8	15	15
77	2408TCCSE052	Ritesh Kumar	4	3	3	2	3	4	4	4	4	13	8	8	21	21
76	2408TCCSE060	Ritesh Kumar	4	3	3	1	7	1	1	1	1	15	0	0	8	8
75	2408TCCSE121	Ritesh Kumar	4	2	1	1	4	3	4	4	4	10	4	4	14	14
74	2408TCCSE116	Rakesh Kumar	4	1	1	4	3	4	6	4	4	10	4	4	10	10
73	2408TCCSE107	Rakesh Kumar	4	2	1	1	4	3	4	6	4	10	4	4	14	14



John W.

School of Emerging and Technological End Term Examinations (Odd Semester 2022-23)

Student Full Name	Survey	Attainment of survey parameter 1	Attainment of survey parameter 2	Attainment of survey parameter 3	Attainment of survey parameter 4	Date of Survey: 28/12/2024	Program: B.Tech	Course Name: Mathematics I	Faculty Name: Dr. Manimala
Aarti Negi	Very Good	20	Very Good	20	Very Good	CO2	CO1	CO3	Sem: I
Aaryan Kashyap	Very Good	20	Very Good	20	Very Good				Academic Year - Even Semester 2023-24
Aashi Thakran	Very Good	20	Very Good	20	Very Good				School of Engineering and Technology, Sushant University, Gurugram
Abhinav Raniga	Very Good	20	Very Good	20	Very Good				Course Code: 23BTC-0MA11T
Akshat Shukla	Good	18	Very Good	20	Very Good				Course Name: Mathematics I
Aditya Chaudhary	Excellent	20	Excellent	20	Excellent				Faculty Name: Dr. Manimala
Akshit Matnur	Very Good	18	Very Good	20	Very Good				Date of Survey: 28/12/2024
Ankit Nagar	Very Good	20	Very Good	20	Very Good				
Annu Kumar	Excellent	20	Excellent	20	Excellent				
Arav	Good	18	Good	20	Good				
Arish Dahiya	Very Good	20	Very Good	20	Very Good				
Arman Sait	Excellent	20	Excellent	20	Excellent				
Arpan Kumar	Excellent	20	Excellent	20	Excellent				
Arpan Napti	Very Good	20	Good	18	Good				
Ashish Kumar Sharma	Very Good	20	Very Good	20	Very Good				
Ashish Gupta	Good	18	Very Good	20	Excellent				
Avinash	Excellent	20	Excellent	20	Excellent				
Ayusha Gupta	Good	18	Good	20	Excellent				
Bhavik Chawla	Very Good	20	Very Good	20	Very Good				
Dhruv Vadav	Very Good	18	Good	18	Good				
Dishant	Excellent	20	Excellent	20	Excellent				
Divyanshu Kaushik	Very Good	20	Very Good	20	Very Good				
Drishtika Anelia	Very Good	20	Good	18	Good				
Faizan Khan	Excellent	20	Very Good	20	Excellent				
Harshit Sharma	Very Good	18	Very Good	20	Excellent				
Harshit Chhillar	Good	18	Very Good	20	Excellent				
Harshit Kumar Pandey	Very Good	20	Very Good	20	Excellent				
HARSHITA KAKKAR	Excellent	20	Very Good	20	Excellent				
Jai Kumar Jha	Good	18	Good	20	Very Good				
Jatin Rana	Very Good	20	Very Good	20	Very Good				
Jayant Gaur	Very Good	20	Very Good	20	Excellent				
Kanishka Srivastava	Very Good	20	Very Good	20	Excellent				
Kanishka Vadav	Excellent	20	Very Good	20	Excellent				
Krishna Gemlji	Very Good	18	Very Good	20	Excellent				
Kumar Aryan	Very Good	20	Very Good	20	Excellent				
Kunal Joon	Excellent	20	Excellent	20	Very Good				
Kunjal Joon	Excellent	20	Excellent	20	Very Good				
Kyathika Rao Seelam	Good	18	Good	18	Good				



John M. Dill



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Mohit Hameza	Very Good	20	Excellent	20	Bxcellent	20	Very Good	18
Narej Rana	Very Good	20	Very Good	20	Very Good	20	Very Good	18
Nikhil Patel	Very Good	20	Very Good	20	Excellent	20	Excellent	20
Nitin Shethawat	Very Good	20	Excellent	20	Excellent	20	Very Good	20
Palk Shrivastava	Very Good	20	Very Good	20	Excellent	20	Very Good	20
Parneeta	Very Good	18	Good	20	Bxcellent	20	Very Good	20
Pavay Yadav	Very Good	20	Very Good	20	Excellent	20	Very Good	20
Piyush Choubey	Very Good	20	Very Good	20	Excellent	20	Very Good	20
Poorav Yadav	Very Good	20	Very Good	20	Excellent	20	Very Good	20
Prashant Sharma	Good	20	Very Good	20	Excellent	20	Very Good	18
Rahul Shekawat	Very Good	20	Very Good	20	Excellent	20	Very Good	18
RAJ ARYAN	Very Good	20	Very Good	20	Excellent	20	Very Good	20
Ritesh Kumar	Good	18	Good	20	Excellent	20	Very Good	20
Ritesh Meenak	Very Good	20	Very Good	20	Excellent	20	Very Good	18
Rupesh Singh	Very Good	20	Excellent	20	Excellent	20	Very Good	20
Saraa Tewaria	Very Good	20	Very Good	20	Excellent	20	Very Good	20
Sameer Patwa	Good	20	Very Good	18	Good	20	Excellent	18
Sana Ghosh	Very Good	18	Good	20	Excellent	20	Very Good	20
Sanjeev Kumar	Very Good	20	Very Good	20	Good	18	Good	18
Sarthak Mehta	Very Good	20	Very Good	20	Excellent	20	Very Good	20
Sarvit Upadhyay	Good	20	Excellent	20	Excellent	20	Very Good	20
Shiv Kumar Ray	Good	18	Good	20	Very Good	20	Very Good	20
Shubham Tamwar	Very Good	18	Good	20	Very Good	20	Very Good	18
Soham Verma	Very Good	20						
Stritra Parshica	Very Good	20	Very Good	20	Excellent	20	Very Good	20
Tanishka Gupta	Good	20	Excellent	20	Excellent	20	Very Good	18
Tanviya Malik	Very Good	20	Very Good	20	Good	20	Very Good	20
Unnati	Very Good	20	Very Good	20	Excellent	20	Very Good	20



John Mathew

Assessment Methods		Attainment Levels	Assessment
50% students scoring more marks.	Level 1	50% to less than average%	Assessment
50% students scoring more marks.	Level 2	50% to less than average%	Assessment
50% students scoring more marks.	Level 3	60% students scoring more marks than average	Assessment
60% students scoring more marks than average		% marks in	than average



M. P. S.

COs	Direct (80%)	Indirect (20%)	Total (100%)
CO1	2.25	3	2.4
CO2	1.65	3	1.92
CO3	1.35	3	1.68

SUSHANT UNIVERSITY
SCHOOL OF ENGINEERING AND TECHNOLOGY
CO Attainment
Sem-I
Program: B.Tech
Course Name: Mathematics I
Course Code: 23BTC-0MATT
Faculty Name: Dr. Manimala
Date of Analysis: 28/12/2024

SCHOOL OF ENGINEERING AND TECHNOLOGY						
Result Analysis (Even Semester 2023-24)						
Program:B.Tech	Sem:	Course Name: Mathematics I	Course Code:23BTC-0MA11T	Faculty Name:Dr. Manimala	Date of Analysis:28/12/2024	
COs	Mid-Term	Assignment	Quiz	Total	Mid term 15 : Assignment/Presentation 25	Consolidated CO Attainment (Midterm)
CO1	2	3	3	2.625	2.625	Mid term 40 : Assignment/Quiz 60
CO2	2	3	3	2.625	2.625	Consolidated CO Attainment (Midterm+Extreme)
COs	Mid-Term	Assignment	Quiz	Total	(Mid term+Assignment+Presentation)	COs
CO1	2.625	2	2.25	2.25	1.65	CO2
CO2	2.625	2	2.25	2.25	1.875	CO3
CO3	1.875	1	1	1	1.35	

*Mouli
Ganguly*





Mauraj

COs	P01	P02	P03	P04	P05	P06	P07	P08	P09	P010	P011	P012	P01	P02	P03
CO1=2A	72	72	24	24	24	48	24	24	48	48	48	72	72	24	
CO2=192	5.76	5.76	1.92	3.84	3.84	3.84	3.84	3.84	1.92	5.76	1.92	3.84	5.76	1.92	
CO3=304	5.04	5.04	1.68	5.04	3.36	5.04	3.36	1.68	3.36	5.04	1.68	3.36	5.04	1.68	
Attestment	2.00	2.00	2.00	1.88	1.92	1.95	1.88	1.92	2.00	1.99	2.10	2.12	2.00	2.00	

CO3	3	3	1	1	2	2	3	3	2	1	2	2	1	1	1
CO2	3	3	1	1	1	1	1	1	2	2	3	3	1	1	1
CO1	3	3	1	1	1	1	1	1	2	1	2	1	1	1	1
COs	P01	P02	P03	P04	P05	P06	P07	P08	P09	P010	P011	P012	P01	P02	P03

Program: B.Tech	CO-PO-PSO Mapping	Date of Analysis: 28/12/2024
Course Name: Mathematics I	Faculty Name: Dr. Manimala	Course Code: 23BTC-OMA11T

SUSHANT UNIVERSITY
SCHOOL OF ENGINEERING AND TECHNOLOGY
Sem: I

EP:	Total
AB:	Absent
DP:	Debarred
DE:	Defered
UFM:	Unfair Means
	Pass with Grade Marks

SUSHANT UNIVERSITY, SECTOR-55, GURGAON
End Semester Examination: Regular (December, 2024)
B.Tech - CSE- Semester-1

Sub Code		23BTE-CED1C	23BTE-0EE1C	23BTE-0IP1C	23BTE-0MA17	23BTE-0PY1C	23BTE-0NS1C	24BYC-0PY1C	EVS211	SEL11									
Subject Name		Engineering Graphics & Design	Basics of Electronics and Electrical Engineering	Introduction to Programming	Mathematics-I	Physics	Workshop	Python	Environmental Studies	Universal Human Values									
S.No	Student Roll Number	Student Name	SGPA	Exam Name	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	
1	240BTCCSE001	NIMAI PANDEY	7.000	External	-	-	63	B	73	B+	61	B	-	-	87	A+	76	A	
2	240BTCCSE002	ROSSANE HENRICK	-	Internal	-	-	37	45	38	-	-	-	52	48	44	73	B+	78	
				External	-	-	26	28	28.5	-	-	-	35	28	29	-	-	78	
				Internal	-	-	-	-	-	-	-	-	-	-	-	-	-	-	
3	240BTCCSE003	DRISHKA ANEJA	9.095	External	80	A	-	-	96	D	84	A	97	0	-	-	90	A+	91
				Internal	45	-	-	-	56	-	48	60	-	-	-	-	55	52	-
4	240BTCCSE004	PRINCE BHARDWAJ	9.238	External	-	-	95	0	90	A+	91	A+	-	-	-	-	35	39	92
				Internal	35	-	-	-	40	-	35.5	37	-	-	-	-	56	57	-
5	240BTCCSE005	PYUSH CHOUDHARY	7.905	External	-	-	81	A	83	A	77	A	-	-	-	-	35	37	93
				Internal	-	-	49	47	46	-	-	-	55	47	47	-	31	33	-
6	240BTCCSE006	SAARA TEMATHIA	8.095	External	-	-	76	A	83	A	70	B+	-	-	-	-	35	27	78
				Internal	-	-	45	48	44	-	-	-	56	56	56	-	31	33	-
7	240BTCCSE007	AKSHAT SHUKLA	7.475	External	79	A	-	-	83	A	68	A+	74	B+	-	-	84	A	78
				Internal	49	-	-	-	49	-	38	44	-	-	-	-	52	45	-
8	240BTCCSE008	ASTIK GUPTA	7.905	External	62	B	-	-	81	A	77	A	88	A+	-	-	85	A+	69
				Internal	36	-	-	-	45	-	43	35	-	-	-	-	53	52	-
9	240BTCCSE009	AYESHA GUPTA	8.952	External	45	A+	-	-	36	A+	88	A+	80	A	97	O	-	-	88
				Internal	39.5	-	-	-	51	-	42	60	-	-	-	-	54	45	-
				External	39	-	-	-	37	-	37.5	37	-	-	-	-	34	-	92

S. K. Shukla
 Prepared By:

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Controller of Examinations

16/11/25

Legend	
TP:	Total
ABS:	Absent
DB:	Defered
DE:	Deferred
UFM:	Unfair Means
*:	Pass with Grade Marks

SUSHANT UNIVERSITY, SECTOR-55, GURGAON
End Semester Examination: Regular (December, 2024)
B.Tech - CSE- Semester-1

Sub Code		23BTC-0ED1C	23BTC-0EE1C	23BTC-0IP1C	23BTC-0MA1C	23BTC-0PY1C	23BTC-0WS1C	24BTC-0PV1C	EVS211	SE151	
S.No	Student Roll Number	Subject Name	Subject Name	Engineering Graphics & Design	Basics of Electronics and Electrical Engineering	Introduction to Programming	Mathematical Physics	Workshop	Python	Environmental Studies	Universal Human Values
		Total Credit Point (21)		3	5	4	4	5	3	1	2
10	2408TCCSE010	SOHAM VERMA	9.852	EP External	-	72 B+	91 A+	74 B+	-	90 A+	93 A+
11	2408TCCSE011	YUKASHI YADAV	0.952	EP Internal	-	44 B	54 A	41 B+	-	57 A+	55 A+
12	2408TCCSE012	MAYANK KAUSHIK	9.095	EP External	-	38 F	37 F	33 C	-	33 C	38 B
13	2408TCCSE013	KANISHK GAUR	8.762	EP Internal	-	14 D	23 C	31 B	-	22 D	0 F
14	2408TCCSE014	WICKH PRAKASH KUMAR	5.143	EP External	-	95 O	95 O	95 O	-	0 F	0 F
15	2408TCCSE015	TAKSH ROOP SRIVASTAVA	7.361	EP External	-	82 A	81 A	85 A-	-	86 A+	75 A
16	2408TCCSE016	ARYAN NAPIT	6.810	EP Internal	-	46 B	55 A	97 A	0 F	80 A	90 A+
17	2408TCCSE017	JAYANT GAUR	5.952	EP External	-	20 D	25 C	22 B	-	81 A	64 B
18	2408TCCSE018	HARSHIT KUMAR PANDEY	8.714	EP Internal	-	62 B	79 A	74 B+	-	29 B	77 A
				25	33	45	42	-	52 B	42 B	27 B
				33	32	-	-	-	22 B	22 B	-
				66 B	57 C	72 B+	-	-	85 A+	56 C	94 A+
				37 B	24 C	44 B+	-	-	53 A+	32 B	-
				29 B	32.5 C	28 B	-	-	32 B	24 B	94 A+
				55 C	47 D	75 A	-	-	58 C	65 B	74 B+
				32 B	29 C	48 B+	-	-	44 B	33 B	-
				23 B	24 C	27 B	-	-	14 B	32 B	-
				94 A+	84 A	91 A+	-	-	94 A+	74 B+	95 O
				57 B	45 C	51 B	-	-	57 B	39 B	-
				37 B	38.5 C	40 B	-	-	37 B	35 B	-
				40	-	-	-	-	95 O	-	-
				37	-	-	-	-	-	-	-

Shweta
Prepared By:

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Legend
EP : Total
ABSENT : Absent
DEBARRED : Debarred
DEFERRED : Deferred
UHM : Unfair Means
PWM : Pass With Grace Marks

SUSHANT UNIVERSITY, SECTOR-55, GURGAON
End Semester Examination: Regular (December, 2024)
B.Tech - CSE- Semester-1

Sub Code	238TC-0ED1C	238TC-0EE1C	238TC-0IP1C	238TC-0MATH1	238TC-0PY1C	238TC-0WS1C	248TC-0PY1C	EVS211	SE151
Subject Name									
Total Credit Point (21)									
3 5 5 4 4 5 3 1 2 2									
S.No Student Roll Number Student Name SGPA Exam Name Marks Grade Marks Grade Marks Grade Marks Grade Marks Grade Marks Grade Marks Grade									
19 2408TCCSE020 AASHI THAKRAN 5.905 EP 69 B - - 56 C 42 D 72 B+ - - 88 A+ 44 0 93 A+									
20 2408TCCSE021 NIKHIL PATEL 7.143 External 34 - - - 30 C 42 D 72 B+ - - 88 A+ 44 0 93 A+									
21 2408TCCSE022 DHRUV YADAV 2.857 EP 45 D - - 35 F 26 F 51 C - - 71 B+ 16 F 82 A									
22 2408TCCSE023 ARPIT KUMAR 5.571 External 30 - - - 19 4 19 C - - 40 ABS									
23 2408TCCSE024 PALAK SHRIVASTAV 6.048 Internal 15 C - - 16 D+ 21.5 32 31 31 31 31 16 82 82 A									
24 2408TCCSE025 NAKESH KUMAR 6.048 EP - - 54 C 66 B 42 D+ - - 87 A+ 70 B+ 61 8 82 A									
25 2408TCCSE026 HARSHIT CHHILLAR 5.476 EP 43 D - - 55 C 53 C 61 B - - 70 B+ 68 B 73 B+									
26 2408TCCSE028 PRASHANT SHARMA 7.619 External 10 - - 70 B+ 84 A 63 B - - 92 A+ 82 A 87 A+									
27 2408TCCSE029 AARTI NEGI 9.286 External 97 0 - - 33 36 30.5 A+ 81 A 100 0 - - 90 A+ 91 A+ 96 0									
Result Withheld*									
Internal External Internal External									
Controller of Examinations 16/11/2025									

S. Kumar
Prepared By:

Total	
EP:	Total
AB:	Absent
OB:	Deferred
DE:	Deferred
UFL:	Unfiled
PF:	Pass
NP:	No Pass

SUSHANT UNIVERSITY, SECTOR-55, GURUGRAM
End Semester Examination: Regular (December, 2024)
B.Tech - CSE- Semester-1

Sub Code		23BTC-0ED1C	23BTC-0EE1C	23BTC-0IP1C	23BTC-0MMA1T	23BYC-0PV1C	23BTC-0WS1C	24BTC-0PY1C	EVS211	SE151											
Subject Name		Engineering Graphics & Design	Basics of Electronics and Electrical Engineering		Introduction to Mathematics-I		Physics		Workshop	Python	Environmental Studies		Universal Human Values								
S.No	Student Roll Number	Student Name	SGPA	Exam Name	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	
Total Credit Point(21)																					
31	240BTCCSE033	HIMANSHU KUMAR CHAUDHARY	7.286	External	47	A	-	-	73	B+	55	C	93	A+	76	A	61	B	77	A	
32	240BTCCSE034	YASHI YADAV	5.619	External	31	-	-	-	30	32.5	55	48	48	-	34	-	28	-	27	-	
33	240BTCCSE035	VARSHA	7.810	External	41	B+	46	B+	43	A-	82	A	88	A+	73	B+	93	A+	41	A+	
34	240BTCCSE036	JAIKUMAR JHA	4.571	External	49	D	58	C	31	F	-	-	80	A	64	B	68	B	72	B+	
35	240BTCCSE037	KANISHKA SRIVASTAVA	6.190	External	87	A+	-	-	57	C	54	C	58	C	-	-	80	A	63	B	
36	240BTCCSE038	BHAVIK SHANKAR	4.190	External	49	D	29	24	33	-	50	-	52	C	58	C	-	85	A+	35	F
				Internal	38	F	28	30	25	-	30	-	31	C	30	-	30	30	90	A+	
				Internal	18	-	-	-	23	-	-	-	30	-	19	-	52	-	19	-	
				Internal	8	-	-	-	18	28.5	-	-	33	-	16	-	33	-	93	-	

S. K. Singh
 Prepared By:

Legend	
EP:	Totl
AB:	Absent
OB:	Debarred
DE:	Deferred
UFA:	Inferior Marks
PAS:	Pass with Grade Marks

SUSHANT UNIVERSITY, SECTOR-55, GURGAON
End Semester Examination: Regular (December, 2024)
B.Tech - CSE- Semester-1

Sub Code		23BTC-0ED1C	23BTC-0EE1C	23BTC-0IP1C	23BTC-0M1C	23BTC-0PV1C	23BTC-0WS1C	24BTC-0PY1C	EVS211	SE51										
Subject Name		Engineering Graphics & Design	Basics of Electronics and Electrical Engineering	Introduction to Programming	Mathematics-I	Physics	Workshop	Python	Environmental Studies	Universal Human Values										
S.No	Student Roll Number	Student Name	SGPA	Exam Name	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade
37	2408TCCSE039	SUHANI GUPTA	8.285	EP	-	-	83	A	81	A	80	A	-	-	90	A+	90	A+	72	B+
				External	-	-	51	C	45	C	43	C	-	-	55	C+	55	C+	41	C
				Internal	-	-	32	C	36	C	37	C	-	-	35	C-	35	C-	31	C
38	2408TCCSE040	SARTHAK MENTA	5.667	EP	-	-	52	C	52	C	61	B	-	-	64	B	76	A	45	D
				External	-	-	31	C	29	C	35	C	-	-	38	B	48	A	83	A
				Internal	-	-	21	C	23	C	26	C	-	-	26	C	28	B	20	B
39	2408TCCSE041	BHAVIK CHAWLA	4.143	EP	49	D	-	-	57	C	53	C	35	F	-	-	87	A+	43	D
				External	28	-	-	-	33	C	40	C	20	-	-	53	C	19	A+	-
				Internal	21	-	-	-	24	C	27	C	15	-	-	34	C	29	A+	94
40	2408TCCSE042	KANISHKA YADAV	7.429	EP	71	B+	-	-	81	A	58	C	61	A	-	-	88	A+	79	A
				External	40	47	-	-	47	C	26	C	49	-	-	54	C	43	B	94
				Internal	31	-	-	-	34	C	32	C	32	-	-	34	C	36	A	92
41	2408TCCSE043	ARAV	5.810	EP	70	B+	-	-	59	C	52	C	52	C	-	-	76	A	54	C
				External	43	-	-	-	30	C	24	C	24	-	-	48	B	22	B	89
				Internal	27	-	-	-	29	C	28	C	28	-	-	28	C	32	A+	89
42	2408TCCSE044	FAIZAN KHAN		EP	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
				External	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-
43	2408TCCSE046	KVATHIKA RAO SEELAM	9.571	EP	96	O	-	-	95	O	94	A+	97	O	-	-	90	A+	87	A+
				External	57	-	-	-	56	C	60	C	-	-	-	55	C	47	-	-
				Internal	39	-	-	-	40	C	38.5	C	37	-	-	35	C	40	94	-
44	2408TCCSE047	ASHISH KUMAR SHARMA	7.476	EP	67	B	-	-	78	A	69	B	94	A+	-	-	84	A	62	B
				External	42	-	-	-	45	C	36	C	54	C	-	-	52	B	28	A+
				Internal	25	-	-	-	33	C	32.5	C	40	-	-	32	C	34	92	-
45	2408TCCSE048	PARNEETA	6.000	EP	-	-	-	-	64	B	55	C	-	-	-	83	A	78	A	84
				External	-	-	-	-	27	C	29	C	-	-	-	50	C	48	A	43
				Internal	-	-	-	-	19	C	25.5	C	-	-	-	33	C	30	B	27
				-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-

Result Withheld*

Subject Name	23BTC-0ED1C	23BTC-0EE1C	23BTC-0IP1C	23BTC-0M1C	23BTC-0PV1C	23BTC-0WS1C	24BTC-0PY1C	EVS211	SE51
KVATHIKA RAO SEELAM	9.571	EP	96	O	-	-	95	O	94
ASHISH KUMAR SHARMA	7.476	EP	67	B	-	-	78	A	69
PARNEETA	6.000	EP	-	-	-	-	64	B	55
		External	57	-	-	-	56	C	60
		Internal	39	-	-	-	40	C	38.5
		EP	67	-	-	-	78	A	69
		External	42	-	-	-	45	C	36
		Internal	25	-	-	-	33	C	32.5
		EP	-	-	-	-	64	B	55
		External	-	-	-	-	27	C	29
		Internal	-	-	-	-	19	C	25.5

S. K. Mehta
 Prepared By:

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Controller of Examinations

16/11/25

Present	Total
Absent	
OB:	Absent
DE:	Debarred
UFM:	Unfiled Marks
Pass with Grade Marks	

SUSHANT UNIVERSITY, SECTOR-55, GURGAON
End Semester Examination: Regular (December, 2024)
B.Tech - CSE- Semester-1

Sub Code			23BTC-0901C	23BTC-09E1C	23BTC-09P1C	2301C-JWAI1	23BTC-09V1C	23BTC-09S1C	24BTC-09V1C	EVS211	SE151											
S.No	Student Roll Number	Subject Name	Engineering Graphics & Design			Basics of Electronics and Electrical Engineering			Introduction to Mathematics			Physics	Workshop	Python	Environmental Studies	Universal Human Values						
Total Credit Point (21)			3	5	4	4	4	5	3	3	1	2	2									
46	240BTCCSE049	TANISHKA GUPTA	6.238	External	-	-	77	A	78	A	84	A	-	89	A+	80	A	76	A	91	A+	
47	240BTCCSE050	KUNAL JODH	6.381	External	82	A	-	49	48	49	49	-	-	56	50	50	44	-	33	30	32	91
48	240BTCCSE051	MAVANK RATHORE	5.952	External	47	-	-	83	A	75	A	89	A+	-	88	A+	83	A	83	A+	-	
49	240BTCCSE052	RITESH MAAN	6.333	External	16	-	-	49	39	58	A+	-	-	54	43	43	-	34	31	34	40	93
50	240BTCCSE053	ASHANK SHARMA	6.333	External	-	-	-	34	35	31	31	-	-	34	34	34	-	62	59	C	72	B+
51	240BTCCSE054	AVINASH	6.333	External	-	-	53	C	70	B+	52	C	-	76	A	64	B	73	B+	84	A	
52	240BTCCSE055	KUNWAR ARVAN	5.567	External	-	-	26	C	43	30	-	-	-	50	42	45	-	-	26	22	27	33
53	240BTCCSE056	SARTHAK PANDAY	6.429	External	88	A+	-	56	C	70	B+	45	D	-	62	B	68	B	66	B	73	B+
54	240BTCCSE057	DIVYANSHU RANA	7.810	External	37	-	-	22	45	45	45	22	-	-	40	44	38	-	24	24	28	73
				Internal	-	-	25	25	25	25	25	25	25	22	22	22	24	24	24	24	27	27
				Internal	-	-	40	40	40	40	40	40	40	35	35	35	38	38	38	38	38	38
				Internal	-	-	28	28	28	28	28	28	28	26.5	26.5	26.5	29	29	29	29	29	29
				Internal	-	-	81	81	81	81	81	81	81	73	73	73	82	82	82	82	82	82
				Internal	-	-	45	45	45	45	45	45	45	42	42	42	49	49	49	49	49	49
				Internal	-	-	38	38	38	38	38	38	38	35	35	35	42	42	42	42	42	42
				Internal	-	-	35	35	35	35	35	35	35	31	31	31	37	37	37	37	37	37
				Internal	-	-	36	36	36	36	36	36	36	31	31	31	34	34	34	34	34	34
				Internal	-	-	31	31	31	31	31	31	31	-	-	-	79	79	79	79	79	79

Result Withheld*

Shweta
Prepared By:

Shweta
Page No. 12

Total	201
AB:	Absent
OB:	Debarred
DE:	Defered
NPW:	Unfair Means
Pass with Grace Marks	

SUSHANT UNIVERSITY, SECTOR-55, GURGAON
End Semester Examination: Regular (December, 2024)
B.Tech - CSE- Semester-1

Subject Name		Sub Code		23BTC-0ED11C	23BTC-0EE11C	23BTC-0IP11C	23BTC-0MATH11C	23BTC-0PY11C	23BTC-0WS11C	24BTC-0PY11C	EVS211	SE151	
S.No	Student Roll Number	Student Name	SGPA	Engineering Graphics & Design	Basics of Electronics and Electrical Engineering	Introduction to Programming	Mathematics	Physics	Workshop	Python	Environmental Studies	Universal Human Values	
55	240BTCCS058	SAMA GHOSH	5.000	External EP	3	5	4	4	5	3	1	2	
56	240BTCCS059	ATHARV MALIK	5.000	Internal EP	5	4	4	5	3	2	2	2	
57	240BTCCS060	RITESH KUMAR	5.857	External EP	48	D	65	8	49	D	A+	82	
				Internal	-	28	40	20	-	-	57	C	89
				External EP	-	20	25	28.5	-	-	51	34	-
58	240BTCCS061	MOHAMOUD ALLAELDEEN	3.000	Internal EP	33	F	46	D	30	F	33	31	23
				External	-	13	30	8	-	-	61	8	70
				Internal EP	-	20	16	22	-	-	35	45	18
59	240BTCCS062	ARMAN SAIFI	7.357	External EP	64	B	-	90	A+	61	B	92	25
				Internal	40	-	55	25	59	A+	-	84	20
				External EP	-	35	34.5	34.5	33	A	77	A	73
60	240BTCCS063	ARVAN KUMAR	6.429	External EP	61	B	-	76	A	65	B	52	31
				Internal	25	-	42	30	30	C	-	78	36
				Internal EP	36	-	34	35	23	-	-	53	92
61	240BTCCS064	MOHAMED KHLD KHLD	2.571	External EP	-	28	F	41	D	33	F	-	41
				Internal	-	9	27	8	-	-	50	C	23
				External EP	-	19	14	24.5	-	-	30	72	93
62	240BTCCS065	HARSH SHARMA	4.810	External EP	7	F	-	50	C	62	B	52	10
				Internal	7	-	29	93	B	52	C	-	-
				External EP	-	21	29	26	-	-	44	8+	-
63	240BTCCS066	MUSKIR	5.476	External EP	-	52	C	67	B	-	62	B	24
				Internal	-	26	39	74	-	-	64	8	20
				External EP	-	28	26	22	-	-	42	42	-
				Internal	-	26	21	22	-	-	25	25	-
				External EP	-	26	21	22	-	-	79	79	-

S. K. J.
Prepared By:

Page 7 of 12

Legend	
EP:	Total
AB:	Absent
DP:	Deemed
DS:	Deferred
UFAW:	Unfair Means
P:	Pass with Grade Marks

SUSHANT UNIVERSITY, SECTOR-55, GURGAON
End Semester Examination: Regular (December, 2024)
B.Tech - CSE- Semester-1

Sub Code		23BTC-0ED11C		23BTC-0EE11C		23BTC-0IP11C		23BTC-0MALL		23BTC-0PY11C		23BTC-0WS11C		24BTC-0PY11C		EVS211		SE111				
Subject Name		Engineering Graphics & Design		Basics of Electronics and Electrical Engineering		Introduction to Programming		Mathematical		Physics		Workshop		Python		Environmental Studies		Universal Human Values				
S.No	Student Roll Number	Student Name	SGPA	Exam Name	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade		
64	240BTCCSE067	UNNATI	8.285	External EP	-	-	80	A	85	A+	73	B+	-	-	91	A+	88	A+	84	A		
65	240BTCCSE068	YASHRAJ KAUSHIK	0.000	External EP	-	-	34	F	35	F	31	F	-	-	35	F	34	F	49	A+		
66	240BTCCSE059	KRISHNA GEMINI	6.000	Internal EP	-	-	0	DB	1	DB	0	DB	-	-	0	D	0	F	0	F		
67	240BTCCSE070	MAYANK SHARMA	8.905	External EP	92	A+	-	-	22	B+	48	D	-	-	84	A	57	C	30	A+		
68	240BTCCSE071	PRAGYA	8.905	External EP	53	A+	-	-	86	A+	90	A+	-	-	32	B+	27	B+	87	A+		
69	240BTCCSE074	SANJEEV KUMAR	6.905	Internal EP	69	B	-	-	71	B+	69	B	75	A	-	-	86	A+	49	D	93	A+
70	240BTCCSE075	TANIYA MAJUM	8.381	Internal EP	25	-	-	-	45	26	29.5	24	-	-	53	19	-	-	-	-	-	
71	240BTCCSE076	POORAV VADAV	8.381	Internal EP	-	-	75	A	77	A	81	A	-	-	93	33	30	-	93	92	A+	
72	240BTCCSE077	ANUPRIYA	8.619	Internal EP	-	-	42	45	44	-	-	-	56	A+	92	A+	76	A	41	A	95	O
				Internal	36	32	37	-	-	37	-	-	35	35	36	35	35	43	39	91	-	
Result Withheld*																						
External	50	49	40	A+	-	-	84	A	77	A	90	A+	-	-	94	A+	78	A	95	O		
Internal	36	35	37	A+	-	-	49	A	40	55	-	-	-	-	57	39	37	39	95	95		

S. K. Kullu
 Prepared By:

Legend	
EP :	Total
ABT :	Absent
DE :	Debarred
DF :	Deferred
UFA :	Unfair Means
Fail with Grade Marks	

SUSHANT UNIVERSITY, SECTOR-55, GURGAON
End Semester Examination: Regular (December, 2024)
B.Tech - CSE: Semester-1

Sub Code	23BTC-0ED11C	23BTC-0EE11C	23BTC-0FP11C	23BTC-0MATH11	23BTC-0PY11C	23BTC-0RS11C	24BTC-0PY11C	EVS211	SE151
Subject Name									
\$No	Student Roll Number	Student Name	SGPA	Engineering Graphics & Design	Basics of Electronics and Electrical Engineering	Introduction to Programming	Mathematical Physics	Workshop	Python
				3	5	4	4	5	3
				Exm Name	Marks	Grade	Marks	Grade	1
73	240BTCSE078	KAUSHAL YADAV	8.443	EP External	82	A	-	81	A
74	240BTCSE079	AKSHIT MATHUR	7.476	Internal	44	-	-	45	A+
75	240BTCSE080	DEEKSHA SORAI	6.667	EP External	63	B	-	36	44
76	240BTCSE081	ANKIT NAGAR	2.762	Internal	30	-	-	82	A
77	240BTCSE083	VIRINCHI YADAV	5.667	EP External	19	F	-	33	63
78	240BTCSE084	SHIV KUMAR RAY	7.381	Internal	15	-	-	34	86
79	240BTCSE085	MOHD HAMZA	6.667	External	4	-	-	16	A+
80	240BTCSE086	SAMEER PAMWA	5.762	Internal	63	B	-	13	30
81	240BTCSE087	ABHINAV RANGA	5.429	External	28	-	-	59	C
				Internal	31	-	-	40.00*	D
				External	32	-	-	37	B+
				Internal	22	-	-	17	B
				External	46	-	-	22	A+
				Internal	28	-	-	28	A
				External	74	B+	-	78	A
				Internal	78	A	-	69	B
				External	46	-	-	84	A
				Internal	37	-	-	52	B
				External	30	-	-	31.5	C
				Internal	56	C	-	32	D
				External	34	B+	-	73	A+
				Internal	44	C	-	56	A
				External	22	-	-	27	B+
				Internal	29	-	-	29	A
				External	20.5	-	-	55	B+
				Internal	35	-	-	51	C
				External	31	-	-	36	D
				Internal	32	-	-	31	A+
				External	34	-	-	34	B+
				Internal	32	-	-	34	C
				External	34	-	-	90	D
				Internal	90	A+	-	82	A
				External	70	B+	-	70	B+
				Internal	88	A+	-	88	A+
				External	47	C	-	47	B+
				Internal	28	-	-	28	A
				External	27	-	-	27	B
				Internal	95	-	-	95	C
				External	30	-	-	30	D
				Internal	74	-	-	74	A+
				External	60	B	-	60	B
				Internal	88	-	-	88	A+
				External	31	-	-	31	C
				Internal	15	-	-	15	D
				External	29	-	-	29	B+
				Internal	83	-	-	83	A+

5 Nov 2024
 Prepared By:

Legend	
GP:	Total
AB:	Absent
DE:	Deferred
UFM:	Unfair Means
* PGS with Grade Marks	

SUSHANT UNIVERSITY, SECTOR-55, GURGAON
End Semester Examination: Regular (December, 2024)
B.Tech - CSE- Semester-1

			Sub Code		23BTC0ED1C	23BTC-0EE1C	23BTC-MPL1C	7351C-00111	23BTC-0PV1C	23BTC-0NS1C	24BTC-0PY1C	EVS2111	SE151	
			Subject Name		Engineering Graphics & Design	Basics of Electronics and Electrical Engineering	Introduction to Programming	Mathematics	Physics	Workshop	Python	Environmental Studies	Universal Human Values	
S.No	Student Roll Number	Student Name	SGPA	Exam Name	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade	Marks	Grade
82	240BTCCSE010	RUPESH SINGH	6.476	External EP	-	-	63	B	71	B+	-	-	90	A+
83	240BTCCSE009	JATIN RANA	5.619	External EP	89	A+	-	-	69	B	69	D	64	B
84	240BTCCSE000	KRRISH SHARMA	8.192	Internal EP	55	F	-	-	39	C	39	D	36	C
85	240BTCCSE091	ADITYA CHAUDHARY	2.286	External EP	6	F	-	-	41	D	20	F	22	F
86	240BTCCSE092	SRITARA PASRICHA	7.905	External EP	-	-	51	C	87	A+	85	A+	78	A
87	240BTCCSE093	SAMEER VATS	-	External EP	-	-	24	C	52	B	48	B	52	B
88	240BTCCSE106	DISHANT	-	External EP	-	-	27	C	35	B	36.5	B	26	C
89	240BTCCSE107	SHRUVAT	6.610	Internal EP	53	C	-	-	81	A	59	C	75	A
90	240BTCCSE108	DHRUV YADAV	6.571	Internal EP	25	-	48	B	33	B	47	B	60	B
				Internal EP	28	-	33	B	28	B	-	-	40	B+
				External EP	46	-	66	B	60	B	67	B	20	C
				Internal	35	-	36	B	28	C	35	B	51	A
				External EP	-	-	30	C	315	C	32	C	30	A+
				Internal EP	-	-	-	-	-	-	-	-	28	-
				External EP	-	-	-	-	-	-	-	-	33	-
				Internal EP	-	-	-	-	-	-	-	-	96	-

Result Withheld*

UFM

S. Murthy
 Prepared By:

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